

Per informazioni

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QUANTITATIVE APPROACHES TO RISK ASSESSMENT AND INVESTMENT TRANSPARENCY Workshop

with the presentation of the book "A Quantitative Framework to Assess the Risk-Reward Profile of Non-Equity Products" of Marcello Minenna

GIOVANNA MARIA BOI

RITA D'ECCLESIA

HÉLYETTE GEMAN

STEFANO MARMI

DOMENICO MIGNACCA

MARCELLO MINENNA

DONGNING QU

PAOLO SIRONI

PAOLO VERZELLA

10.45 Registration11.00 Opening address

Book Presentation: A Quantitative Framework to Assess the
Risk-Reward Profile of Non-Equity Products

11.10 KEYNOTE ADDRESS - **HÉLYETTE GEMAN**

11.50 SPECIAL ADDRESS - MARCELLO MINENNA, GIOVANNA MARIA BOI,

PAOLO VERZELLA

13.00 Lunch

TECHNICAL CONTRIBUTIONS

14.00 RITA D'ECCLESIA

Risk Assessment of debt liabilities: overview and case studies"

14.30 DONGNING QU

Understanding Risks in Structured Products

15.00 PAOLO SIRONI

Enhancing competitiveness through transparent investment decision-making

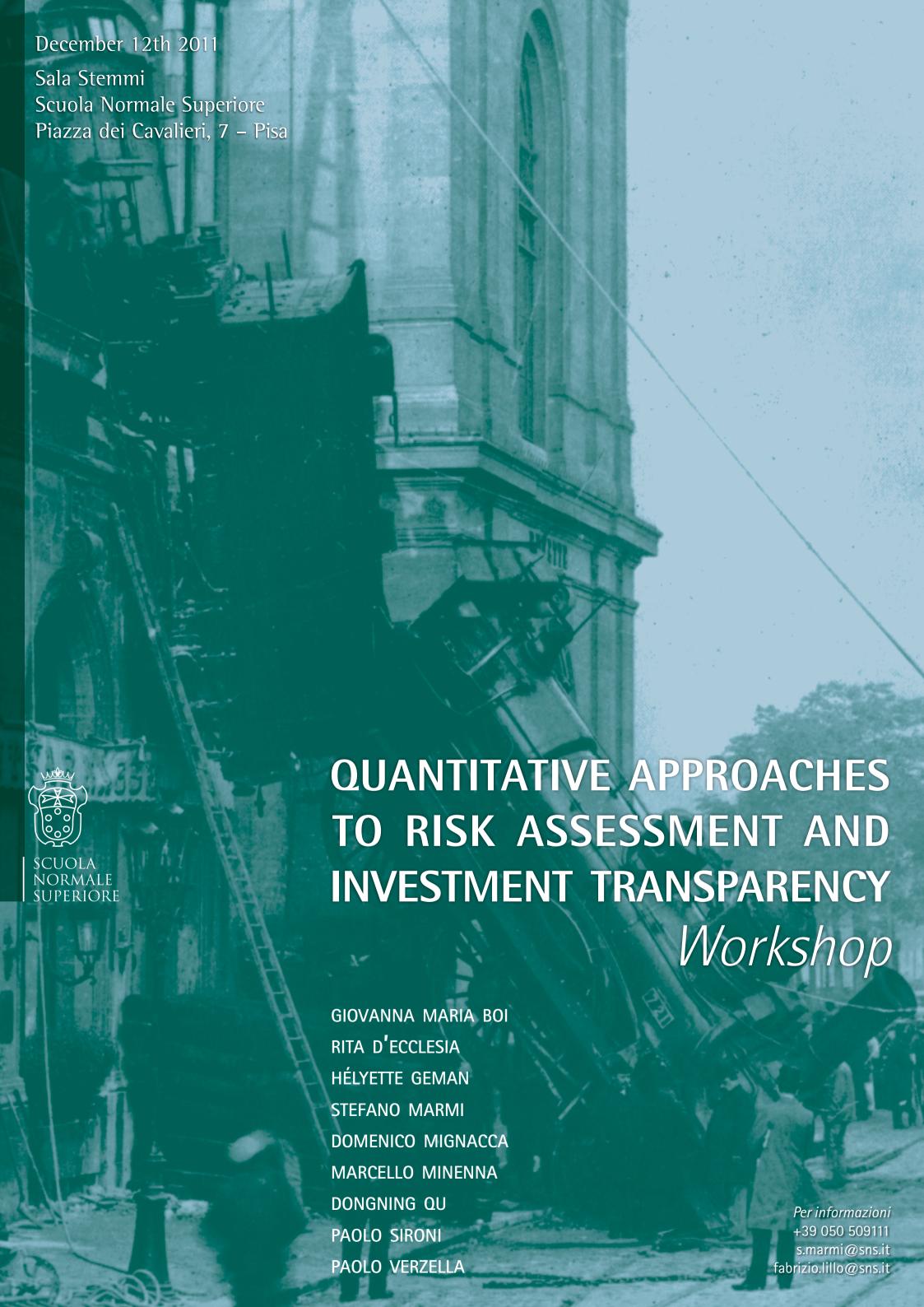
15.30 Coffee break

16.00 Round Table: **Risk Transparency through Quantitative Methods**

Moderator: STEFANO MARMI

Panelists: RITA D'ECCLESIA, HÉLYETTE GEMAN, DOMENICO MIGNACCA,

MARCELLO MINENNA, DONGNING QU, PAOLO SIRONI.



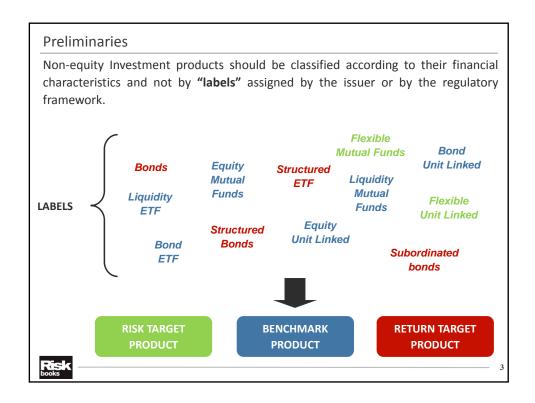


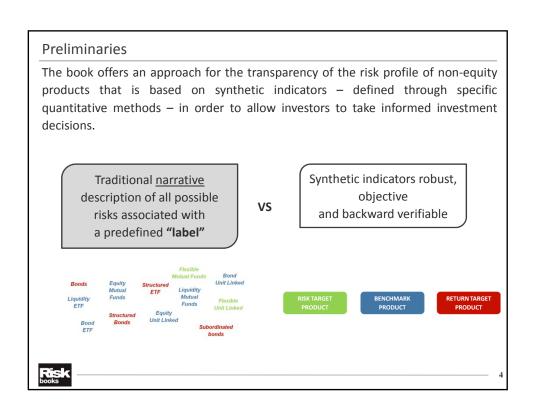
Syllabus

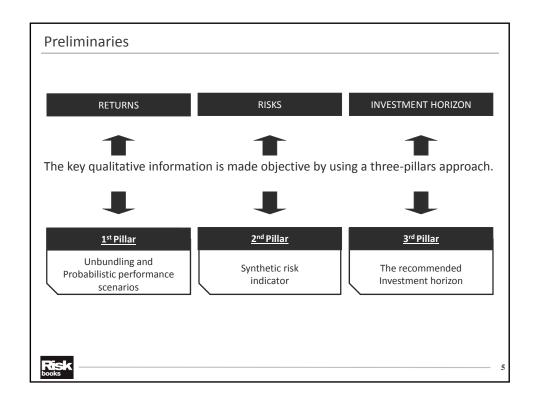
- Preliminaries: the three pillars
- The recommended Investment horizon
- Synthetic risk indicator
- Unbundling and Probabilistic performance scenarios
- An Application of the methodology

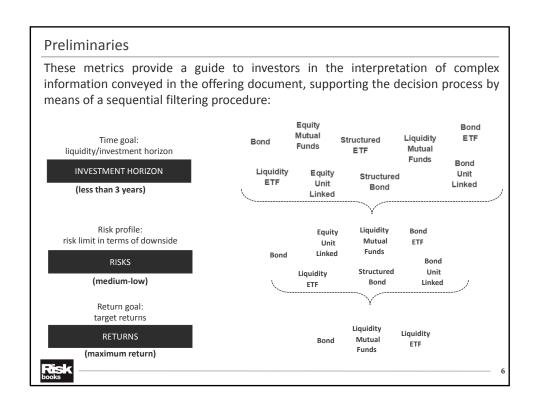


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Syllabus

- Preliminaries: the three pillars
- The recommended Investment horizon
- Synthetic risk indicator
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The recommended Investment horizon

RETURNS

RISKS

INVESTMENT HORIZON

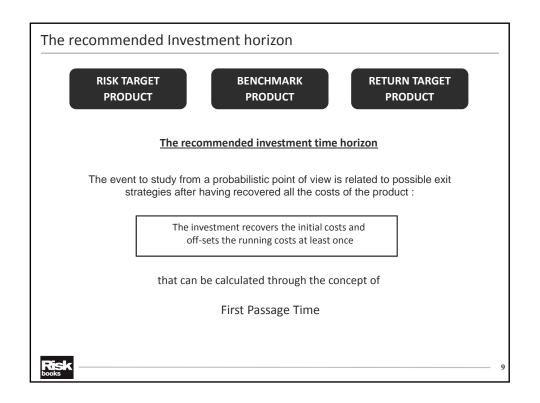
The key qualitative information is made objective by using a three-pillars approach.

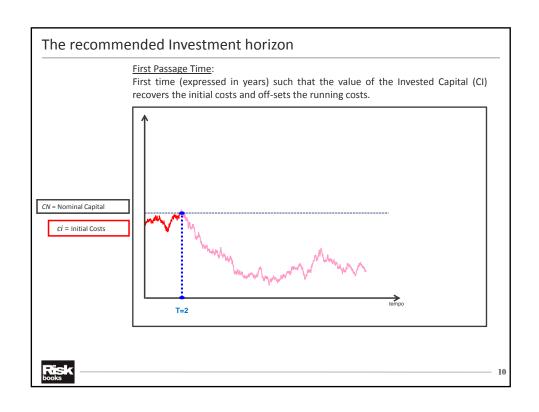
Investment Horizon

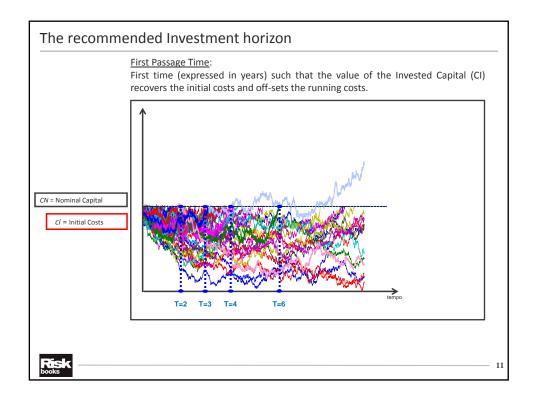
The recommended Investment horizon

Synthetic risk indicator

The recommended Investment horizon







The probability of the event:

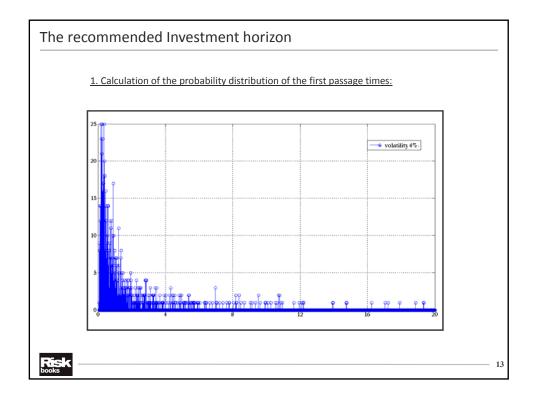
The investment recovers the initial costs and off-sets the running costs at least once

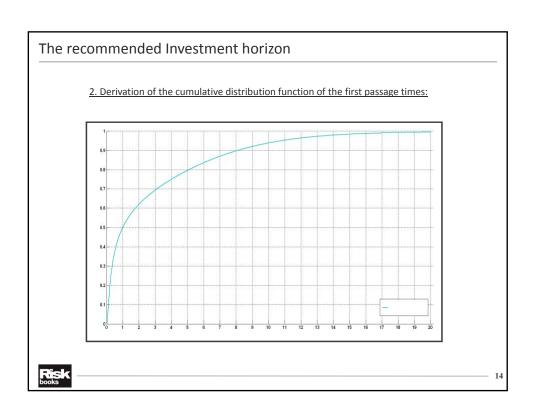
given a confidence level α , uniquely identifies a time \emph{T}^* on the cumulative distribution function of the first passage times, i.e.:

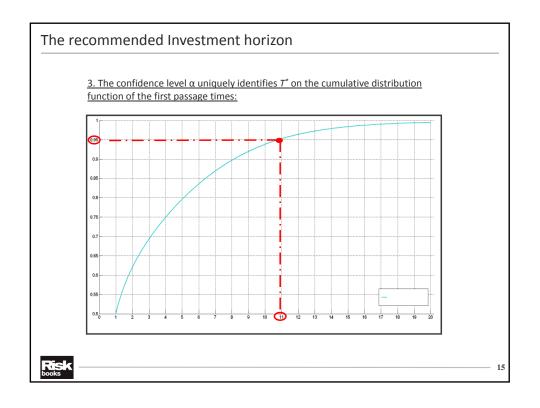
$$T^* = \left\{ T \in \mathfrak{R}^+ : P[t^* \le T] = \alpha \right\}$$
where
$$t^* = \inf[t \in \mathfrak{R}^+ : CI_t > CN]$$

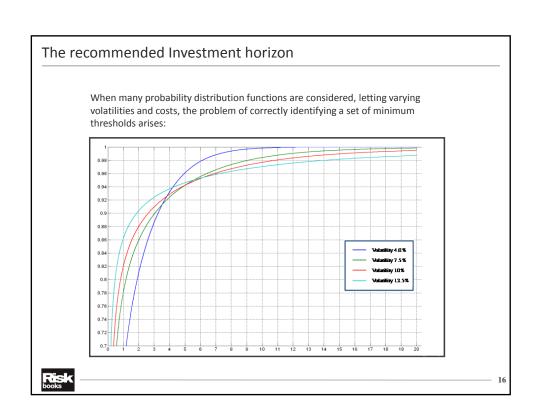
$$t^* = \inf \left[t \in \mathfrak{R}^+ : CI_t > CN \right]$$

is the first passage time









Anyway, the recommended minimum investment time horizon...

$$T^* = \left\{ T \in \mathfrak{R}^+ : P[t^* \le T] = \alpha \right\}$$



.... Must be coherent with the principle

+ VOLATILITY + TIME HORIZON



The correct way to solve the problem is to set up an operative procedure to select properly each threshold according to the above principle

Risk books

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The recommended Investment horizon

Connection between probability, volatility and costs

<u>First passage times for the break-even barrier are monitored at infinitesimal time intervals:</u>



 $dt \rightarrow 0$

$$T^* = \left\{ T \in \mathfrak{R}^+ : P\left[t^* \le T\right] = \alpha \right\}$$

$$P\left[t^* \le T\right] = N\left(d_2\left(\frac{CI_0}{CN}\right)\right) + \left(\frac{CN}{CI_0}\right)^{\frac{2(\bar{r}-cr)}{\sigma^2}-1} \cdot N\left(-d_2\left(\frac{CN}{CI_0}\right)\right)$$

$$d_2(x) = \frac{\log x + \left(\bar{r}-cr-\frac{1}{2}\sigma^2\right)T}{\sigma\sqrt{T}}$$

$$N(x) = \int_{-\pi}^{x} \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2} dz$$

Risk books

Connection between probability, volatility and costs

Asymptotic properties: $T \rightarrow \infty$

cr: recurrent costs as a fixed %

 $\lim_{T \to \infty} P[t^* \le T] = \begin{cases} 1 & \text{if } (\bar{r} - cr) \ge \frac{1}{2}\sigma^2 \\ \left(\frac{CN}{CI_0}\right)^{\frac{2(\bar{r} - cr)}{\sigma^2} - 1} & \text{if } (\bar{r} - cr) < \frac{1}{2}\sigma^2 \end{cases}$

Dooks

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The recommended Investment horizon

Connection between probability, volatility and costs

<u>Under our assumptions:</u>

 $\lim_{T \to \infty} P[t^* \le T] = \begin{cases} 1 & \text{if } (\bar{r} - cr) \ge \frac{1}{2}\sigma^2 \\ \left(\frac{CN}{CI_0}\right)^{\frac{2(\bar{r} - cr)}{\sigma^2} - 1} & \text{if } (\bar{r} - cr) < \frac{1}{2}\sigma^2 \end{cases}$

For a given level of costs, it is possible to analytically derive the connection between volatility and time horizon

Risk

The recommended Investment horizon

Connection between probability, volatility and costs

$$T \to \infty, dt \to 0$$

$$\frac{dP}{d\sigma} = \left(-4 \frac{\left(\overline{r} - cr\right)}{\sigma^3} \ln \left(\frac{CN}{CI_0} \right) \left(\frac{CN}{CI_0} \right)^{\frac{2(\overline{r} - cr)}{\sigma^2} - 1} \right)$$

$$1. \quad (\overline{r} - cr) > 0 \Leftrightarrow \frac{dP}{d\sigma} < 0$$

$$2. \quad (\overline{r} - cr) \le 0 \Leftrightarrow \frac{dP}{d\sigma} \ge 0$$

The existence of two alternative states of nature requires to verify whether both of them make sense in financial terms under the risk-neutral measure.

Risk books

Connection between probability, volatility and costs

$$\begin{split} T &\to \infty, dt \to 0 \\ \frac{d\mathbf{P}}{d\sigma} &= \left(-4\frac{\bar{r}}{\sigma^3} \ln \left(\frac{CN}{CI_0} \right) \left(\frac{CN}{CI_0} \right)^{\frac{2\bar{r}}{\sigma^2} - 1} \right) \\ 1. \quad \bar{r} &> 0 \Leftrightarrow \frac{d\mathbf{P}}{d\sigma} &< 0 \\ 2. \quad \bar{r} &\le 0 \Leftrightarrow \frac{d\mathbf{P}}{d\sigma} &\ge 0 \end{split}$$

Being running costs a specific feature of any financial product they would interfere with the task of identifying which of the two conditions has a sound financial meaning. Therefore, they will be temporarily neglected.

RISK books 23

The recommended Investment horizon

Connection between probability, volatility and costs

$$T \to \infty, dt \to 0$$

$$\frac{dP}{d\sigma} = \left(-4\frac{\bar{r}}{\sigma^3} \ln \left(\frac{CN}{CI_0} \right) \left(\frac{CN}{CI_0} \right)^{\frac{2\bar{r}}{\sigma^2} - 1} \right)$$
1. $\bar{r} > 0 \Leftrightarrow \frac{dP}{d\sigma} < 0$
2. $\bar{r} \le 0 \Leftrightarrow \frac{dP}{d\sigma} \ge 0$

Since it is safe to assume a positive interest rate r in financial markets, only condition 1. correctly captures the connection between volatility and time horizon.

Risk books

Connection between probability, volatility and costs

$$T \to \infty, dt \to 0$$

$$\frac{dP}{d\sigma} = \left(-4\frac{\bar{r}}{\sigma^3} \ln \left(\frac{CN}{CI_0} \right) \left(\frac{CN}{CI_0} \right)^{\frac{2\bar{r}}{\sigma^2} - 1} \right)$$

$$1. \quad \bar{r} > 0 \Leftrightarrow \frac{dP}{d\sigma} < 0$$

$$2. \quad \bar{r} \le 0 \Leftrightarrow \frac{dP}{d\sigma} \ge 0$$

As $T \rightarrow \infty$ condition 1. implies that the cumulative distribution function P is a strictly decreasing function of the volatility, i.e.:

$$\forall \sigma_i, \sigma_j \in \Re^+, \sigma_j > \sigma_i \Rightarrow P(\sigma_j) < P(\sigma_i)$$

Res

The recommended Investment horizon

Connection between probability, volatility and costs

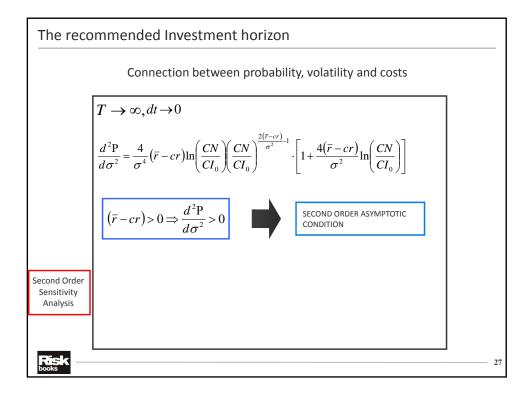
$$T \to \infty, dt \to 0$$

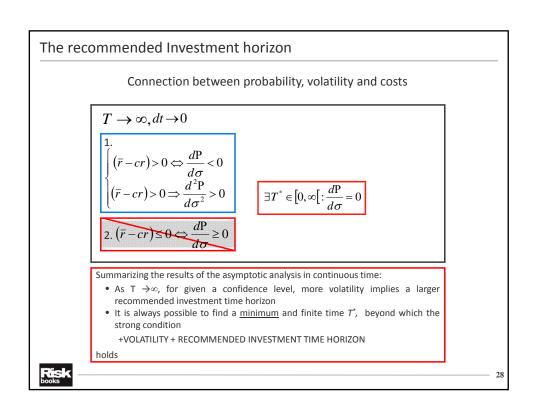
$$\frac{dP}{d\sigma} = \left(-4\frac{\bar{r}}{\sigma^3} \ln\left(\frac{CN}{CI_0}\right) \left(\frac{CN}{CI_0}\right)^{\frac{2\bar{r}}{\sigma^2} - 1} \right)$$
1. $\bar{r} > 0 \Leftrightarrow \frac{dP}{d\sigma} < 0$
2. $\bar{r} \le 0 \Leftrightarrow \frac{dP}{d\sigma} \ge 0$

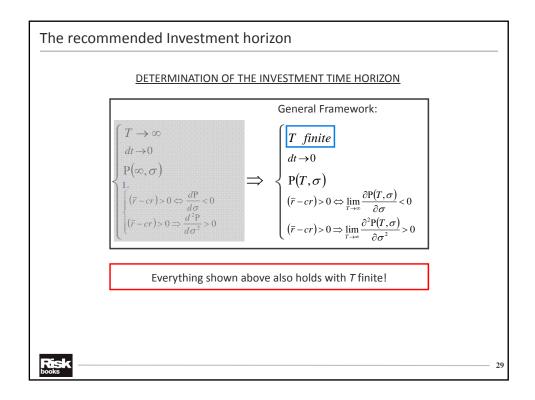
In other words, for a given a confidence level, as the volatility grows, the recommended investment time horizon increases as well:

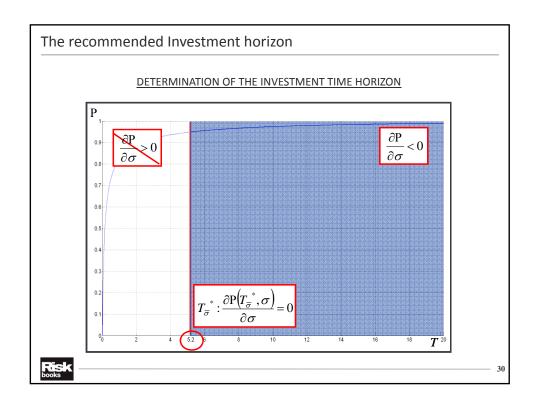
+VOLATILITY + RECOMMENDED INVESTMENT TIME HORIZON

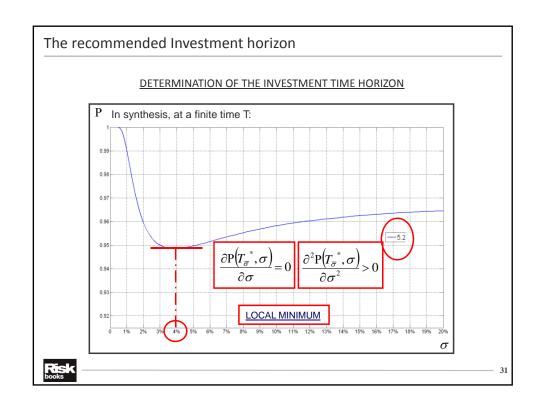
Risk

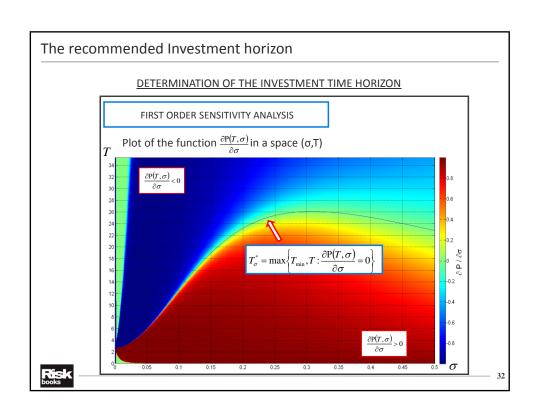


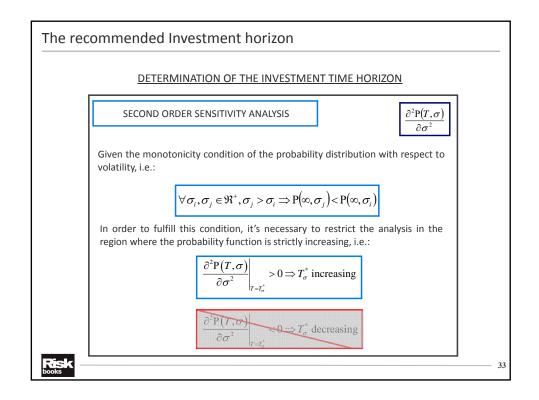


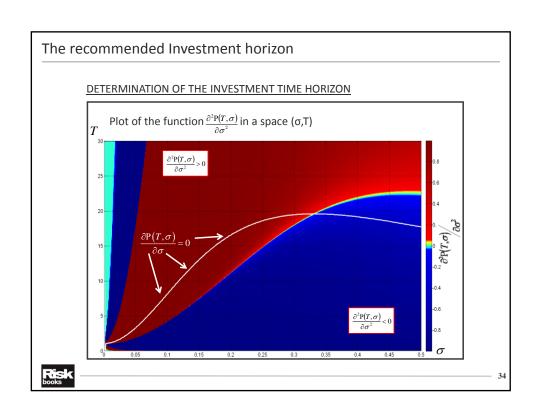


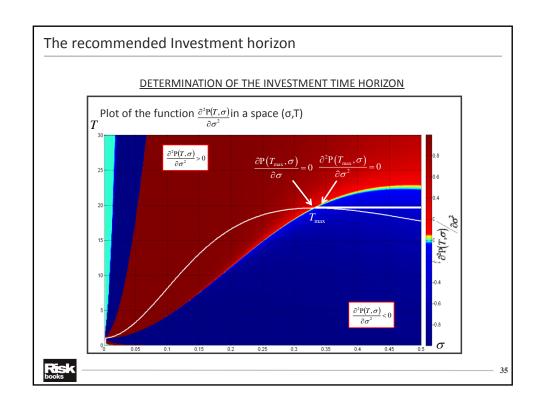


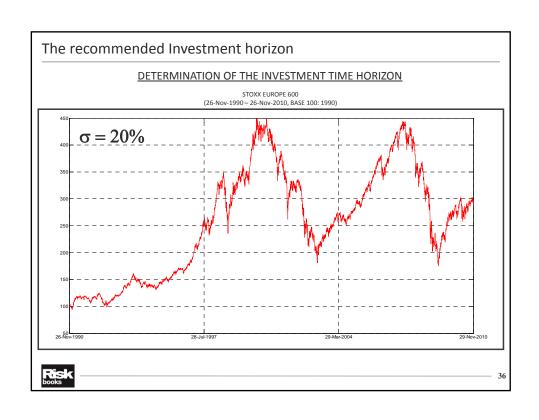


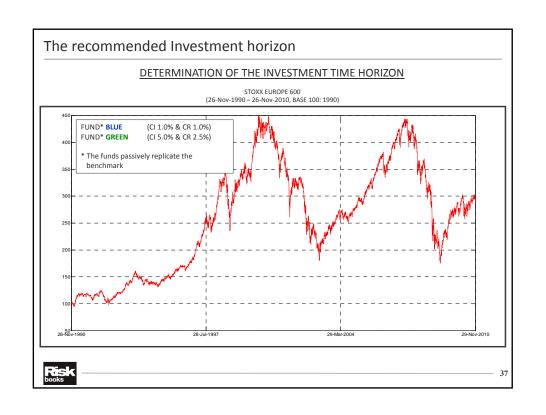


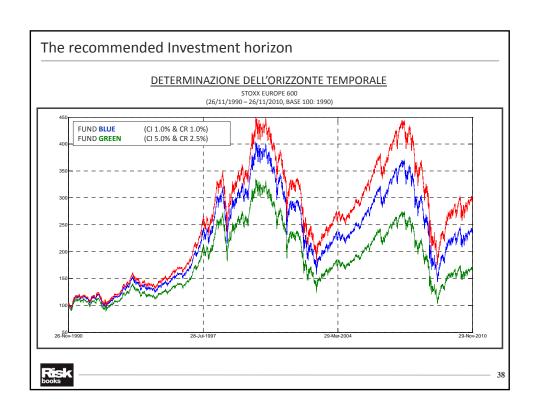


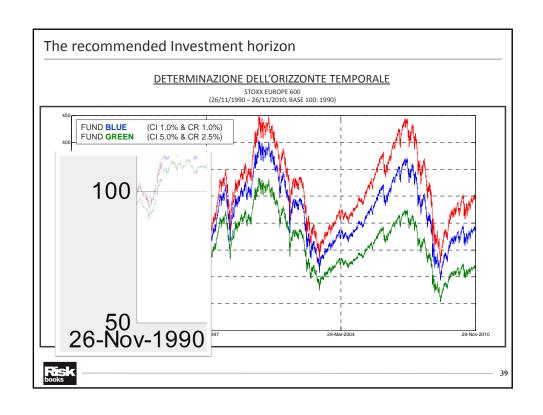


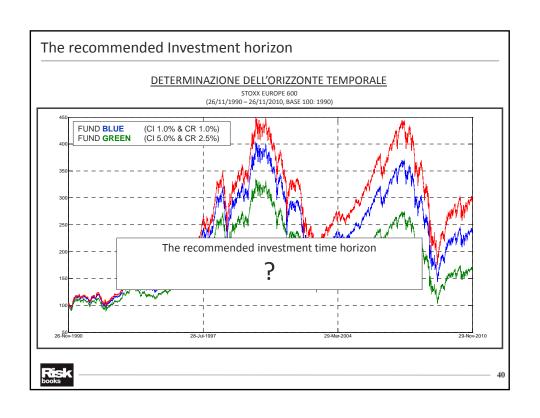


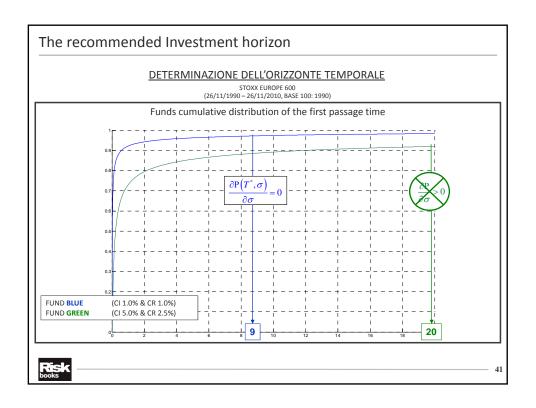








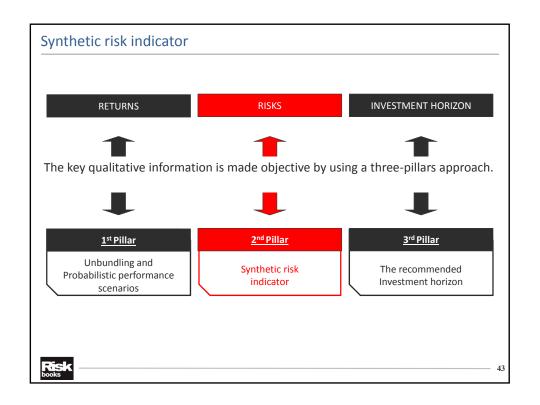


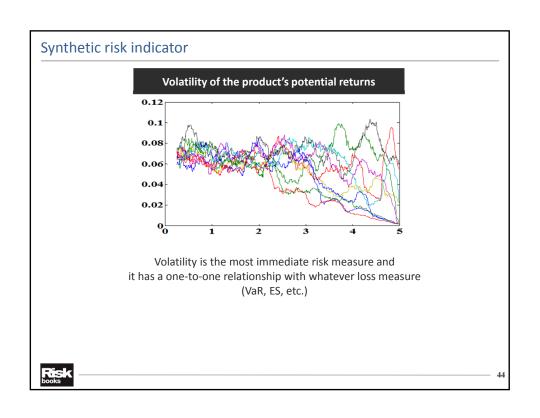


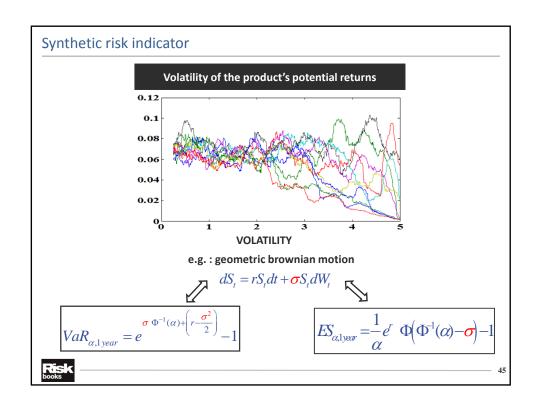
Syllabus

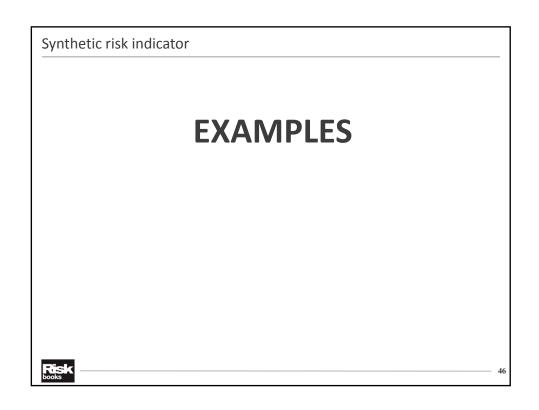
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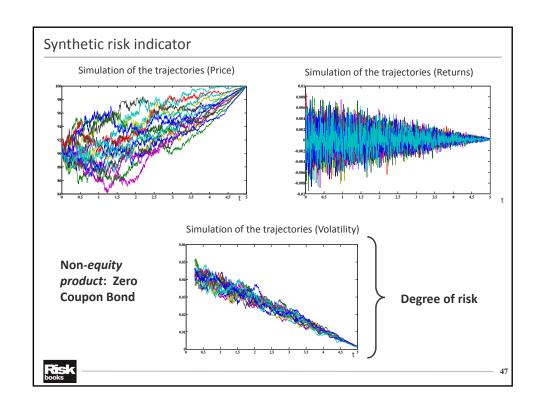
Risk

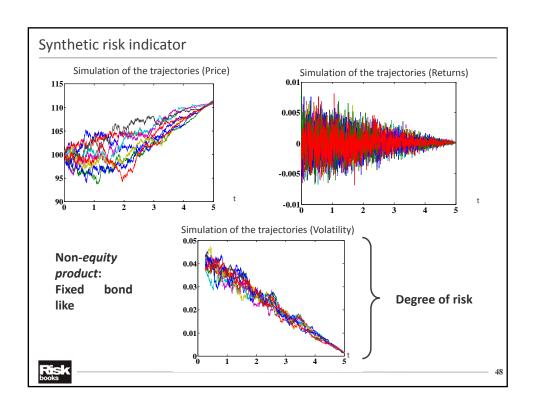


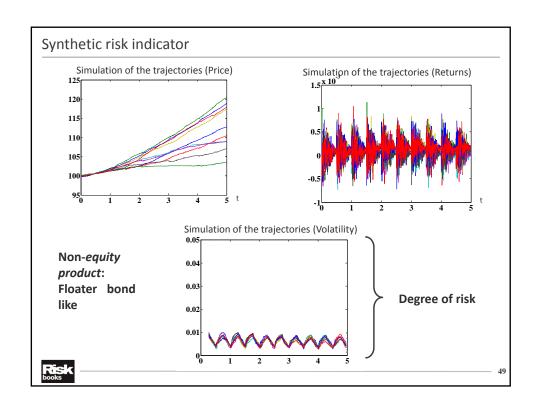


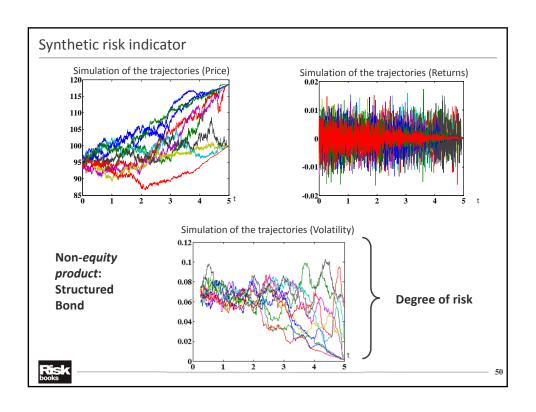


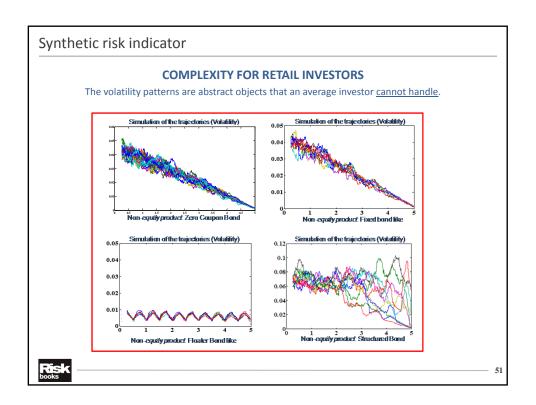






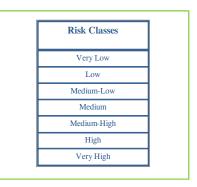






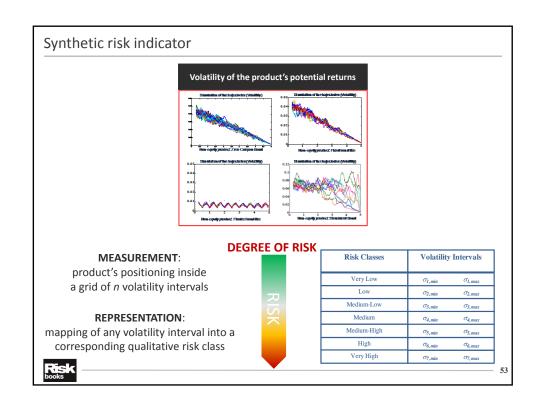
Synthetic risk indicator

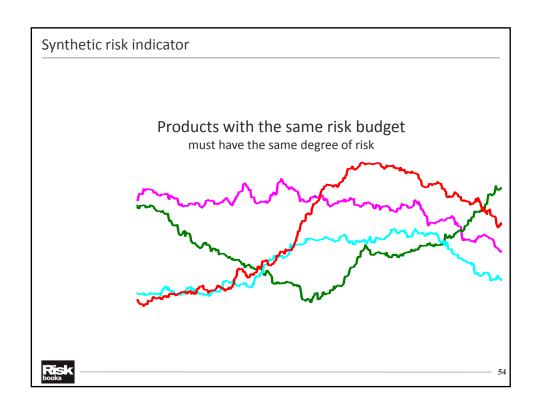
Conversely, a table with qualitative labels that characterizes the risk classes is very easy to understand

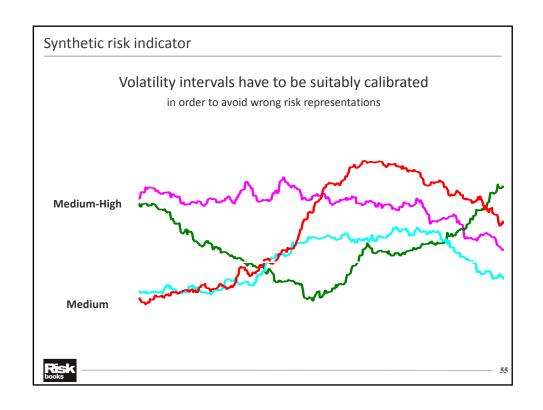


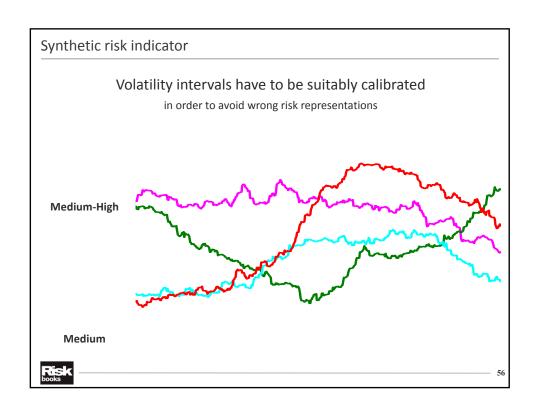
The assignment of the degree of risk is made according to a quantitative criterion that maps coherently any volatility interval into a corresponding qualitative risk class

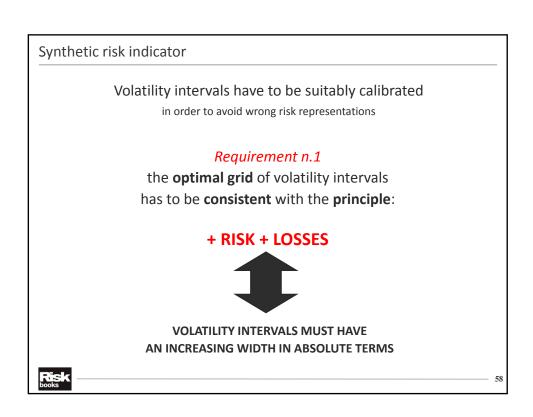
Risk books











Synthetic risk indicator

Volatility intervals have to be suitably calibrated

in order to avoid wrong risk representations

Requirement n.2

the optimal grid of volatility intervals must be

market feasible



REALIZED VOLATILITY CONSISTENT WITH MARKET EXPECTATIONS OF FUTURE VOLATILITY

(UNLESS FOR SIGNIFICANT SUDDEN SHOCKS)



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Synthetic risk indicator

Realized volatility

Any product on the markets reflects specific/different asset management policies

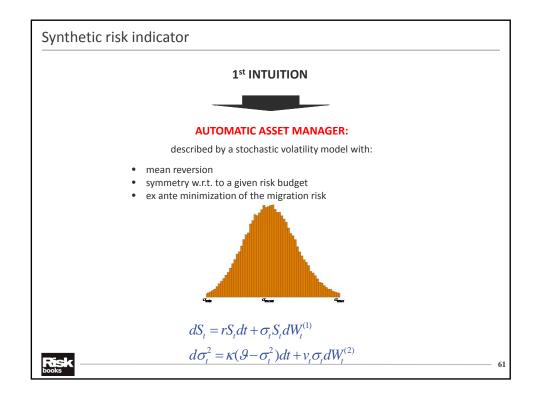
Historical data can be "dirty"

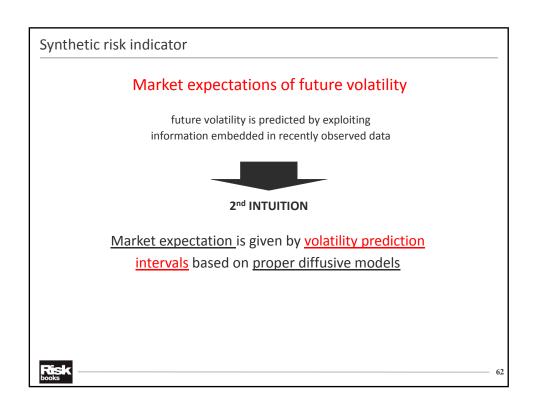


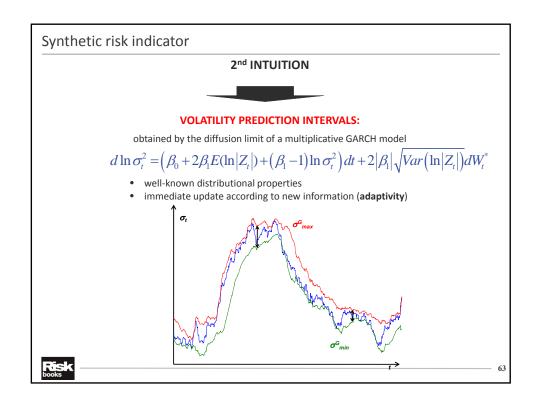
1st INTUITION

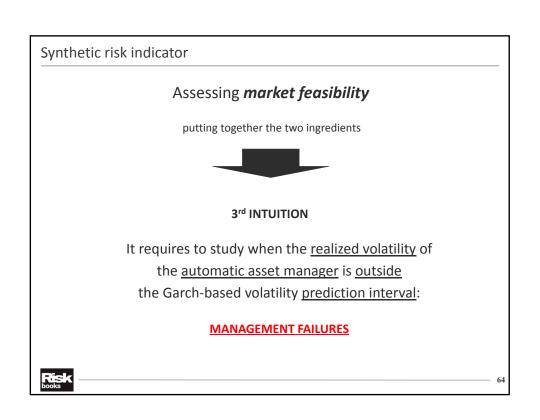
It has to be studied a <u>theoretical product</u> managed by an <u>automatic asset manager</u> who has <u>a specific risk budget</u>, identified by <u>a given volatility interval</u>

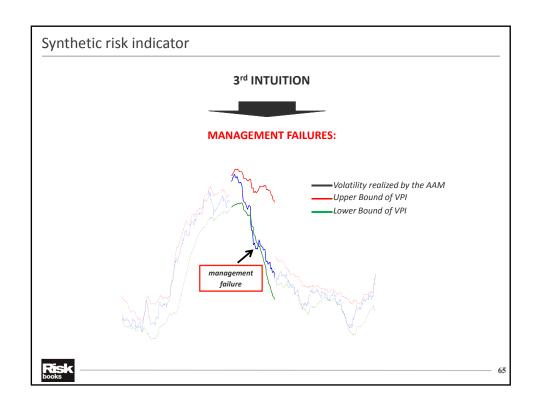


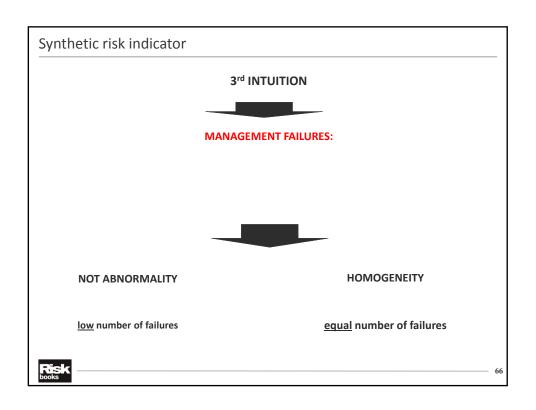


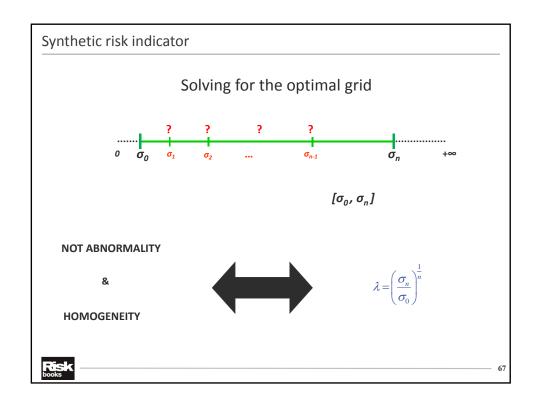


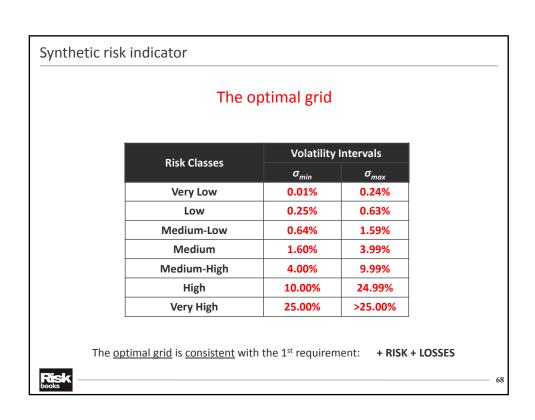


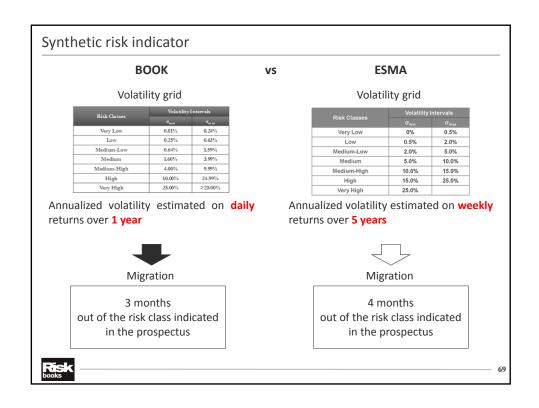


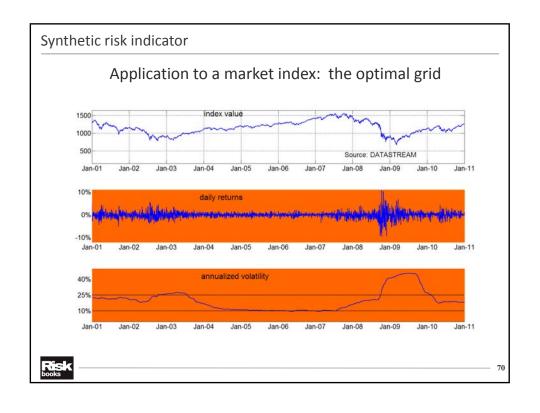


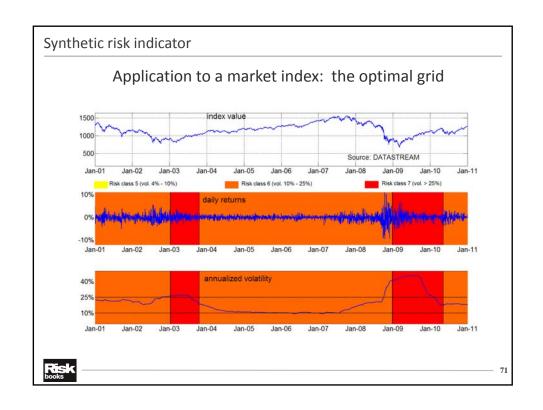


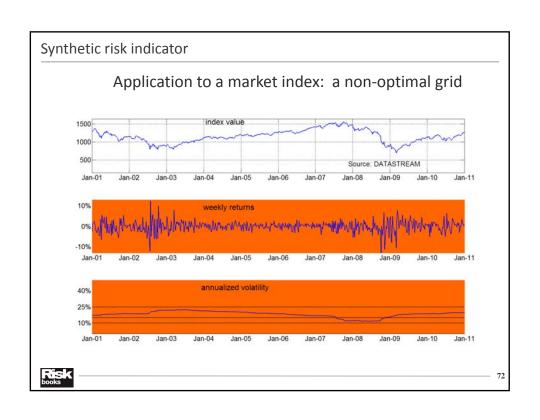


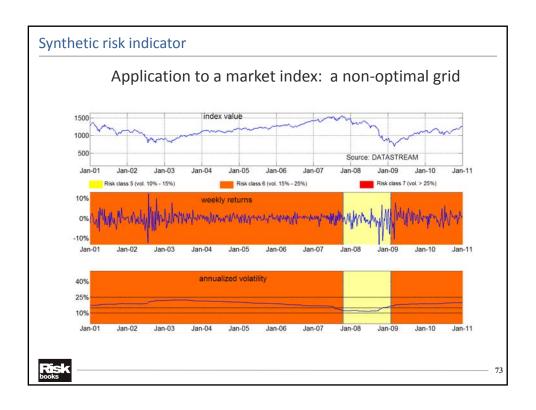










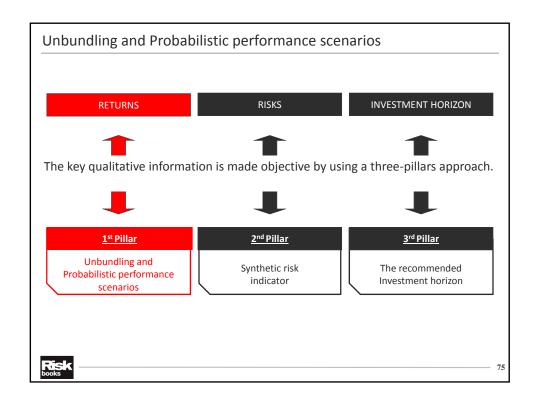


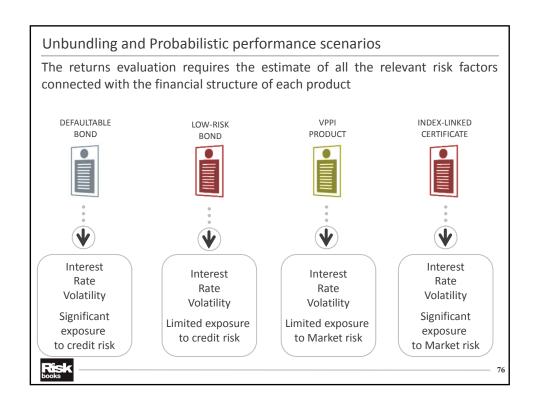
Syllabus

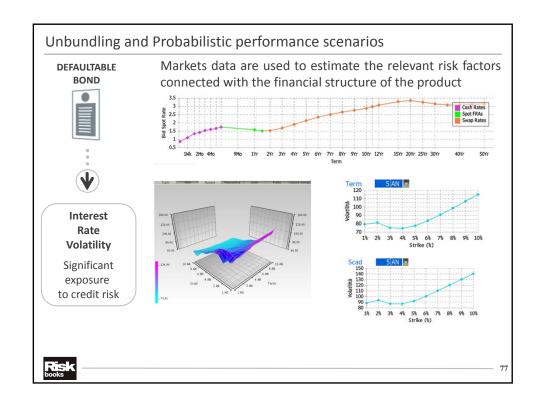
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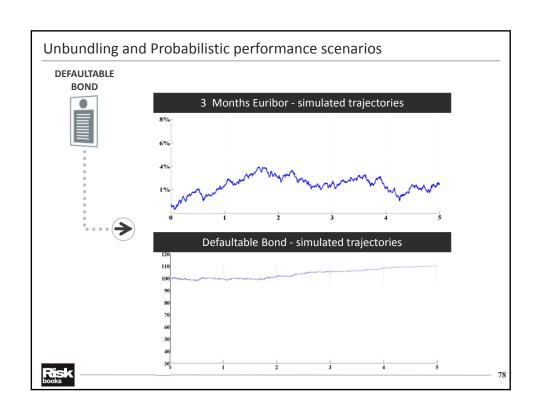
Risk

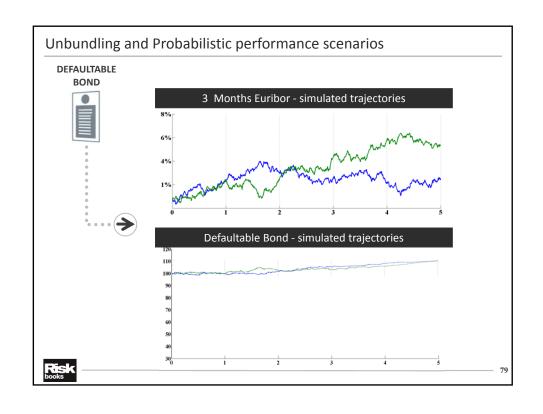
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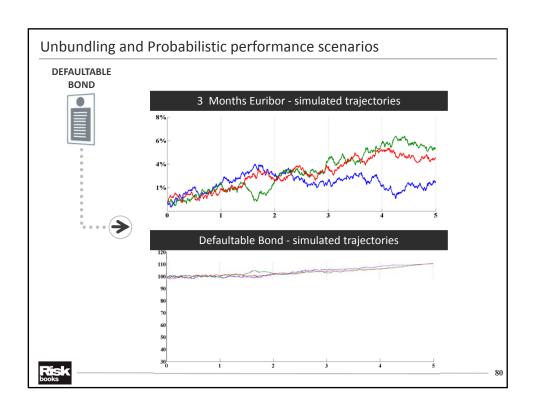


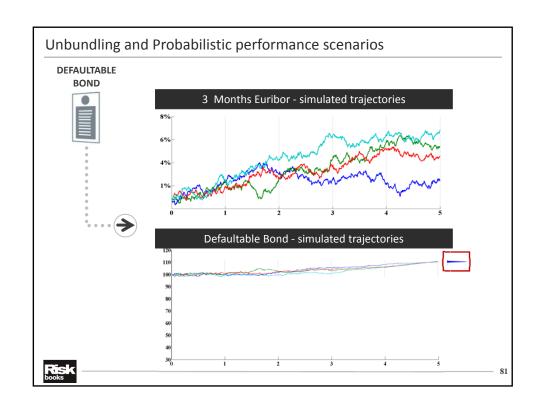


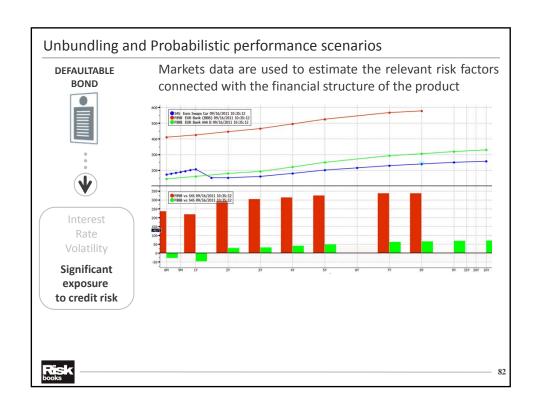


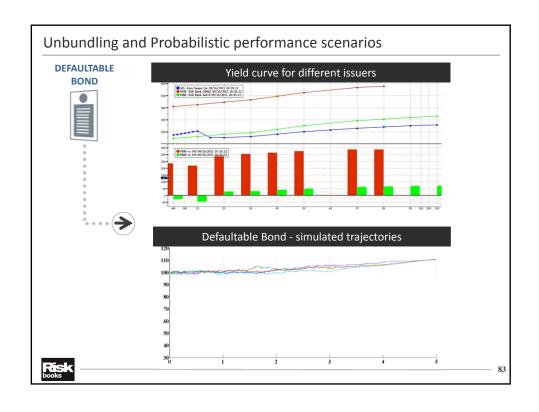


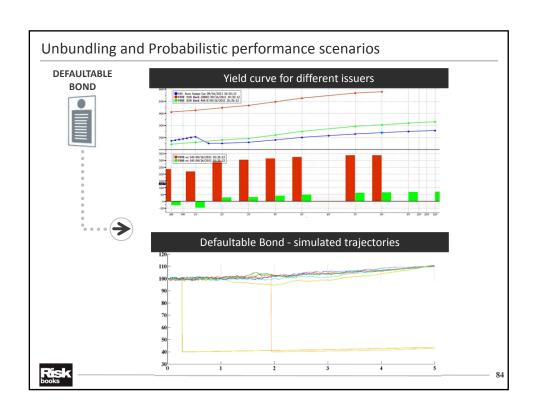


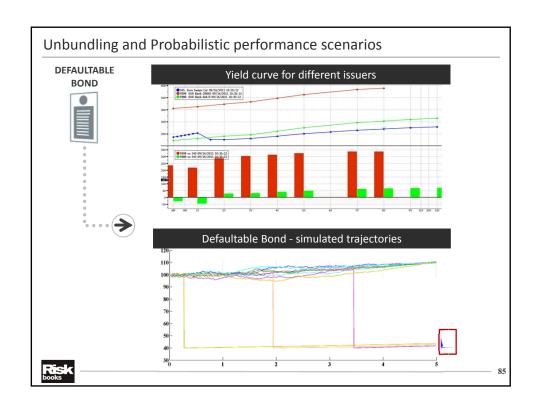


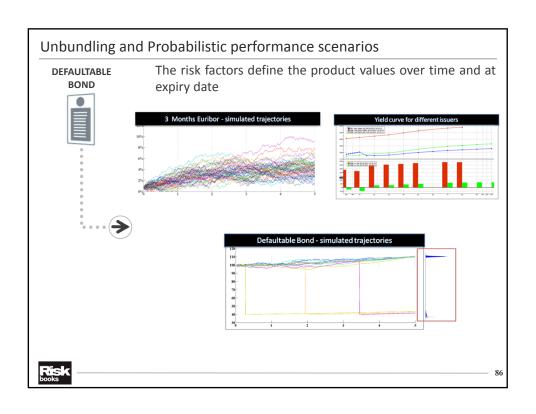


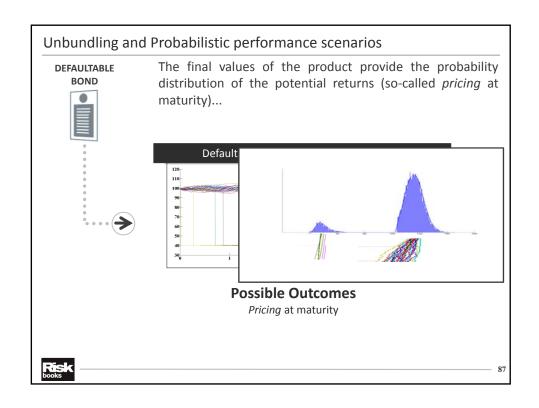


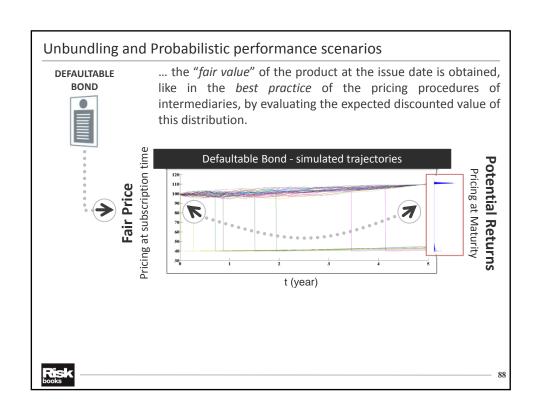


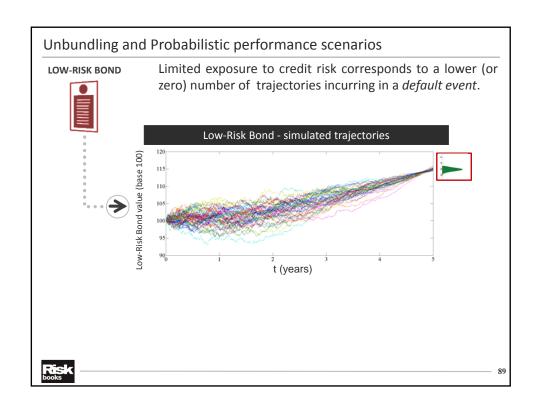


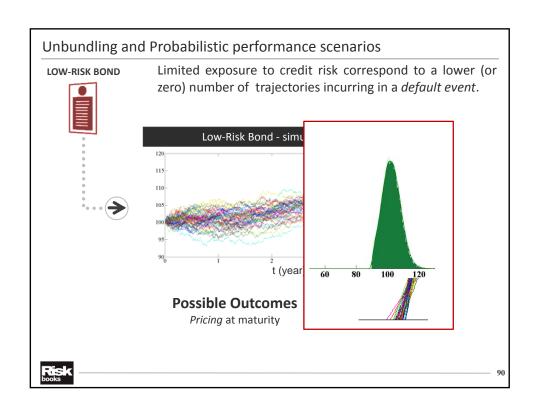


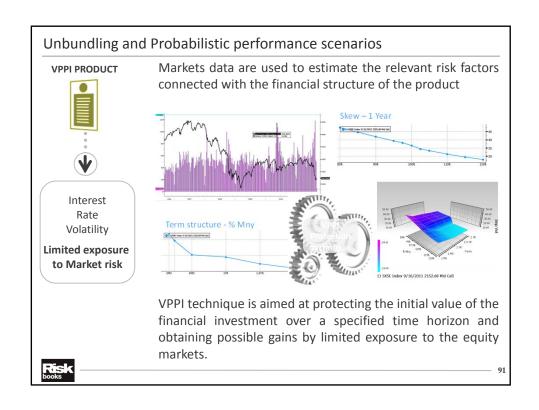


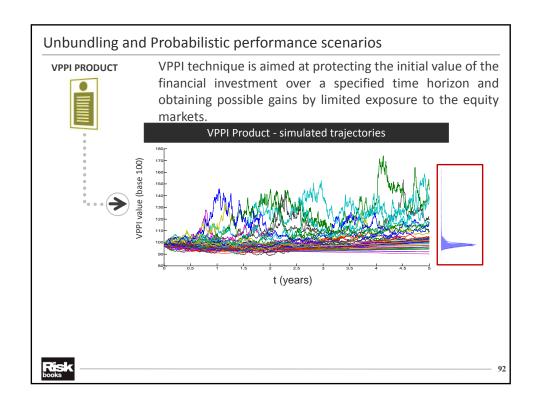


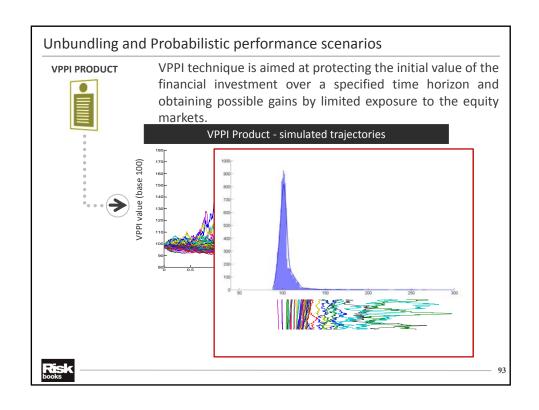


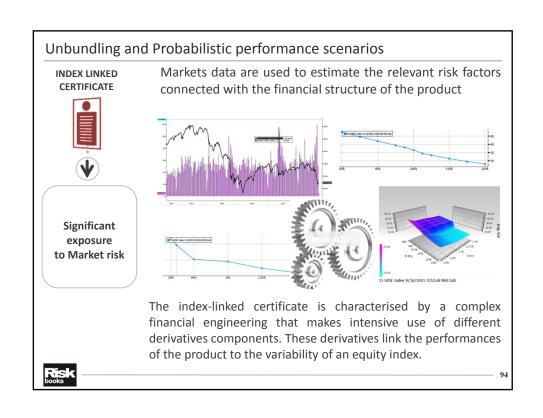


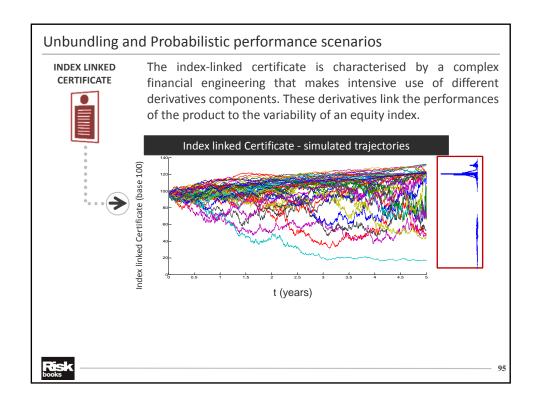


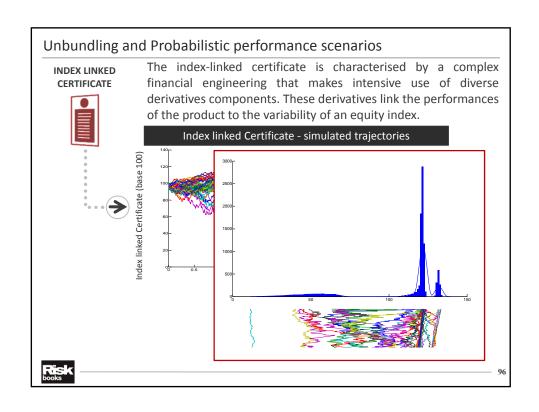


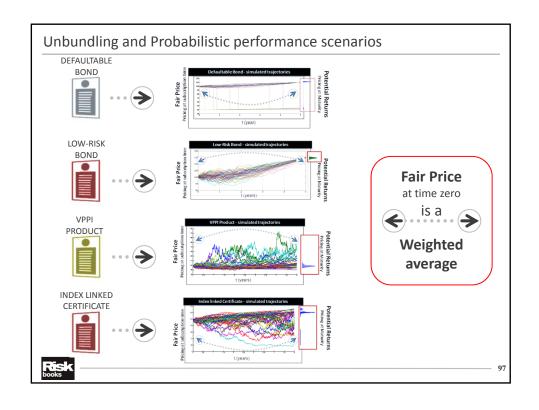


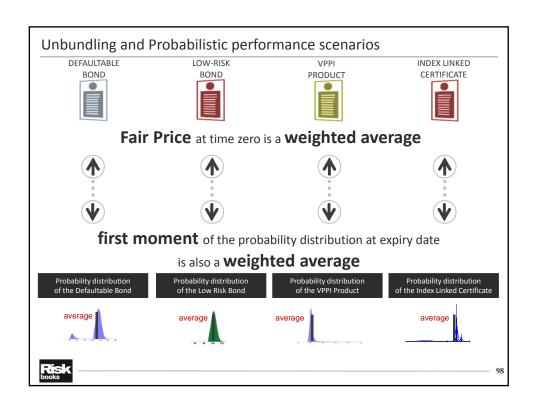


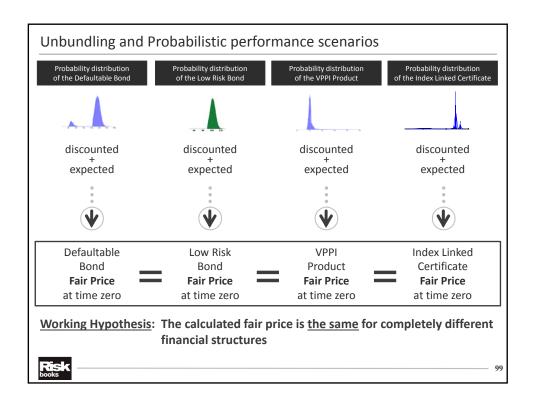


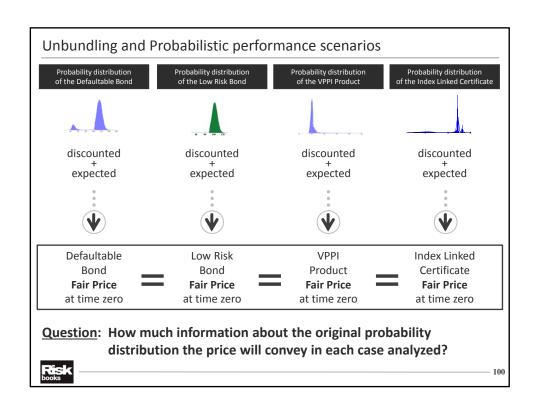


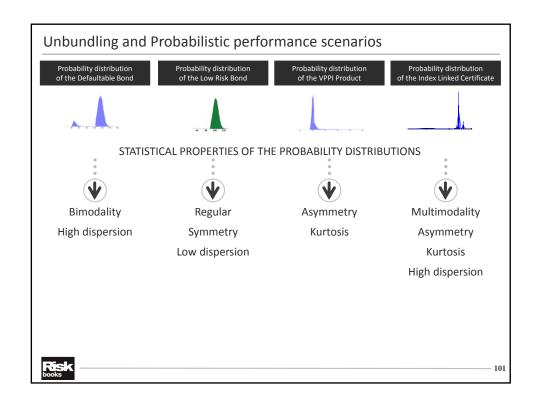


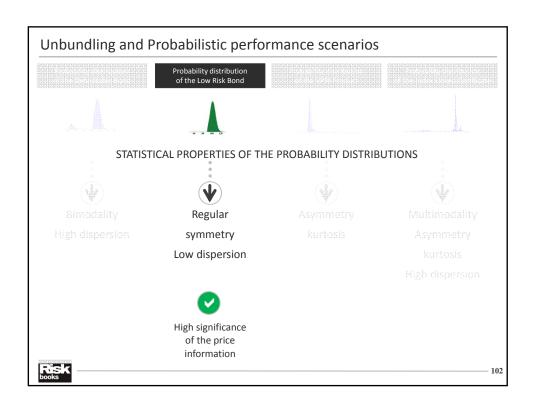


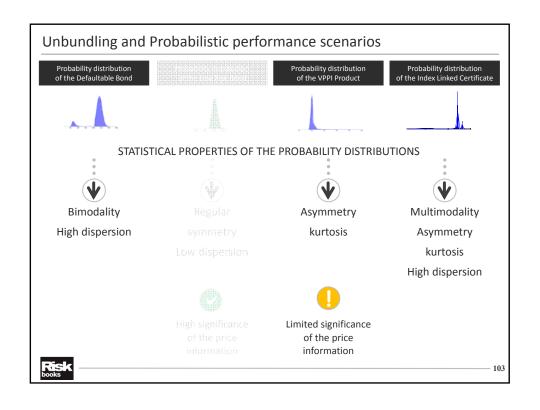


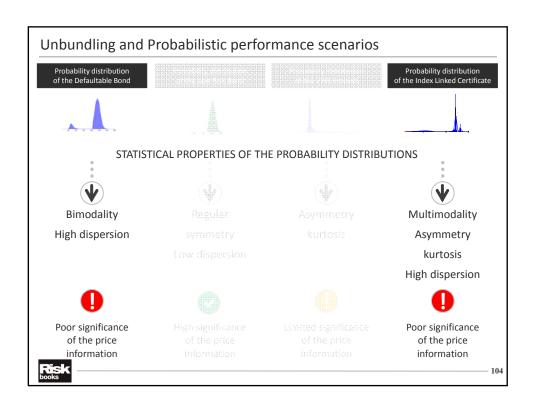


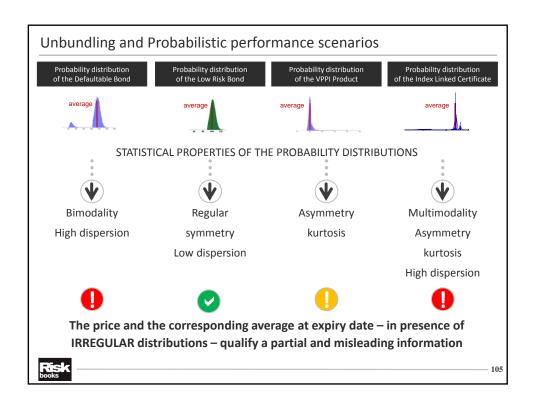
















Significance of the price information



As a weighted average, the price is strictly connected with the first moment of the probability distribution

As the literature suggests, in presence of multimodality and irregular shapes for the probability distributions, the number of moments necessary to properly describe the probability distribution increases drammatically.

See:

- (1) Shohat, Tamarkin, 1943 American Mathematical Survey
- (2) Szego, 1959 American Mathematical Society
- (3) Totik, 2000 Journal of Analytical Mathematics
- (4) Gavriliadis, Athanassoulis, 2009 Journal of Computational and Applied Mathematics

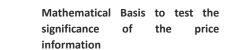


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Unbundling and Probabilistic performance scenarios



Significance of the price information



Given a finite number of moments 2k, it's possible to derive the following approximate relationship between the probability function f (x) and its Christoffel function of degree k:

$$f(x) \approx f_{AP,k}(x) = \frac{k}{c_0 \pi \sqrt{(x-a)(b-x)}} \lambda_k(x)$$

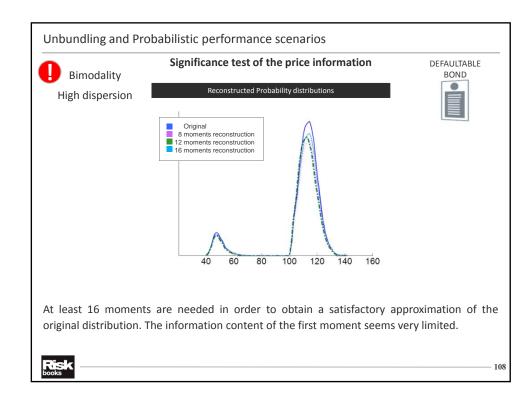
con $x \in [a,b]$. C_0 è un fattore di normalizzazione.

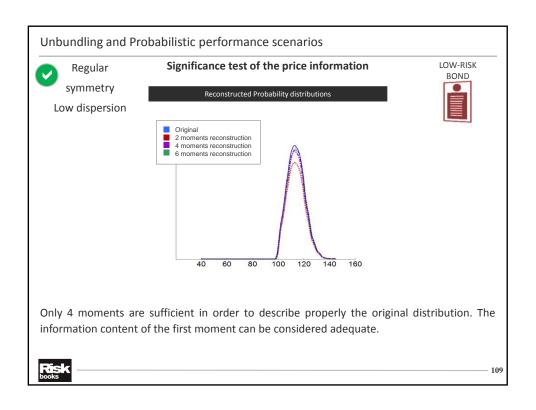


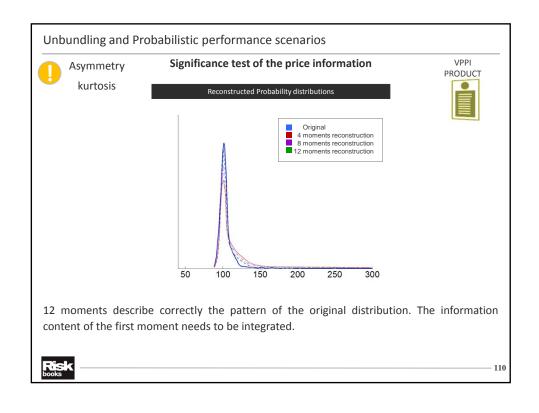
It's then immediate to apply the approximating formula for different values of k in order to test the accuracy of the approximation for the probability distributions corresponding to our different financial products

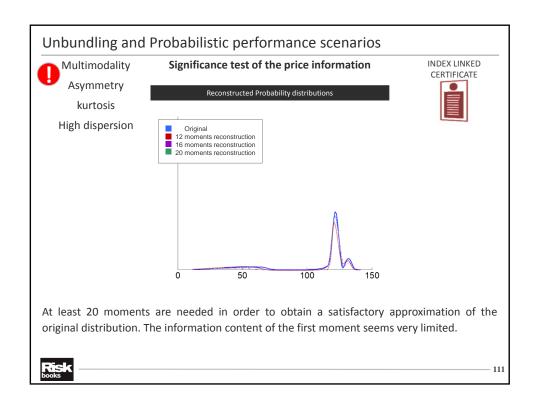


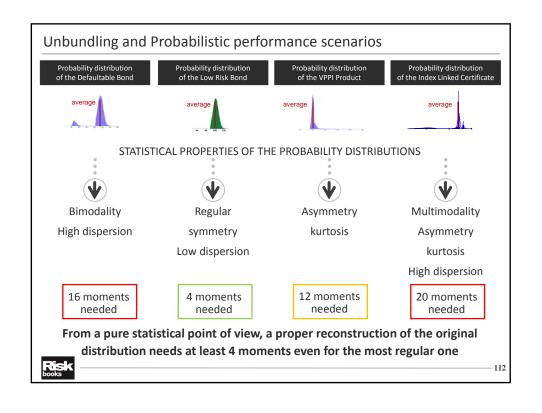
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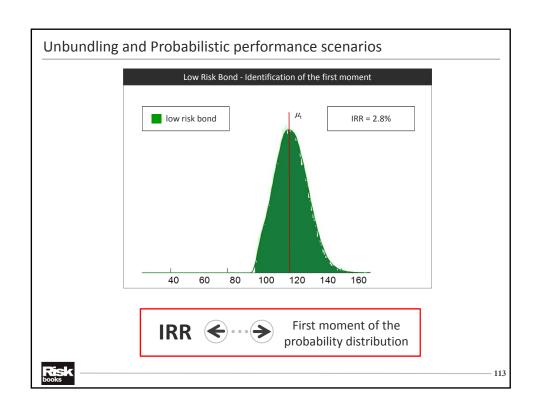


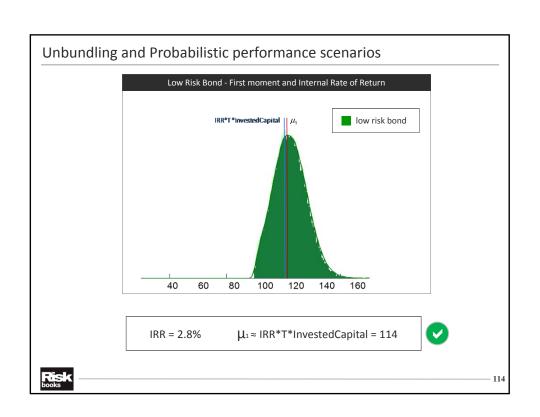


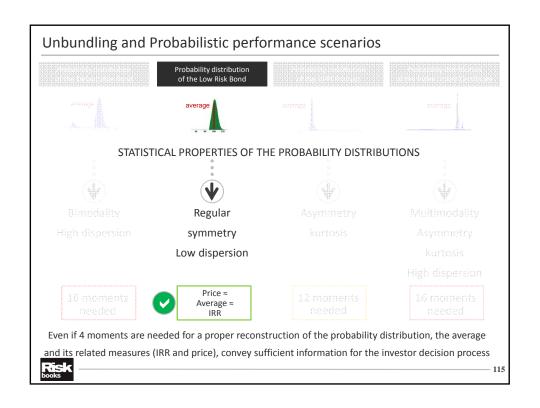


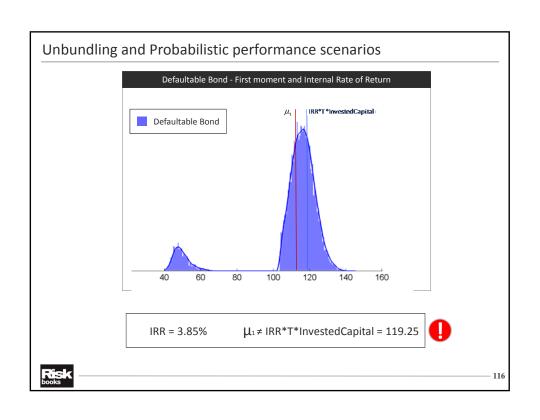


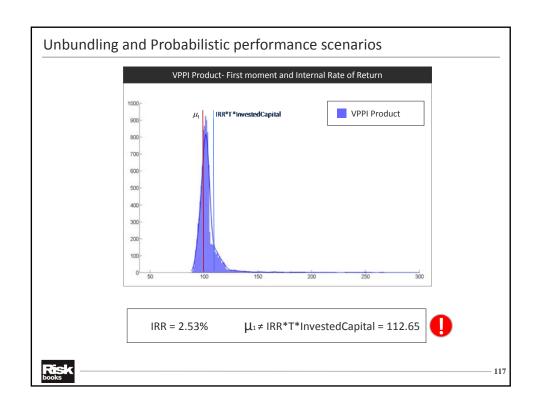


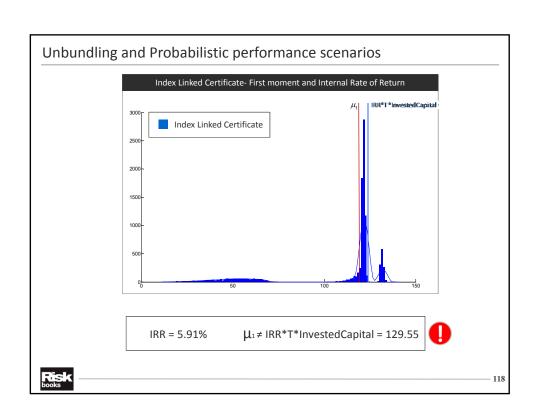


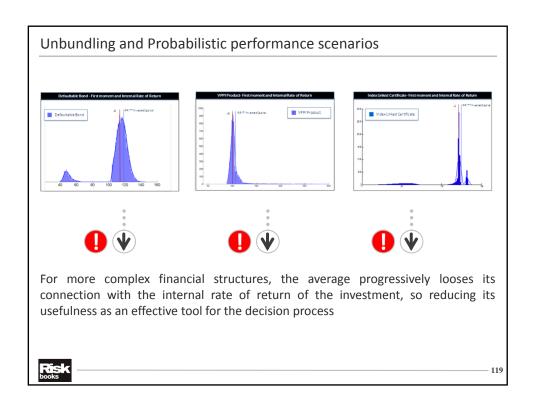


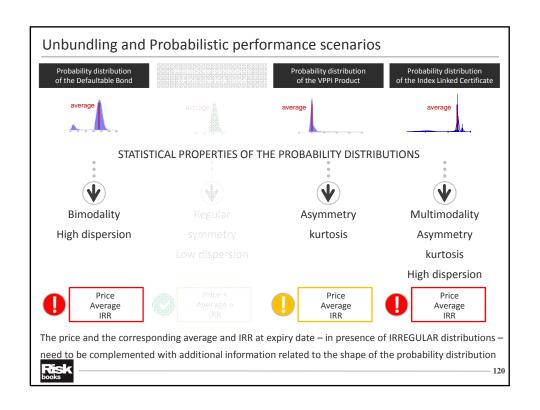


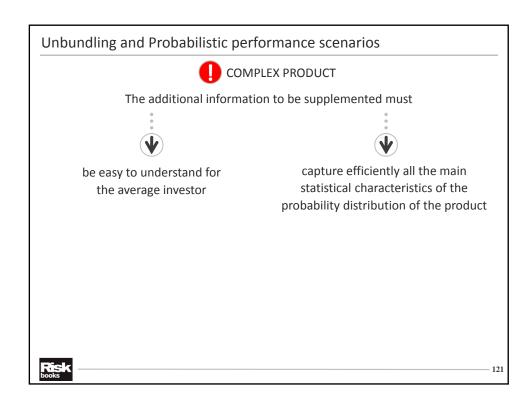


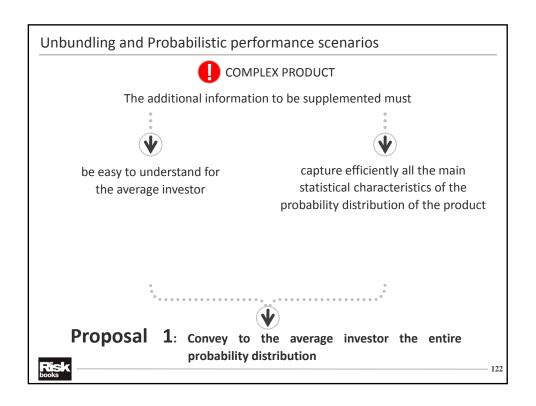


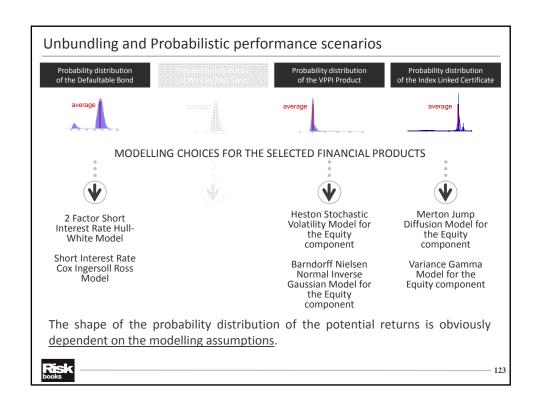


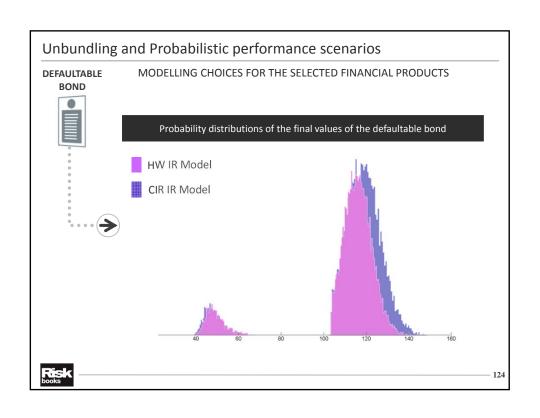


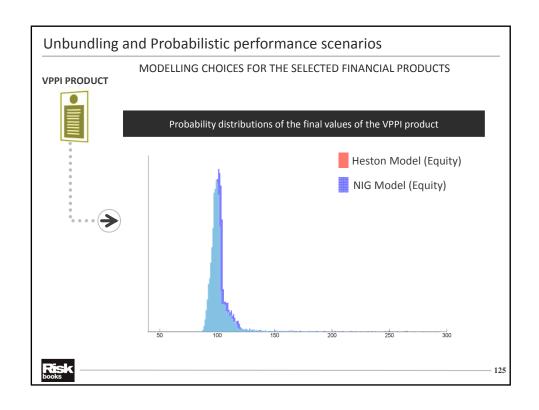


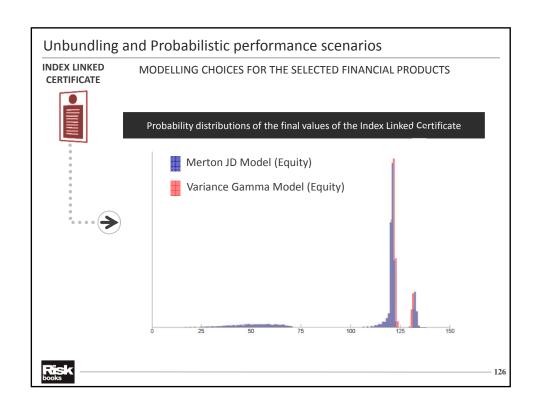


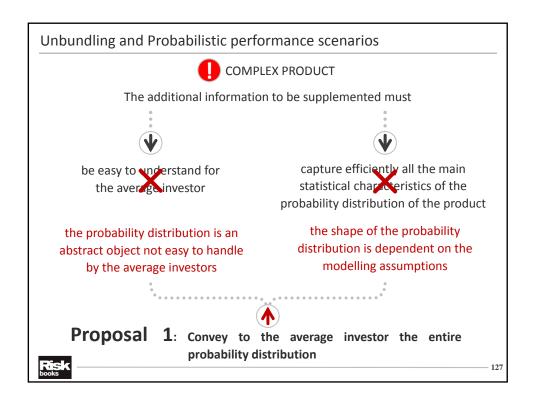


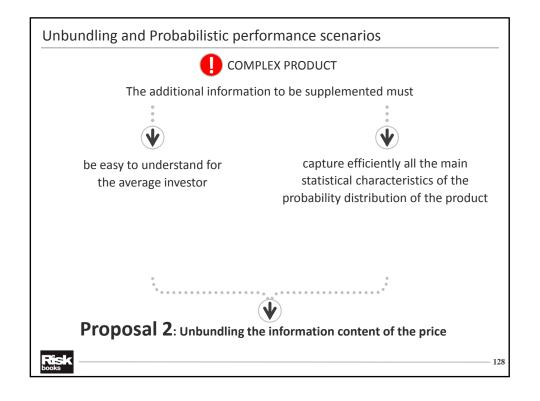


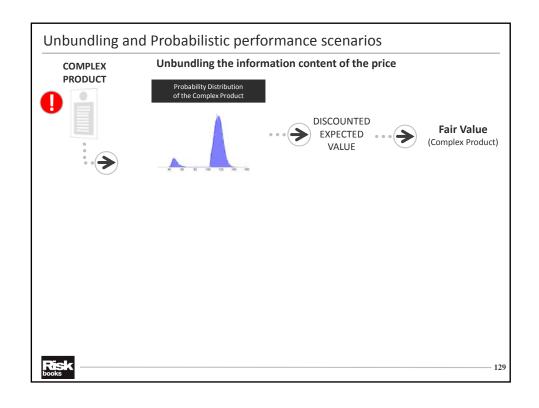


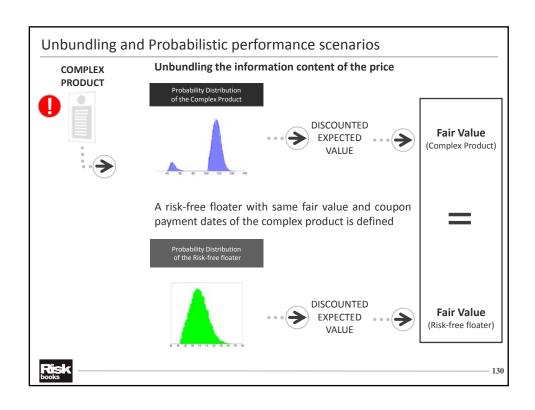


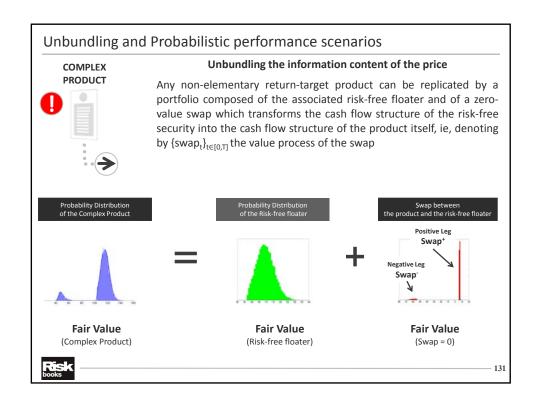


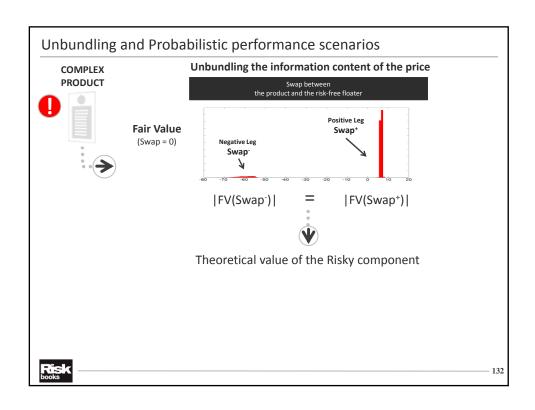


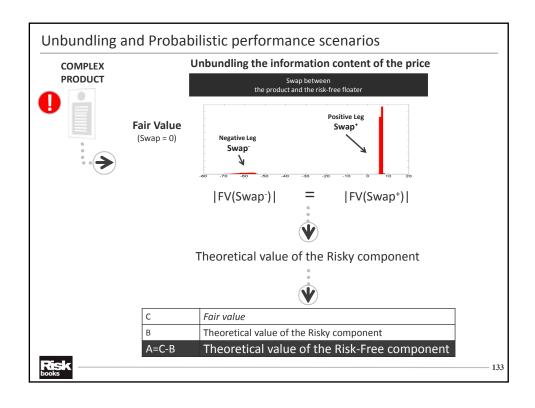


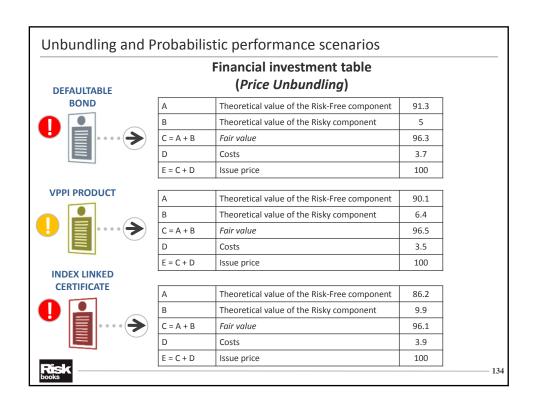


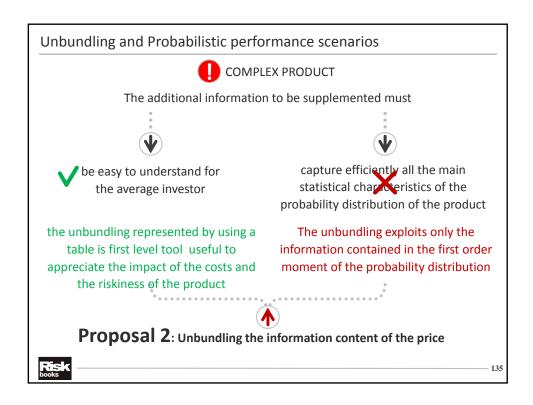


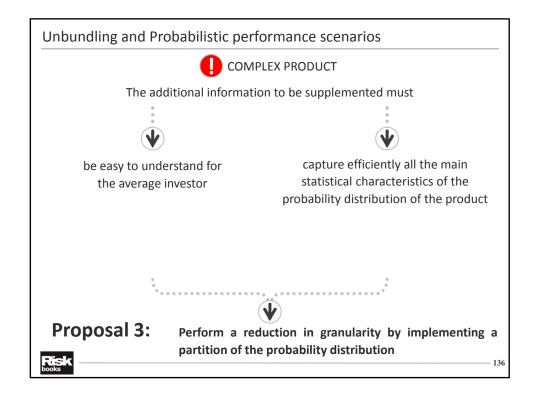


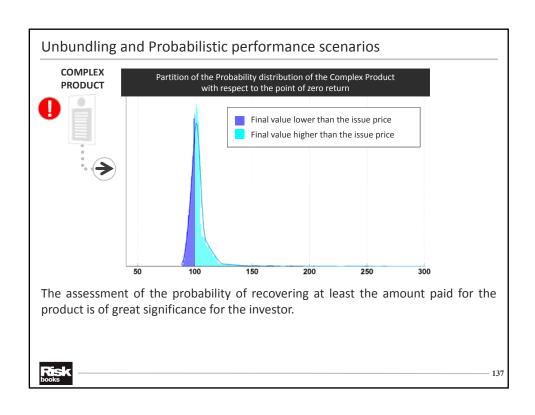


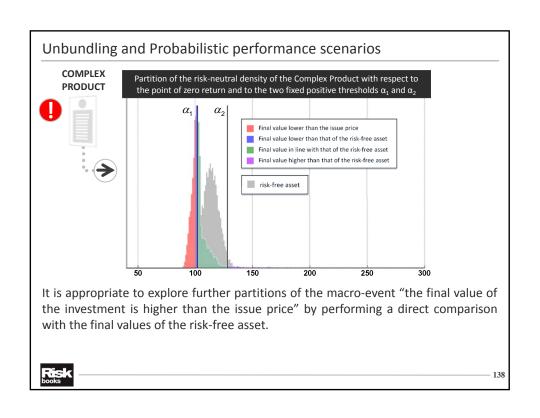


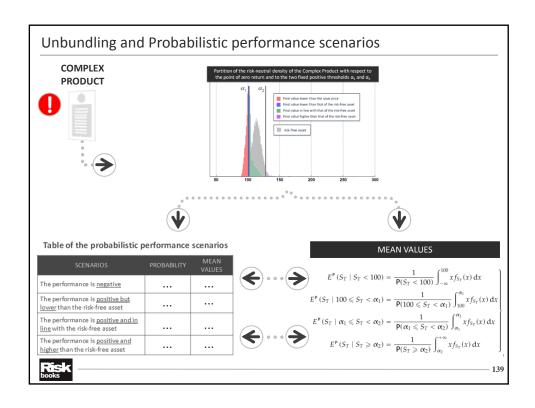


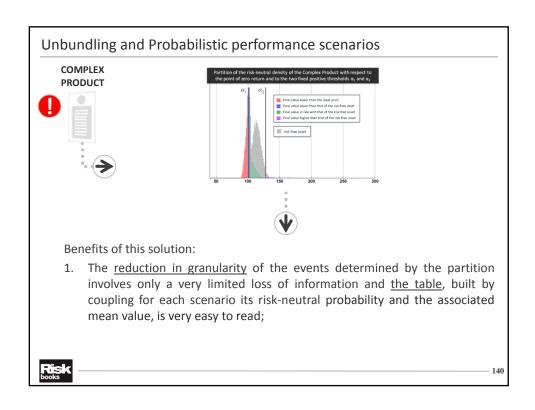


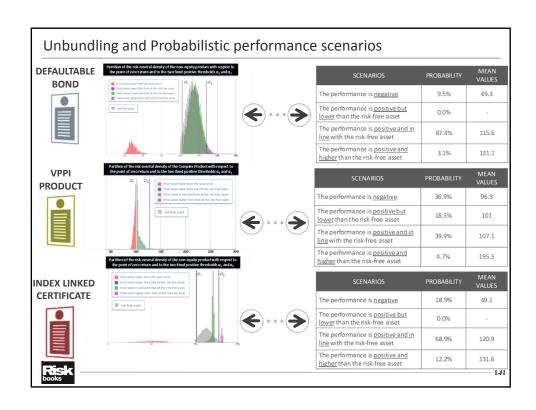


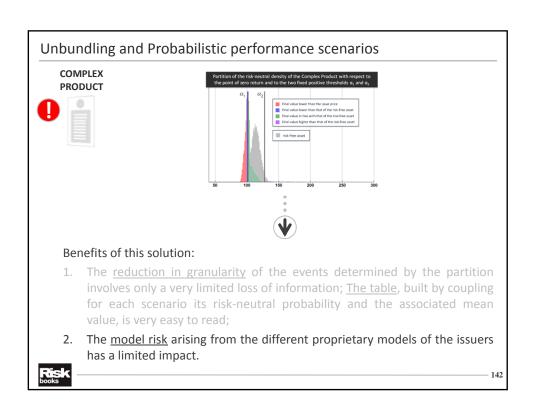


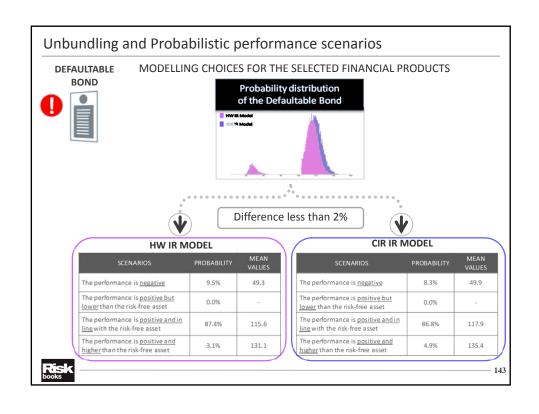


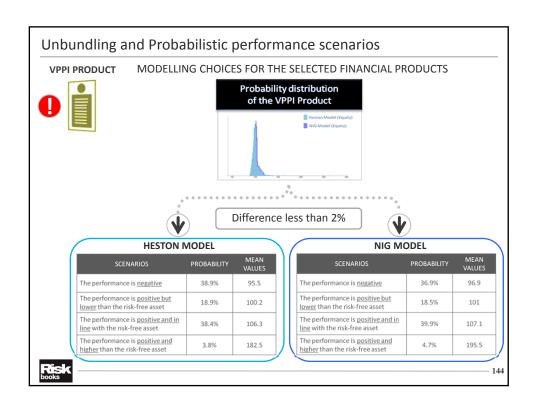


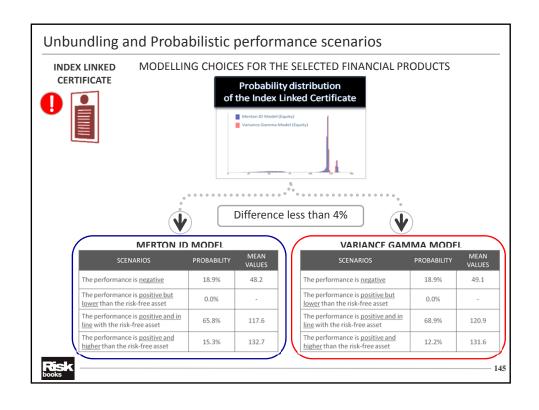


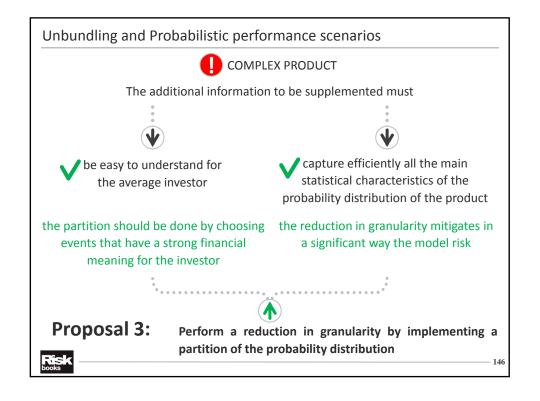


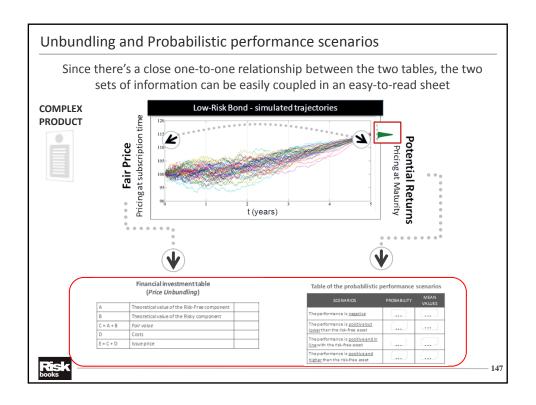










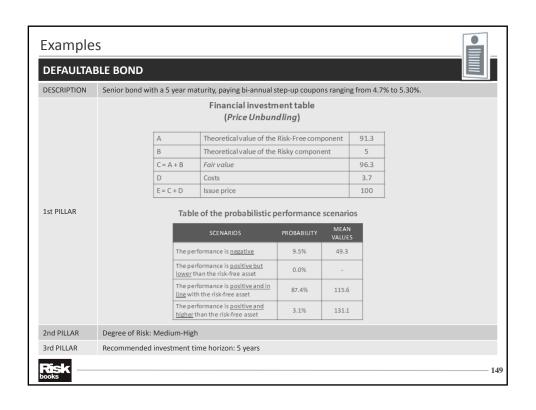


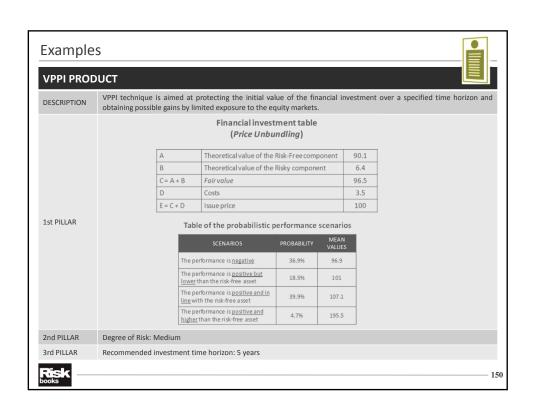
Syllabus

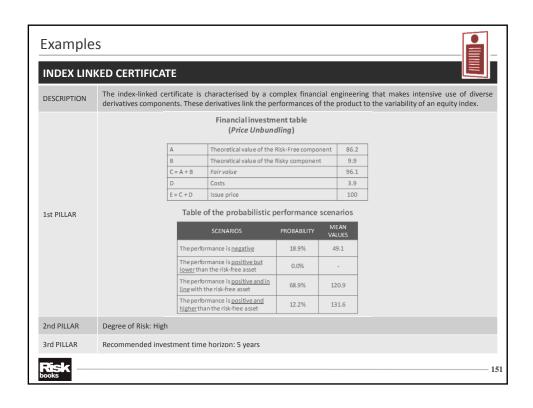
- Preliminaries: the three pillars
- The recommended Investment horizon
- Synthetic risk indicator
- Unbundling and Probabilistic performance scenarios
- An Application of the methodology

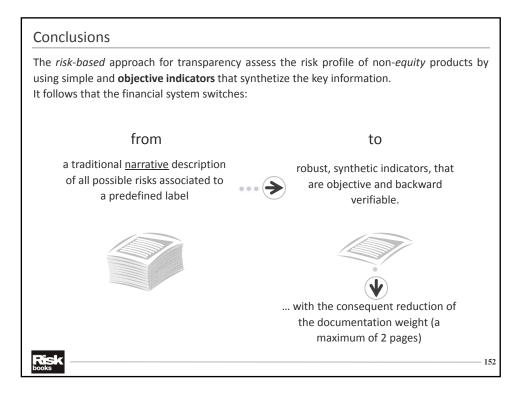
Risk books

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Testimonials

This book fills the gap that exists between the risk management tools available to industry insiders, and those available to investors t is a welcome contribution that will be helpful to anyone who needs to assess the risk of non-equity products."

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"This book constitutes an excellent collection of quantitative methods to the measurement and representation of the risks of non-equity products that comes from a simple but also winning intuition: the information needs of retail investors are not really different from those of financial institutions since they both want the upside gain by trying to contain the downside risk."

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This book contains a valid quantitative methodology to shed light on the risks embedded in any non-equity product. By answering he key questions of any investor about the potential performances, the risk rating and the optimal holding time of the product, the hree "pillars" of the book are the best candidates to definitely remove the informative lack that worldwide regulators have recognized in the existing rules on risks disclosure. The adoption of these "pillars" would be the ideal completion of the regulatory reform undertaken by the European Authorities regarding the revision of the information contents for Packaged Retail Investment Products. Should the quantitative framework set forth in this work become the reference to update the regulatory framework on ransparency, an authentic reversal of the traditional approaches to risks transparency would be realized with effective benefits for nivestors' comprehension and for allowing them to pick the product that best fits their needs."

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'This innovative book sheds a light on the dark path of the financial risks intrinsic to non-equity financial products, which are often underestimated, or even poorly understood, by investors seeking higher returns. Mathematical finance techniques are here applied in in original and unconventional manner for the purpose of effectively disclosing these risks and properly assessing their impact on vestments' returns.'



