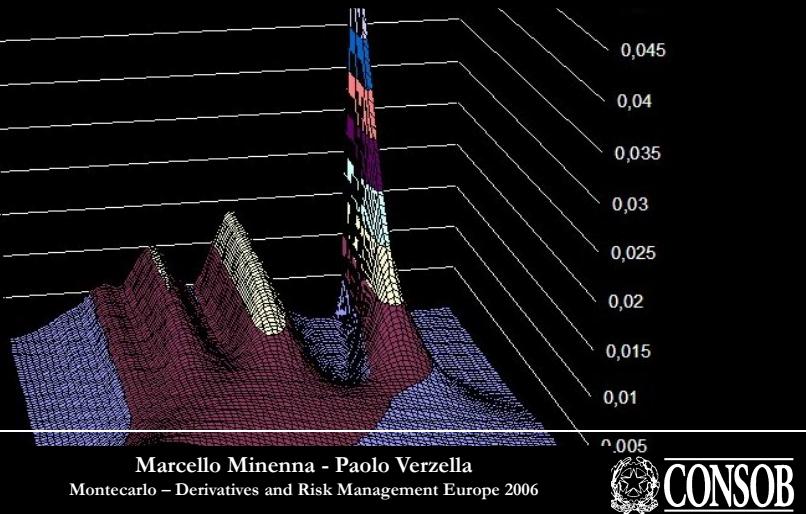


# Masterclass: Implementing affine jump diffusion models at the trading desk



Marcello Minenna - Paolo Verzella  
Montecarlo – Derivatives and Risk Management Europe 2006



## Syllabus of the presentation

- Review of Fourier Methods in Option Pricing
- Calibration and Performance
- Greek derivation
- Greek Behavior of New FT-Q

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## Syllabus of the presentation

- Review of Fourier Methods in Option Pricing
- Calibration and Performance
- Greek derivation
- Greek Behavior of New FT-Q

## Review of Fourier Methods in Option Pricing – theory

European Call      Maturity       $T$       Terminal Spot Price       $S_T$

In AJD models Call Price can be expressed in a form close to the canonical Black – Scholes - Merton style

$$C_t = S_t P_1(\Theta) - K e^{-r\tau} P_2(\Theta)$$

where

$$P_1(\Theta), P_2(\Theta) = \Pr(\ln S_T \geq \ln[K])$$

under different martingale measures



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## Review of Fourier Methods in Option Pricing – theory

$$P_1(\Theta), P_2(\Theta) = \Pr(\ln S_T \geq \ln[K])$$

under different martingale measures



determined by using the Levy's inversion formula, i.e.:

$$\Pr(\ln S_T \geq \ln[K]) = \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \text{Re} \left[ \frac{e^{-i\phi \ln[K]} \tilde{f}_j(\phi)}{i\phi} \right] d\phi$$

## Review of Fourier Methods in Option Pricing – theory

$$\Pr(\ln S_T \geq \ln[K]) = \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \text{Re} \left[ \frac{e^{-i\phi \ln[K]} \tilde{f}_j(\phi)}{i\phi} \right] d\phi$$



a close formula for the Characteristic Function of the log – terminal price, i.e.:

$$\tilde{f}_T(\phi) = E[e^{i\phi \ln S_T}]$$



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## Review of Fourier Methods in Option Pricing – theory

$$\tilde{f}_T(\phi) = E[e^{i\phi \ln S_T}]$$



a closed formula for AJD models

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

$$dS_t = \mu S_t dt + \sqrt{v_t} S_t dz_t^{(1)}$$

$$dv_t = \kappa[\theta - v_t]dt + \sigma \sqrt{v_t} dz_t^{(2)}$$



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## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Derivation for portfolio replication

$$f = f(S, v, t)$$



$$df = \frac{\partial f}{\partial S} (\mu S dt + \sqrt{v} S dz_1) + \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial v} \left[ \kappa (\theta - v) dt + \sigma \sqrt{v} dz_2 \right] + \frac{1}{2} \frac{\partial^2 f}{\partial S^2} (v S^2 dt) + \frac{1}{2} \frac{\partial^2 f}{\partial v^2} (\sigma^2 v dt) + \frac{\partial^2 f}{\partial S \partial v} (S \sigma \rho_{1,2} v) dt$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Derivation for portfolio replication

$$\pi = f_1 - \Delta_1 f_0 - \Delta_0 S$$

the coefficients  $\Delta_1, \Delta_0$  are chosen in order to vanish any randomness of the portfolio

$$d\pi = \frac{\partial f_1}{\partial t} dt + \frac{1}{2} \frac{\partial^2 f_1}{\partial S^2} (v S^2 dt) + \frac{\partial f_1}{\partial v} [\kappa (\theta - v) dt] + \frac{1}{2} \frac{\partial^2 f_1}{\partial v^2} (\sigma^2 v dt) + \frac{\partial^2 f_1}{\partial S \partial v} (S \sigma \rho_{1,2} v) dt - \frac{\partial f_1 / \partial v}{\partial f_0 / \partial v} \frac{\partial f_0}{\partial v} dt - \frac{\partial f_1 / \partial v}{\partial f_0 / \partial v} \frac{1}{2} \frac{\partial^2 f_0}{\partial S^2} (v S^2 dt) - \frac{\partial f_1 / \partial v}{\partial f_0 / \partial v} \frac{1}{2} \frac{\partial^2 f_0}{\partial v^2} (\sigma^2 v dt) - \frac{\partial f_1 / \partial v}{\partial f_0 / \partial v} \frac{\partial^2 f_0}{\partial S \partial v} (S \sigma \rho_{1,2} v) dt$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Derivation for portfolio replication

$$\text{no arbitrage hypothesis} \quad d\pi = r\pi dt$$



$$-rf_0 + \frac{\partial f_0}{\partial t} + \frac{\partial f_0}{\partial S} rS + \frac{1}{2} \frac{\partial^2 f_0}{\partial S^2} vS^2 + \frac{1}{2} \frac{\partial^2 f_0}{\partial v^2} \sigma^2 v + \frac{\partial^2 f_0}{\partial S \partial v} S \sigma \rho_{1,2} v - [\kappa (\theta - v)] \frac{\partial f_0}{\partial v} =$$

$$= -rf_1 + \frac{\partial f_1}{\partial t} + \frac{\partial f_1}{\partial S} rS + \frac{1}{2} \frac{\partial^2 f_1}{\partial S^2} vS^2 + \frac{1}{2} \frac{\partial^2 f_1}{\partial v^2} \sigma^2 v + \frac{\partial^2 f_1}{\partial S \partial v} S \sigma \rho_{1,2} v - [\kappa (\theta - v)] \frac{\partial f_1}{\partial v}$$



$$-rf + \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} rS + \frac{1}{2} \frac{\partial^2 f}{\partial S^2} vS^2 + \frac{1}{2} \frac{\partial^2 f}{\partial v^2} \sigma^2 v + \frac{\partial^2 f}{\partial S \partial v} S \sigma \rho_{1,2} v - [\kappa (\theta - v)] \frac{\partial f}{\partial v} = \lambda^*(S, v, t)$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE specification for the pricing of a Call option

$$-rC + \frac{\partial C}{\partial t} + \frac{\partial C}{\partial S} rS + \frac{1}{2} \frac{\partial^2 C}{\partial S^2} vS^2 + \frac{1}{2} \frac{\partial^2 C}{\partial v^2} \sigma^2 v + \frac{\partial C}{\partial S \partial v} S \sigma \rho_{1,2} v + \frac{\partial C}{\partial v} [\kappa (\theta - v) - \lambda^*(S, v, t)] = 0$$

$$C(S, v, t = T) = \max(0, S_T - K)$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Shift into the forward space

$$\tilde{C}(x, v, \tau) = e^{r\tau} C(x, v, \tau) = e^{r(t-\tau)} C(S, v, t, T)$$



$$-\frac{\partial \tilde{C}}{\partial \tau} + r \frac{\partial \tilde{C}}{\partial x} + \frac{1}{2} \frac{\partial^2 \tilde{C}}{\partial v^2} (\sigma^2 v) + \frac{\partial^2 \tilde{C}}{\partial x \partial v} (v \sigma \rho_{1,2}) + \frac{1}{2} \left( \frac{\partial^2 \tilde{C}}{\partial x^2} - \frac{\partial \tilde{C}}{\partial v} \right) v + \frac{\partial \tilde{C}}{\partial v} [\kappa(\theta - v) - \lambda v] = 0$$

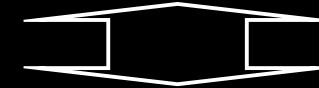
$$\tilde{C}(x_\tau, v_\tau, \tau = 0) = \max(0, e^{x_\tau - v_\tau} - K)$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Shift into Black-Scholes-Merton space

$$C_t(S, v, t, T) = S_t P_1(S, v, t, T) - K e^{-r(T-t)} P_2(S, v, t, T)$$



$$\tilde{C}_t(x, v, \tau) = e^{x\tau} P_1(x, v, \tau) - K P_2(x, v, \tau)$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Shift into Black-Scholes-Merton space

$$-\frac{\partial P_j}{\partial \tau} + \frac{\partial P_j}{\partial x} (r + c_j v) + \frac{1}{2} \frac{\partial^2 P_j}{\partial v^2} (\sigma^2 v) + \frac{\partial^2 P_j}{\partial x \partial v} (v \sigma \rho_{1,2}) + \frac{1}{2} \frac{\partial^2 P_j}{\partial x^2} v + \frac{\partial P_j}{\partial v} (a - b_j v) = 0$$

$$P_j(x_\tau, v_\tau, \tau = 0) = 1_{(x_\tau \geq \ln K)}$$

$$\text{where } c_1 = \frac{1}{2}, \quad c_2 = -\frac{1}{2}, \quad a = \kappa\theta, \quad b_1 = \kappa + \tilde{\lambda} - \rho_{1,2}\sigma, \quad b_2 = \kappa + \tilde{\lambda}$$

by using Feynman Cac formula....



characteristics of the probability measure  $P_j$  at a generic time  $\tau$ :

$$P_j(x_\tau, v_\tau, \tau) = P_j(x_{\tau=0} \geq \ln K | x_\tau, v_\tau)$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Shift into Fourier space

by using the Levy's inversion formula...



$$P_j(x_{\tau=0} \geq \ln K | x_\tau, v_\tau) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{e^{-i\xi \ln K}}{i\xi} \tilde{f}_j(x_\tau, v_\tau, \tau = 0, \xi | x_\tau, v_\tau) d\xi$$



$$-\frac{\partial \tilde{f}_j}{\partial \tau} + \frac{\partial \tilde{f}_j}{\partial x} (r + c_j v) + \frac{1}{2} \frac{\partial^2 \tilde{f}_j}{\partial v^2} (\sigma^2 v) + \frac{\partial^2 \tilde{f}_j}{\partial v \partial x} (v \sigma \rho_{1,2}) + \frac{\partial^2 \tilde{f}_j}{\partial x^2} v + \frac{\partial \tilde{f}_j}{\partial v} [a - b_j v]$$

$$\tilde{f}_j(x_\tau, v_\tau, \tau = 0, \xi) = e^{i\xi x_\tau - \frac{1}{2}\xi^2 \tau}$$

## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### PDE Shift into ODE space

by using the solution:  $\tilde{f}_j(x_\tau, v_\tau, \tau = 0, \xi | x_\tau, v_\tau) = e^{(C_\tau^{(j)} + D_\tau^{(j)})v_\tau + i\xi x_\tau}$



$$\begin{aligned}\frac{\partial C_j}{\partial \tau} &= ri\xi + aD_j \\ \frac{\partial D_j}{\partial \tau} &= c_j i\xi + \frac{1}{2} D_j^2 \sigma^2 + i\xi D_j \sigma \rho_{1,2} - \frac{1}{2} \xi^2 - b_j D_j \\ C_0^{(j)} &= 0 \\ D_0^{(j)} &= 0\end{aligned}$$



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## Review of Fourier Methods in Option Pricing – theory

Example of derivation for Heston Model

### ODE Solutions

$$C_j = ri\xi(T-t) - \frac{2a}{\sigma^2} \left( \alpha_2(T-t) + \ln \frac{\frac{\alpha_2}{\alpha_1} e^{d(T-t)} - 1}{\frac{\alpha_2}{\alpha_1} - 1} \right)$$

$$D_j = -\frac{2\alpha_2}{\sigma^2} \frac{1 - e^{d(T-t)}}{1 - \frac{\alpha_2}{\alpha_1} e^{d(T-t)}}$$

$$\begin{aligned}d &= \sqrt{(\rho_{1,2} \sigma \xi i - b_j)^2 - \sigma^2 (2c_j \xi i - \xi^2)} \\ \alpha_1 &= \frac{\rho_{1,2} \sigma \xi i - b_j + d}{2}, \\ \alpha_2 &= \frac{\rho_{1,2} \sigma \xi i - b_j - d}{2}\end{aligned}$$



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## Review of Fourier Methods in Option Pricing – practice

Example of derivation for Heston Model

### PRICING

$$C_t = S_t P_1 - K e^{-r(T-t)} P_2$$

$$P_j = \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \Re \left\{ \frac{e^{-i\xi \ln K}}{i\xi} e^{[C_\tau^{(j)} + D_\tau^{(j)} v_\tau + i\xi (\ln S_t + r(T-t))]} \right\} d\xi$$

with:

$$C_j = ri\xi(T-t) - \frac{2a}{\sigma^2} \left( \alpha_2(T-t) + \ln \frac{\frac{\alpha_2}{\alpha_1} e^{d(T-t)} - 1}{\frac{\alpha_2}{\alpha_1} - 1} \right)$$

$$D_j = -\frac{2\alpha_2}{\sigma^2} \frac{1 - e^{d(T-t)}}{1 - \frac{\alpha_2}{\alpha_1} e^{d(T-t)}}$$

$$d = \sqrt{(\rho_{1,2} \sigma \xi i - b_j)^2 - \sigma^2 (2c_j \xi i - \xi^2)}$$

$$\alpha_1 = \frac{\rho_{1,2} \sigma \xi i - b_j + d}{2}, \quad \alpha_2 = \frac{\rho_{1,2} \sigma \xi i - b_j - d}{2}$$

$$\begin{aligned}c_{1/2} &= \pm \frac{1}{2} \\ a &= \kappa \theta \\ b_1 &= \kappa + \tilde{\lambda} - \rho_{1,2} \sigma \\ b_2 &= \kappa + \tilde{\lambda}\end{aligned}$$



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## Review of Fourier Methods in Option Pricing – practice

How to compute:  $C_t$



Quadrature Algorithm  
FT - Q for  
 $P_1(\Theta), P_2(\Theta)$



Fast Fourier Transform  
FFT

**Old FT - Q**      **New FT - Q**



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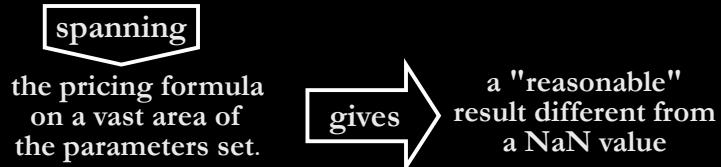


Algorithms Valuation Criteria

## STABILITY

The algorithm is defined stable if and only if

it "closes" the quadrature scheme



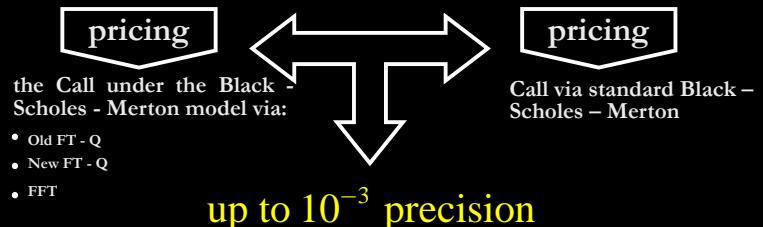
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Algorithms Valuation Criteria

## ACCURACY

The algorithm is defined accurate if and only if



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Algorithms Valuation Criteria

## SPEED

The algorithm is defined fast with respect to

the results of the FFT algorithm



a set of 4100 prices along the strike



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Algorithms Valuation Criteria



High Order Newton Cotes  
Algorithm

Up to 8th



$$C_t = S_t P_1(\Theta) - K e^{-r\tau} P_2(\Theta)$$



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Pros (+)

ACCURACY

Cons (-)STABILITY  
SPEED

In order to overcome the cited problems of Old FT - Q:

- Gauss - Lobatto Quadrature Algorithm
- Re-adjustment of  $\tilde{f}_T(\phi) = E[e^{i\phi \ln S_T}]$



$$C_t = S_t P_1(\Theta) - K e^{-r\tau} P_2(\Theta)$$



In order to overcome the cited problems of Old FT - Q:

- Gauss - Lobatto Quadrature Algorithm
- Re-adjustment of  $\tilde{f}_T(\phi) = E[e^{i\phi \ln S_T}]$



$$C_t = S_t P_1(\Theta) - K e^{-r\tau} P_2(\Theta)$$

- Basic Gauss - Lobatto Quadrature Formula



$$\int_{-1}^1 f(x) dx \approx w_1 f(-1) + w_N f(1) + \sum_{i=2}^{N-1} w_i f(x_i)$$

$$w_i = \frac{2}{N(N-1)[P_{N-1}(x_i)]^2} \quad \text{LIMITED to the interval } (-1,1)$$

$$w_1 = w_N = \frac{2}{N(N-1)}$$



Example of re-adjustment for Heston Model

$$C_j = ri\xi(T-t) - \frac{2a}{\sigma^2} \left( \alpha_2(T-t) + \ln \frac{\frac{\alpha_2}{\alpha_1} e^{d(T-t)} - 1}{\frac{\alpha_2}{\alpha_1} - 1} \right)$$

$$D_j = -\frac{2\alpha_2}{\sigma^2} \frac{1 - e^{d(T-t)}}{1 - \frac{\alpha_2}{\alpha_1} e^{d(T-t)}}$$



$$C_j = ri\xi\tau - \frac{a}{\sigma^2} (\rho_{1,2}\sigma\xi i - b_j + d)\tau - \frac{a}{\sigma^2} 2 \ln \left( 1 - \frac{(1 - e^{-d\tau}) (\rho_{1,2}\sigma\xi i - b_j + d)}{2d} \right)$$

$$D_j = \frac{(2c_j\xi i - \xi^2)(1 - e^{-d\tau})}{2d - (\rho_{1,2}\sigma\xi i - b_j + d)(1 - e^{-d\tau})}$$

$P_1(\Theta), P_2(\Theta)$   Quadrature Algorithm  
New FT - Q

### Pros (+)

STABILITY

ACCURACY

### Cons (-)

SPEED

$C_t$   Fast Fourier Trasform  
FFT

### Cooley - Tukey algorithm

$$\omega(n) = \sum_{j=1}^N e^{-i\frac{2\pi}{N}(j-1)(n-1)} f_j = \sum_{j=1}^{\frac{N}{2}} e^{-i\frac{2\pi}{N}(2j-1)(n-1)} f_{2j} + \sum_{j=1}^{\frac{N}{2}} e^{-i\frac{2\pi}{N}2j(n-1)} f_{2j+1}$$

$C_t$   Fast Fourier Trasform  
FFT

### Cooley - Tukey algorithm

Applied to the equivalent formula via a recombinant FFT parameters



$$C_t = \frac{e^{-\alpha \ln K}}{\pi} \int_0^\infty e^{-i\phi \ln K} \tilde{f}_j(\phi) d\phi \quad \text{for ATM}$$



### Pros (+)

**SPEED**  
FASTER

(up to 40 times the quadrature algorithms)

### Cons (-)

#### STABILITY

\* The formula must be changed **arbitrarily** according to Option moneyness

#### ACCURACY

\*\* the recombinant FFT parameters must be changed according to the choice of the pricing models



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### The Calibration Procedure and Performance

$$SSE_t = \min_{v(t), \Phi} \sum_{n=1}^N [C_{Market}(S_t) - C_{AJD}(S_t)]^2$$

I

II

Quadrature Algorithm  
FT - Q

Fast Fourier Trasform  
FFT



Old FT - Q

New FT - Q

### Syllabus of the presentation

- Review of Fourier Methods in Option Pricing
- **Calibration and Performance**
- Greek derivation
- Greek Behaviour of New FT-Q



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### The Calibration Procedure and Performance

$$SSE_t = \min_{v(t), \Phi} \sum_{n=1}^N [C_{Market}(S_t) - C_{AJD}(S_t)]^2$$

### Pros (+)

**STABILITY**

**ACCURACY**

**SPEED**

### Cons (-)



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## The Calibration Procedure and Performance

$$SSE_t = \min_{v(t), \Phi} \sum_{n=1}^N [C_{Market}(S_t) - C_{AD}(S_t)]^2$$

through  
FFT

Fast Fourier Trasform  
FFT

### Pros (+)

SPEED

### Cons (-)

STABILITY \*  
ACCURACY \*\*

## The Calibration Procedure and Performance

$$SSE_t = \min_{v(t), \Phi} \sum_{n=1}^N [C_{Market}(S_t) - C_{AD}(S_t)]^2$$

through  
New FT - Q

Quadrature Algorithm  
New FT - Q

### Pros (+)

STABILITY  
ACCURACY  
SPEED

### Cons (-)

## The Calibration Procedure and Performance

By keeping in mind that only New FT-Q is stable and accurate,  
some figures on speed

Original Option Pricing Formulas are used

	Heston Model	Merton Model	BCC Model
FFT	<b>7.26 sec.</b>	<b>10.54 sec.</b>	<b>18.33 sec.</b>
NEW FT - Q	<b>55.12 sec.</b>	<b>66.48 sec.</b>	<b>110.39 sec.</b>
OLD FT - Q	<b>390.41 sec.</b>	<b>454.76 sec.</b>	<b>722.1 sec.</b>

By now, the speed of Fourier Trasform method is closer  
than ever to the FFT calibration time

## The Calibration Procedure and Performance

Calibration Performances using  
Option Readjusted Pricing Formulas  
where available

	Heston Model	Merton Model	BCC Model
FFT	<b>7.24 sec.</b>	<b>10.54 sec.</b>	<b>18.32 sec.</b>
NEW FT - Q	<b>23.13 sec.</b>	<b>66.48 sec.</b>	<b>48.7 sec.</b>
OLD FT - Q	<b>331.6 sec.</b>	<b>454.76 sec.</b>	<b>688.5 sec.</b>

## Syllabus of the presentation

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- Review of Fourier Methods in Option Pricing
- Calibration Procedure and Performance
- **Greek derivation**
- Greek Behaviour of New FT-Q



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## Greek derivation

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Example of derivation for Heston Model

$$\Delta_C = P_1$$

$$\Gamma_C = \frac{\partial P_1}{\partial S_t}$$

$$\nu_C = S_t \frac{\partial P_1}{\partial v_t} - K e^{-r\tau} \frac{\partial P_2}{\partial v_t}$$

$$\rho_C = K \tau e^{-r\tau} P_2$$

$$\Theta_C = -\frac{\partial P_1}{\partial S} \left( \frac{1}{2} v S^2 \right) - \frac{\partial P_1}{\partial v} S \left[ \sigma \rho_{1,2} v + [\kappa (\theta - v) - \lambda v] \right] - \frac{\partial^2 P_1}{\partial v^2} \left( \frac{1}{2} S \sigma^2 v \right) - K e^{-r\tau} \left[ r P_2 - \frac{1}{2} \sigma^2 v \frac{\partial^2 P_1}{\partial v^2} - \frac{\partial P_2}{\partial v} [\kappa (\theta - v) - \lambda v] \right]$$

$$\varpi_C = S_t \frac{\partial^2 P_1}{\partial v_t^2} - K e^{-r\tau} \frac{\partial^2 P_2}{\partial v_t^2}$$



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## Greek derivation

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European Call      Maturity       $T$       Terminal Spot Price       $S_T$

In AJD models Greeks can be derived by using the following equivalences



$$S_t \frac{\partial P_1}{\partial S_t} + K \frac{\partial P_1}{\partial K} = 0$$

$$S_t \frac{\partial P_2}{\partial S_t} + K \frac{\partial P_2}{\partial K} = 0$$

$$\frac{\partial^2 P_1}{\partial S_t \partial K} = \frac{\partial^2 P_1}{\partial K \partial S_t}$$

$$\frac{\partial^2 P_2}{\partial S_t \partial K} = \frac{\partial^2 P_2}{\partial K \partial S_t}$$

$$S_t \frac{\partial P_1}{\partial S_t} - e^{-r(T-t)} K \frac{\partial P_2}{\partial S_t} = 0$$

$$\frac{\partial C_1}{\partial K} = \frac{\partial C_2}{\partial S_t} \\ \frac{\partial C_1}{\partial S_t} = -e^{-r(T-t)} P_2$$

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## Syllabus of the presentation

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- Review of Fourier Methods in Option Pricing
- Calibration Procedure and Performance
- **Greek derivation**
- **Greek Behaviour of New FT-Q**



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## Greek behaviour of new FT-Q

An impressive methodology to test Stability of the New FT – Quadrature algorithm is to compute Greeks

Infact, in an AJD setting the Greeks are available in closed form

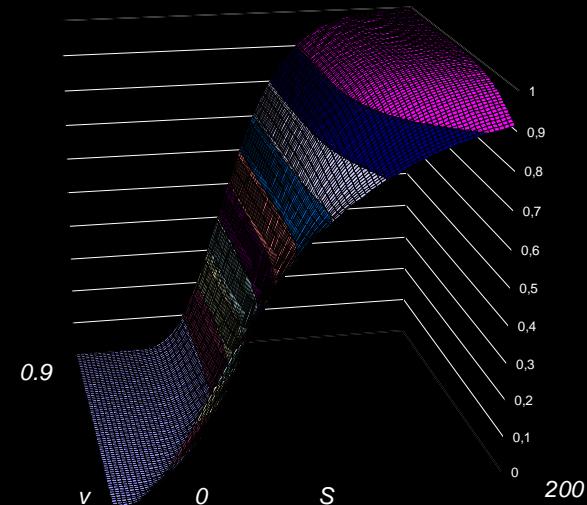
So, an extended spanning of the AJD Greeks on the parameters set is useful to assess models and test Stability



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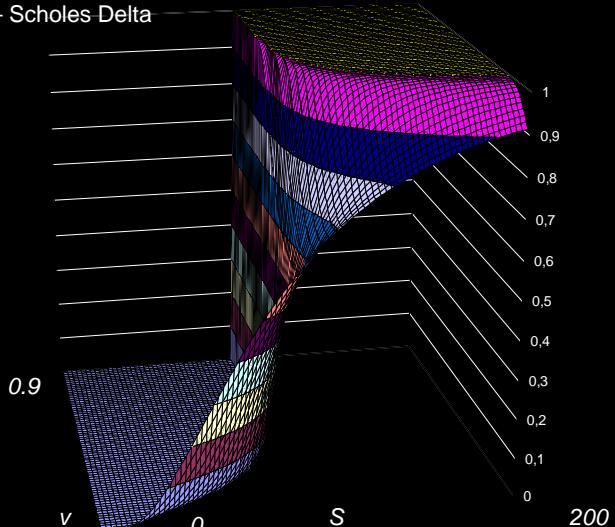
Heston Delta



Lambda = -2

CappaV = 2  
ThetaV = 0.3  
EtaV = 0.1  
Rho = 0

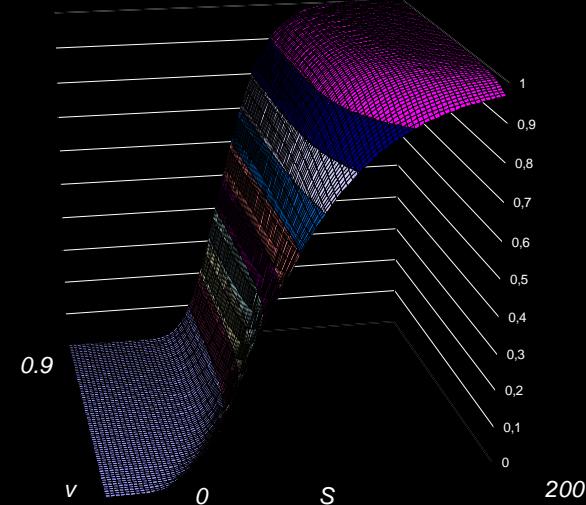
Black – Scholes Delta



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Heston Delta



Lambda = 2 ↑

CappaV = 2  
ThetaV = 0.3  
EtaV = 0.1  
Rho = 0



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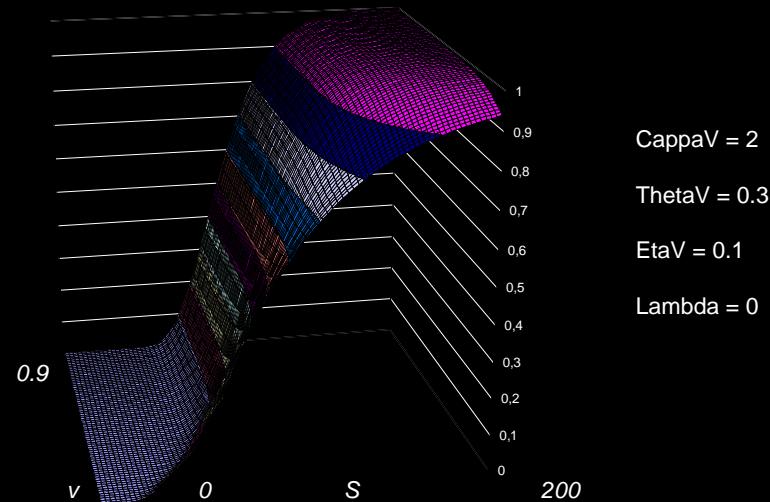


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Heston Delta

Rho = -1

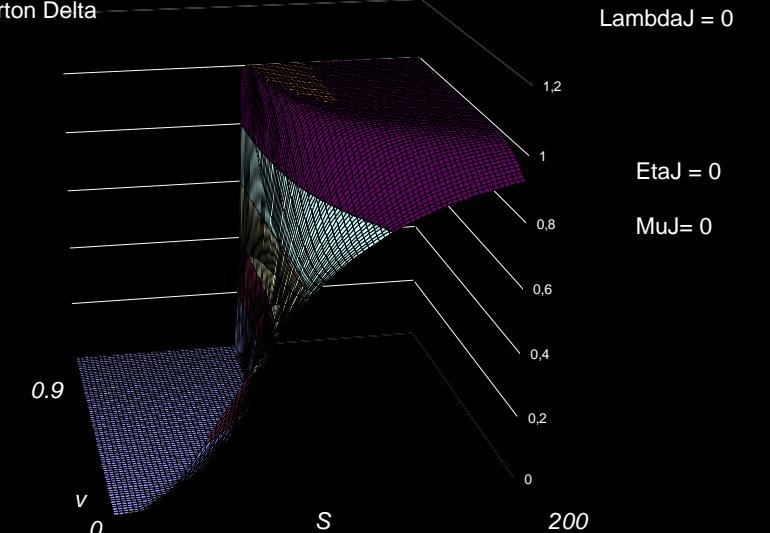


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Merton Delta

LambdaJ = 0

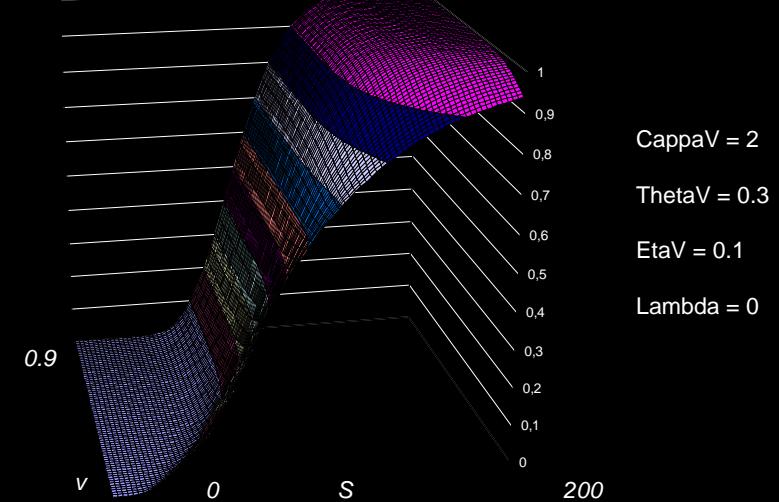


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Heston Delta

Rho = 1

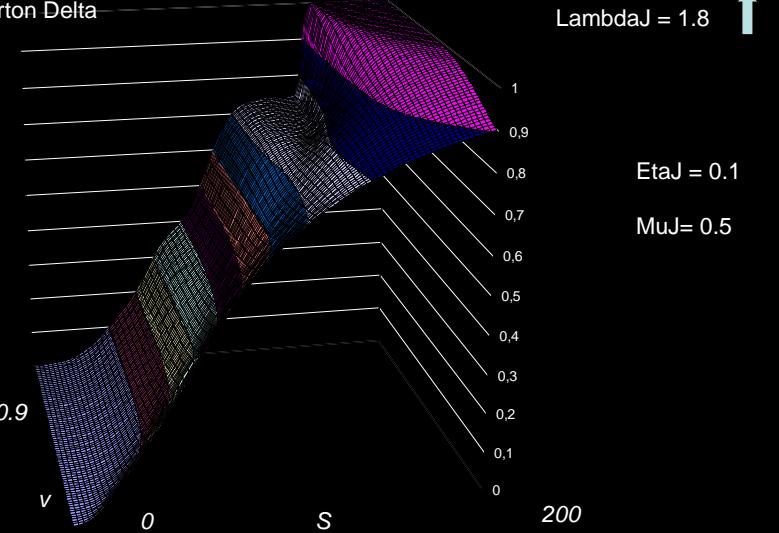


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Merton Delta

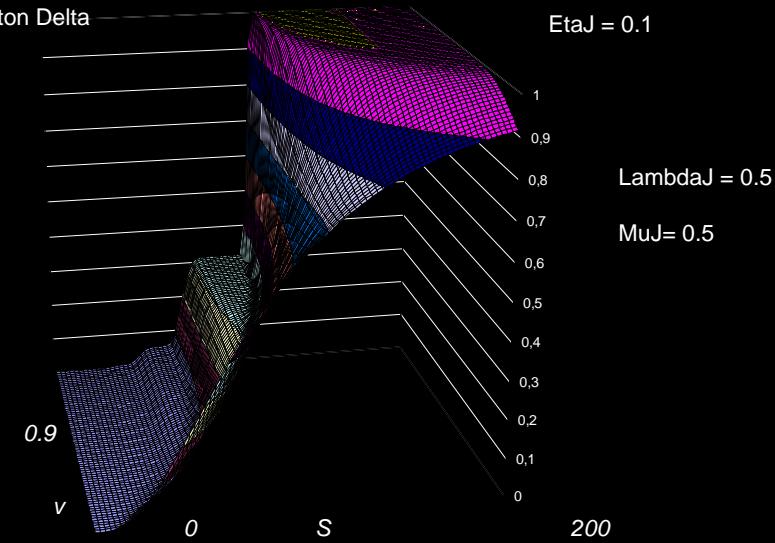
LambdaJ = 1.8 ↑



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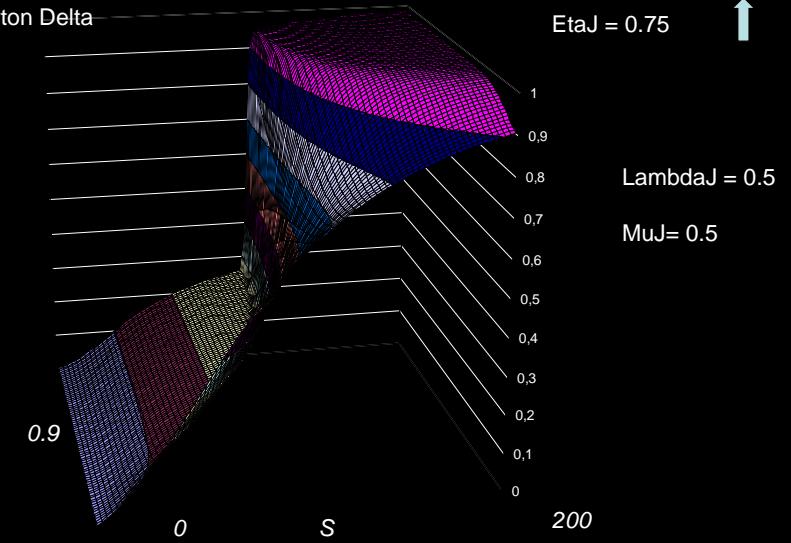
Merton Delta



57



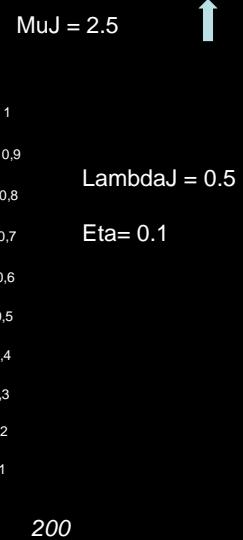
Merton Delta



58



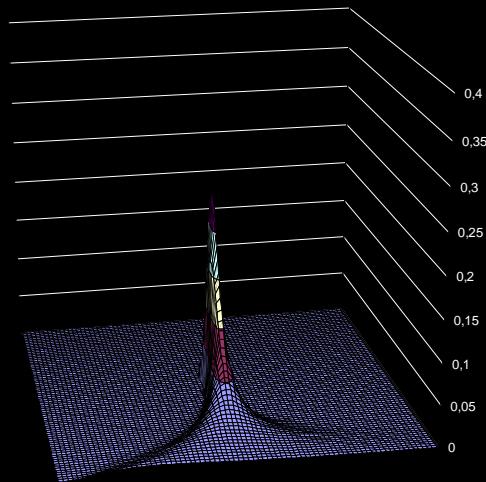
Merton Delta



59



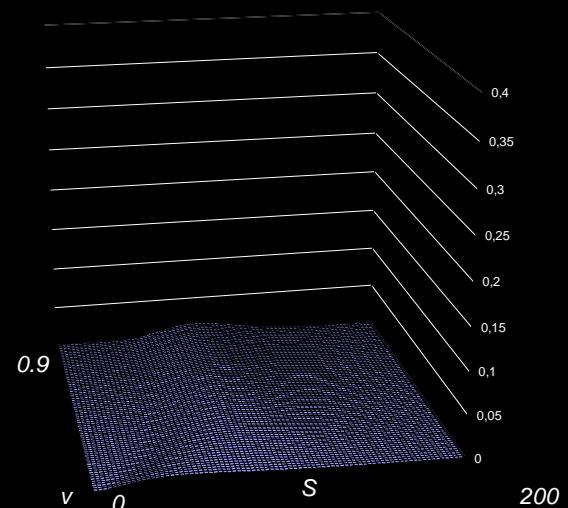
Black – Scholes Gamma



60



Heston Gamma



Lambda = -2

CappaV = 2

ThetaV = 0.3

EtaV = 0.1

Rho = 0

v

61



Lambda = -2

CappaV = 2

ThetaV = 0.3

EtaV = 0.1

Rho = 0

0.9

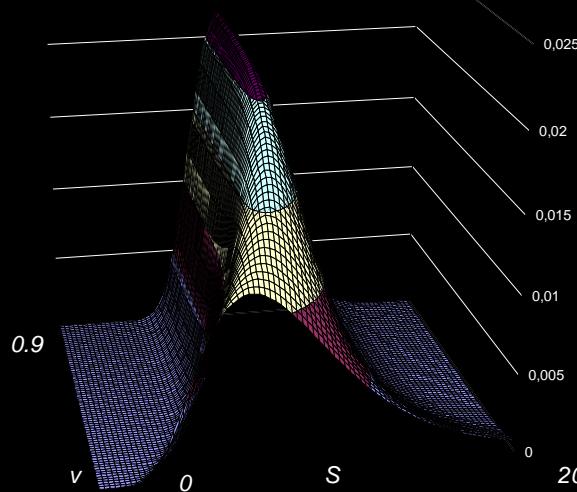
v

62



Heston Gamma

Lambda = 2 ↑



CappaV = 2

ThetaV = 0.3

EtaV = 0.1

Rho = 0

v

63



Rho = -1

CappaV = 2

ThetaV = 0.3

EtaV = 0.1

Lambda = 0

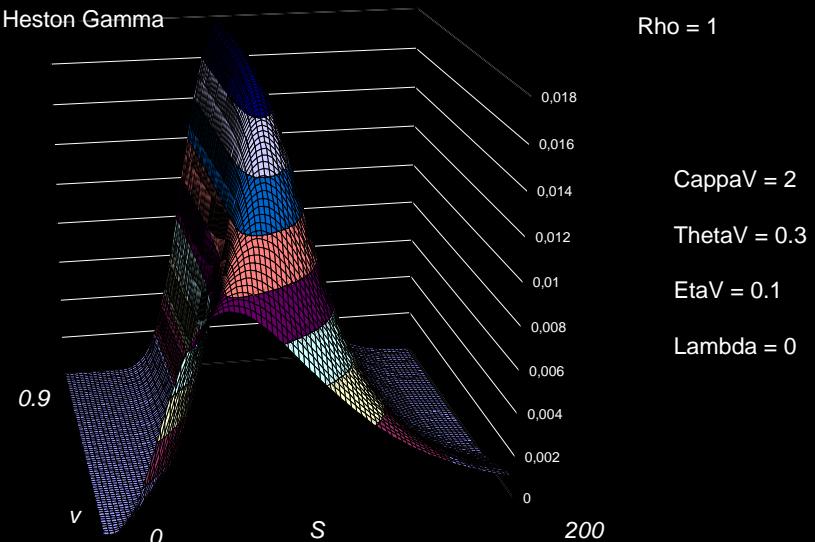
0.9

v

64



Heston Gamma



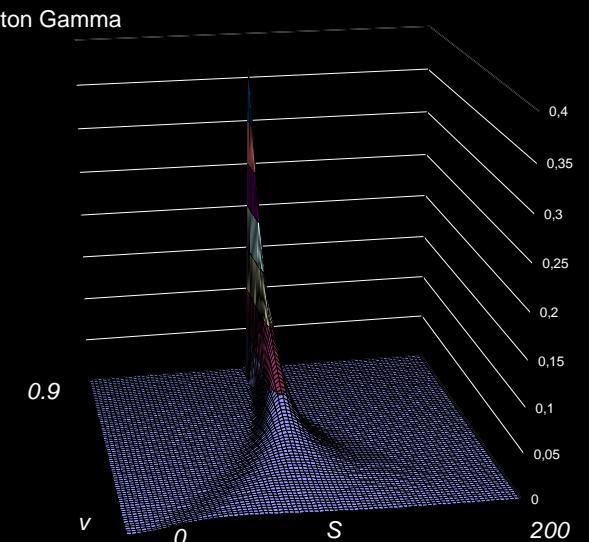
65



CONSOB

LambdaJ = 0

Merton Gamma

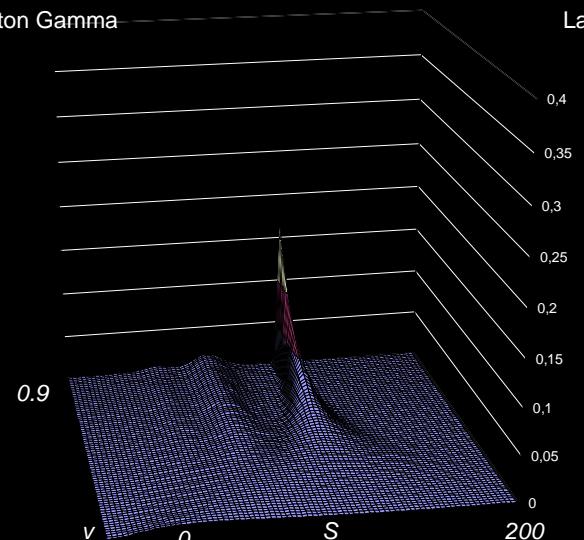


66



Merton Gamma

LambdaJ = 0.9 ↑

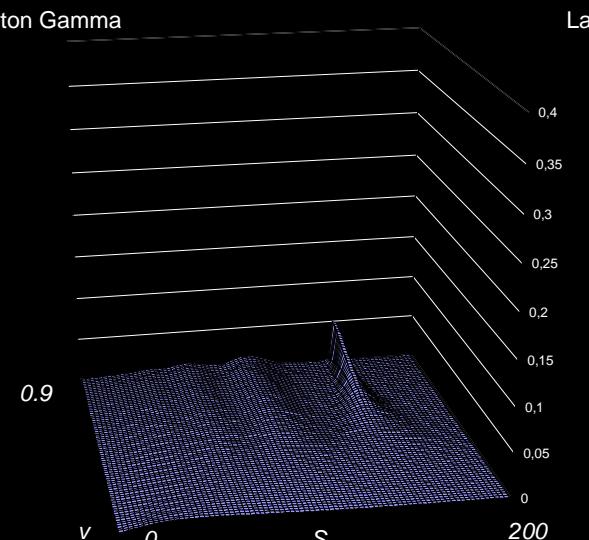


67



LambdaJ = 1.8 ↑

Merton Gamma



68



Merton Gamma

LambdaJ = 1.8

EtaJ = 0.1

MuJ= 0.5

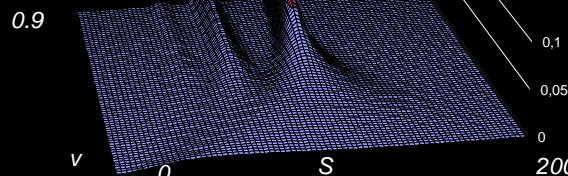


Merton Gamma

EtaJ = 0.1

LambdaJ = 0.5

MuJ= 0.5



69



Merton Gamma

EtaJ = 0.75

LambdaJ = 0.5

MuJ= 0.5

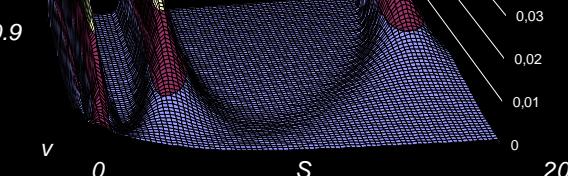


Merton Gamma

MuJ = 2.5

LambdaJ = 0.5

EtaJ= 0.1

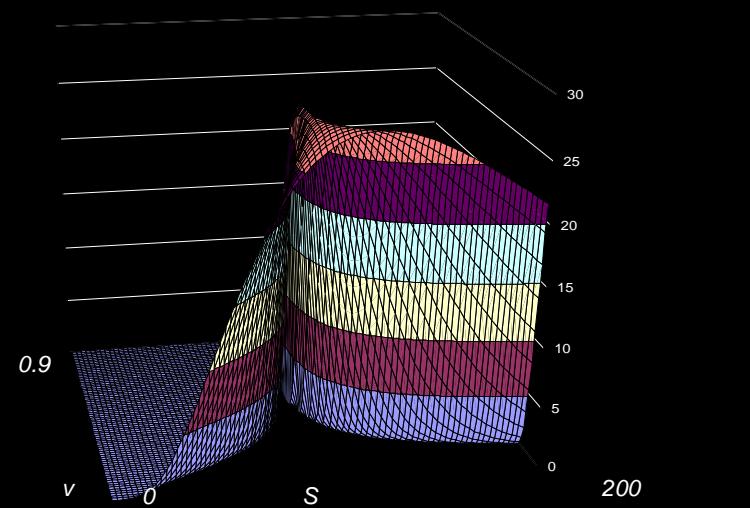


71

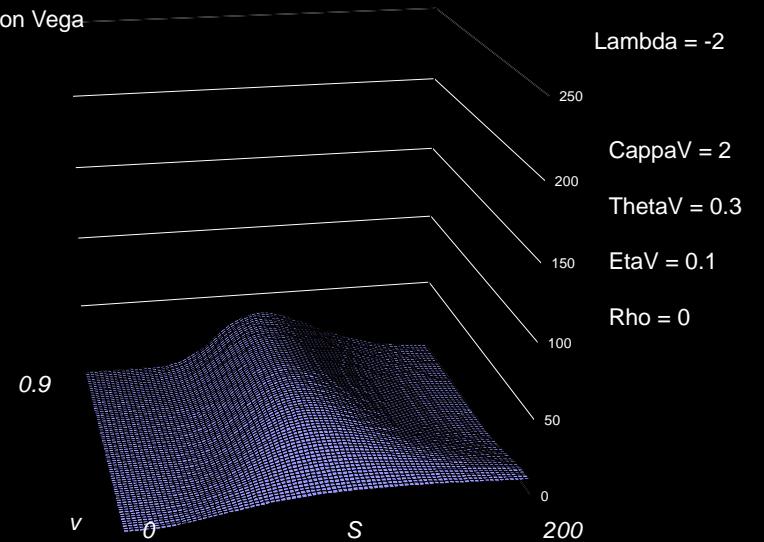


72

Black – Scholes Vega



Heston Vega

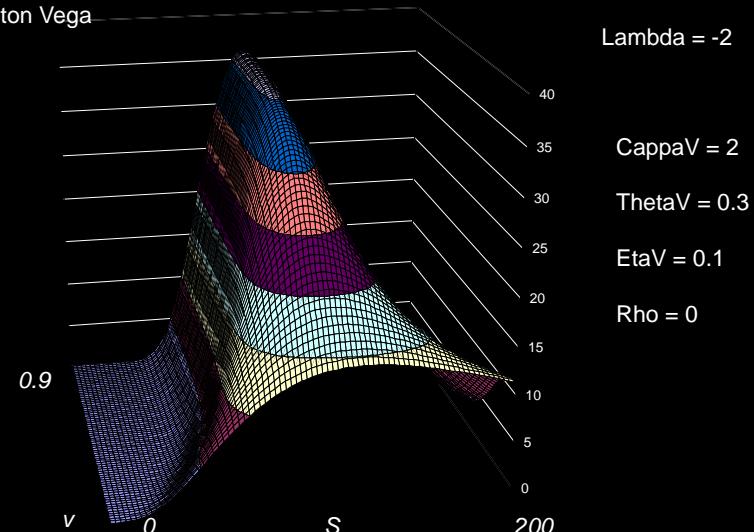


73



Heston Vega

Lambda = -2

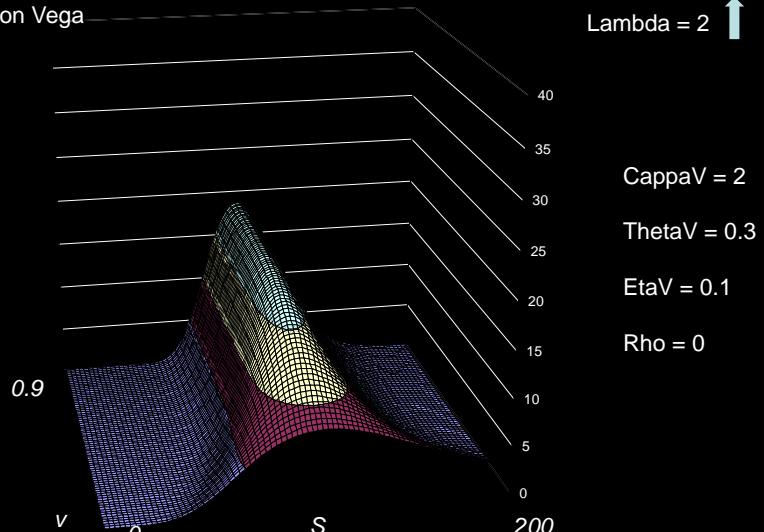


75



Heston Vega

Lambda = 2 ↑

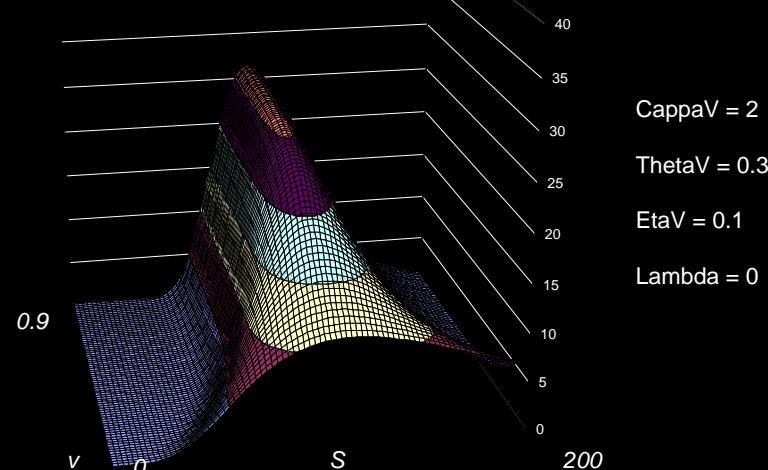


76



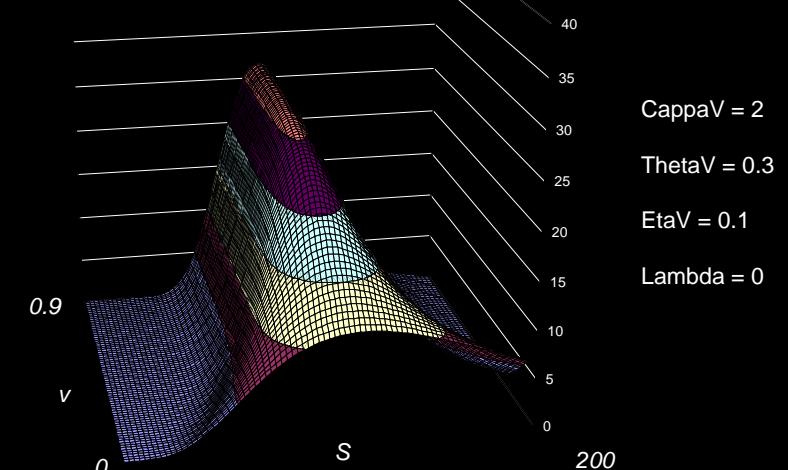
Heston Vega

Rho = -1



Heston Vega

Rho = 1

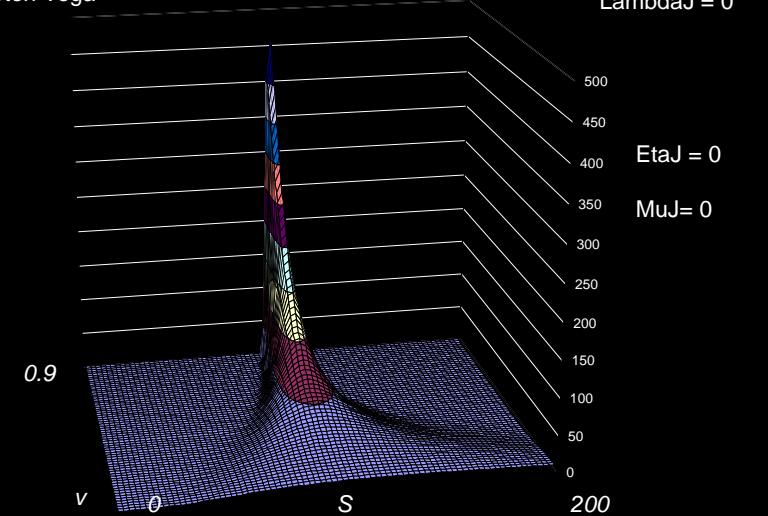


77



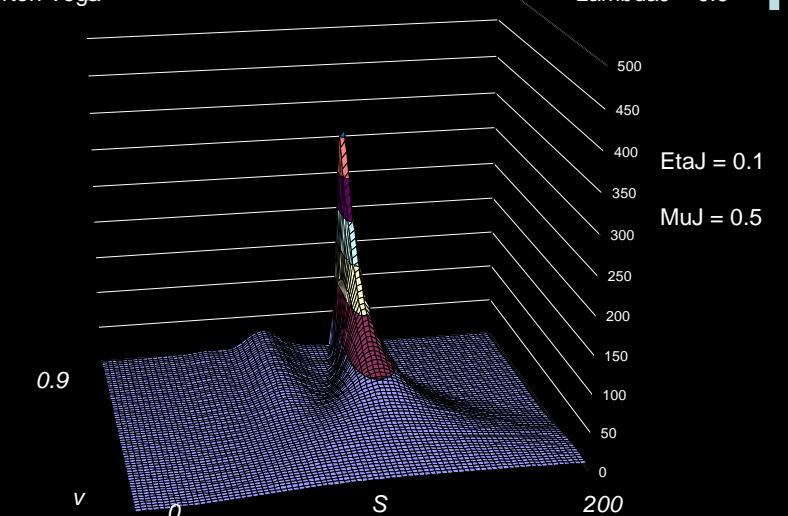
Merton Vega

LambdaJ = 0



Merton Vega

LambdaJ = 0.9



79



80



Merton Vega

LambdaJ = 1.8



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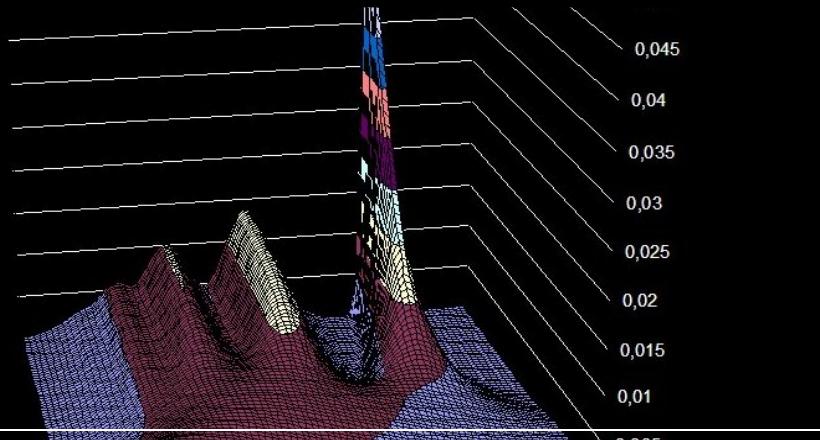
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# Masterclass: Implementing affine jump diffusion models at the trading desk



Marcello Minenna - Paolo Verzella  
Montecarlo – Derivatives and Risk Management Europe 2006

