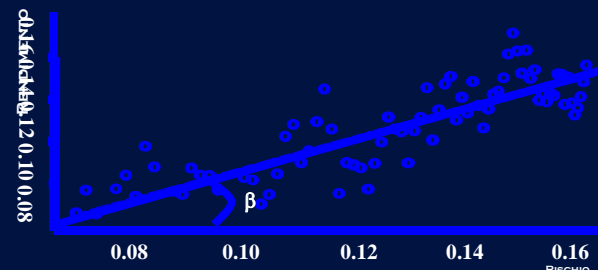
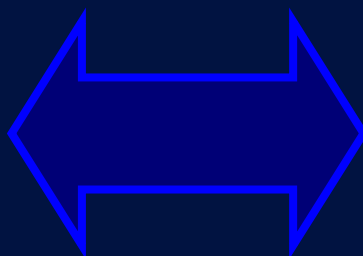


# DERIVATIVES RISK MANAGEMENT AND QUANT SURVEILLANCE



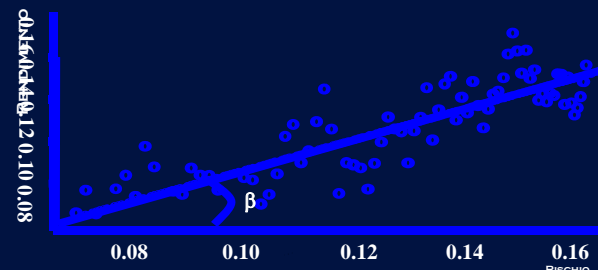
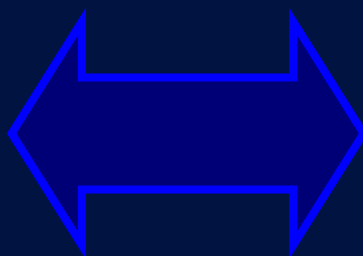
Cass Business School  
CITY UNIVERSITY LONDON

## RISK MANAGEMENT



... A COMPLEX SET OF GEARS RELATED TO RISK-  
RETURN OF FINANCIAL INSTRUMENTS

## RISK MANAGEMENT



... A COMPLEX SET OF GEARS RELATED TO RISK-RETURN OF FINANCIAL INSTRUMENTS



... THAT IS SIMULATED THROUGH PROCESSES

LET US DEFINE:

**S** PROCESS OF THE STOCK

**B** PROCESS OF THE BOND

*f* PROCESS OF THE DERIVATIVE

WHERE:

$$f=f(S,t)$$

# RISK MANAGEMENT: THE GREEK LETTERS

---

LET US DEFINE:

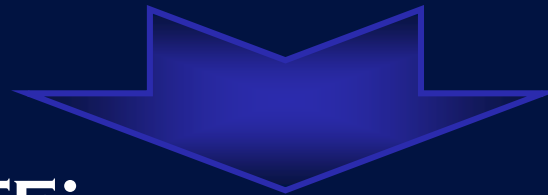
**S** PROCESS OF THE STOCK

**B** PROCESS OF THE BOND

*f* PROCESS OF THE DERIVATIVE

WHERE:

$$f = f(S, t)$$



LET US COMPUTE:

**V** REPLICATING PORTFOLIO OF THE DERIVATIVE

## REPLICATING PORTFOLIO OF THE DERIVATIVE

$$V_t = f(S, t) = N_S S_t + N_B B_t$$

**WHERE:**

$N_S$  NUMBER OF STOCKS

$N_B$  NUMBER OF BONDS

## DEFINITION OF THE PROCESSES

**HP:**

$$dS_t = \mu S_t dt + \sigma S_t dZ_t$$

**WHERE:**

$$dZ_t \sim \varepsilon \sqrt{dt} \quad \varepsilon \sim N(0, 1)$$

## DEFINITION OF THE PROCESSES

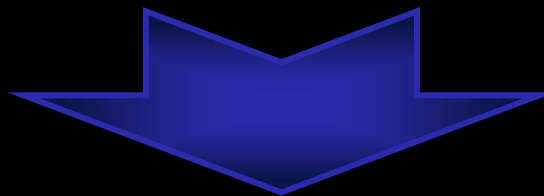
**HP:**

$$dS_t = \mu S_t dt + \sigma S_t dZ_t$$

**WHERE:**

$$dZ_t \sim \varepsilon \sqrt{dt}$$

$$\varepsilon \sim N(0, 1)$$



$$\frac{dS_t}{S_t} \sim N(\mu dt, \sigma^2 dt)$$



## DEFINITION OF THE PROCESSES

HP:

$$dB_t = r B_t dt$$

WHOSE SOLUTION IS:

$$B_t = e^{rt} \quad \forall t \in [0, T]$$

## DEFINITION OF THE PROCESSES

**HP:**

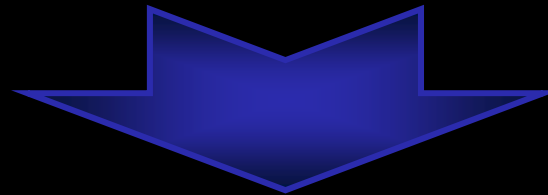
$$dV_t = N_S dS_t + N_B dB_t$$

**WHERE:**

$$V_t = f(S, t)$$

## APPLYING THE DEFINITIONS OF BOTH S AND B PROCESSES

$$dV_t = N_S dS_t + N_B dB_t$$



$$dV_t = N_S (\mu S_t dt + \sigma S_t dZ_t) + N_B (r B_t dt)$$

... MULTIPLYING

$$dV_t = N_S \mu S_t dt + N_S \sigma S_t dZ_t + N_B r B_t dt$$

... MULTIPLYING

$$dV_t = N_S \mu S_t dt + N_S \sigma S_t dZ_t + N_B r B_t dt$$

COLLECTING:

$$dV_t = (N_S \mu S_t + N_B r B_t) dt + \sigma S_t N_S dZ_t$$

LET US DEFINE:

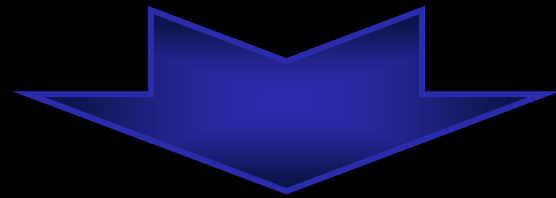
$$\mu S_t = a$$

$$\sigma S_t = b$$

LET US DEFINE:

$$\mu S_t = a$$

$$\sigma S_t = b$$



$$dS_t = a dt + b dZ_t$$

**ITO'S PROCESS**

THE SDE ASSOCIATED TO  $f=f(S,t)$  IS OBTAINED BY  
USING ITO'S LEMMA (BROWNIAN MOTION DIFFERENTIATING RULE)

$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} ds + \frac{1}{2} \sigma^2 \frac{\partial^2 f}{\partial S^2} dt$$



THE SDE ASSOCIATED TO  $f=f(S,t)$  IS OBTAINED BY  
USING ITO'S LEMMA (BROWNIAN MOTION DIFFERENTIATING RULE)

$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} ds + \frac{1}{2} b^2 \frac{\partial^2 f}{\partial S^2} dt$$

BY SUBSTITUTING THE SDE ASSOCIATED TO S  
WE OBTAIN:

$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} (a dt + b dZ_t) + \frac{1}{2} b^2 \frac{\partial^2 f}{\partial S^2} dt$$

... SIMPLIFYING

$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} a + \frac{1}{2} b^2 \frac{\partial^2 f}{\partial S^2} \right) dt + b \frac{\partial f}{\partial S} dZ_t$$

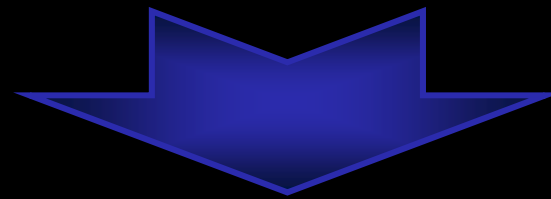
... SIMPLIFYING

$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} a + \frac{1}{2} b^2 \frac{\partial^2 f}{\partial S^2} \right) dt + b \frac{\partial f}{\partial S} dZ_t$$

REMEMBERING:

$$\mu S_t = a$$

$$\sigma S_t = b$$



$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$

BY RECALLING THE HP:

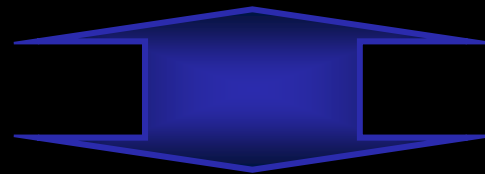
$$dV_t = df$$

BY RECALLING THE HP:

$$dV_t = df$$

... LET US COMPARE THE STOCHASTIC COMPONENTS:

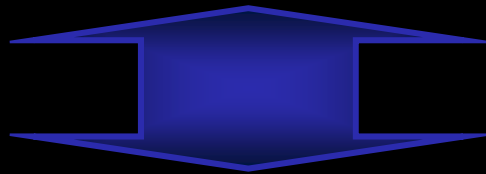
$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$



$$dV_t = (N_S \mu S_t + N_B r B_t) dt + \sigma S_t N_S dZ_t$$


... THAT IS:

$$\sigma S_t N_s dZ_t$$



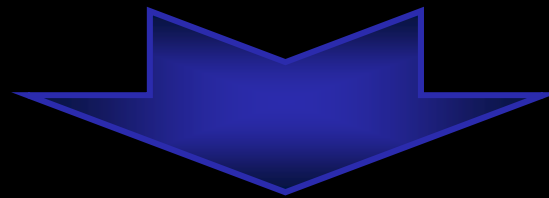
$$\sigma S_t \frac{\partial f}{\partial S} dZ_t$$

... THAT IS:


$$\sigma S_t N_\delta dZ_t$$
$$\sigma S_t \frac{\partial f}{\partial S} dZ_t$$
$$N_\delta = \frac{\partial f}{\partial S}$$

**BY REMEMBERING:**

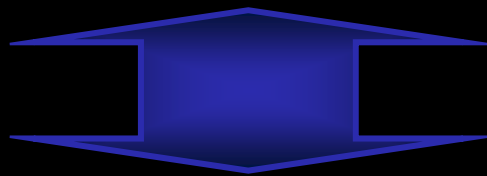
$$V_t = f(S, t) = N_S S_t + N_B B_t$$



$$N_B = \frac{1}{B} (f(S, t) - N_S S)$$

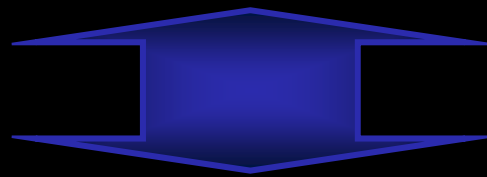


$$N_s = \frac{\partial f}{\partial S}$$



$$N_B = \frac{1}{B} (f(S, t) - N_s S)$$

$$N_S = \frac{\partial f}{\partial S}$$

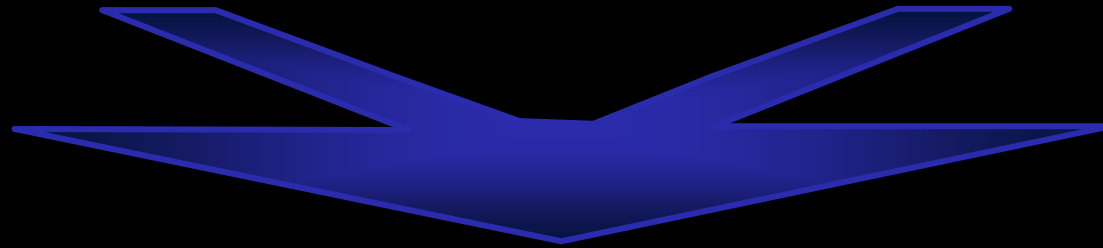


$$N_B = \frac{1}{B} \left( f(S, t) - \frac{\partial f}{\partial S} S \right)$$

$$N_B = \frac{1}{B} (f(S, t) - N_S S)$$

BY SUBSTITUTING IN THE SDE OF  $V$

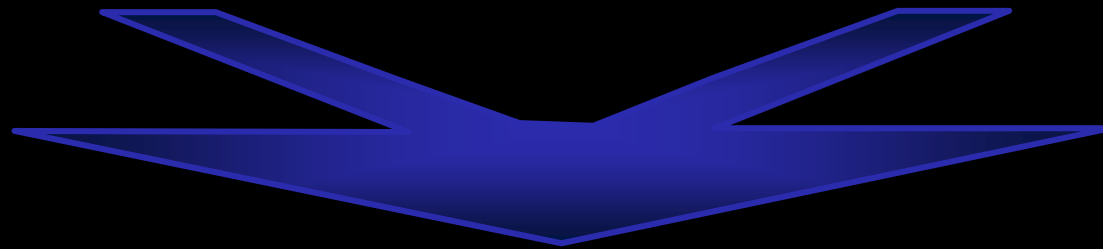
$$N_S = \frac{\partial f}{\partial S} \qquad N_B = \frac{1}{B} \left( f(S, t) - \frac{\partial f}{\partial S} S \right)$$



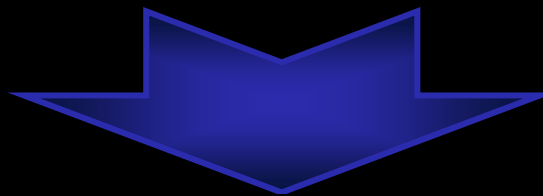
$$dV_t = (N_S \mu S_t + N_B r B_t) dt + \sigma S_t N_S dZ_t$$

BY SUBSTITUTING IN THE SDE OF V

$$N_S = \frac{\partial f}{\partial S} \qquad N_B = \frac{1}{B} \left( f(S, t) - \frac{\partial f}{\partial S} S \right)$$



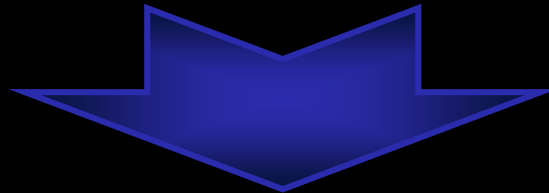
$$dV_t = (N_S \mu S_t + N_B r B_t) dt + \sigma S_t N_S dZ_t$$



$$dV_t = \left( \frac{\partial f}{\partial S} \mu S_t + \frac{1}{B} \left( f(S, t) - \frac{\partial f}{\partial S} S \right) r B_t \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$

## SIMPLIFYING:

$$dV_t = \left( \frac{\partial f}{\partial S} \mu S_t + \frac{1}{B} \left( f(S, t) - \frac{\partial f}{\partial S} S \right) r B_t \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$



$$dV_t = \left( \frac{\partial f}{\partial S} \mu S_t + r f(S, t) - \frac{\partial f}{\partial S} r S \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$

BY RECALLING THE HP:

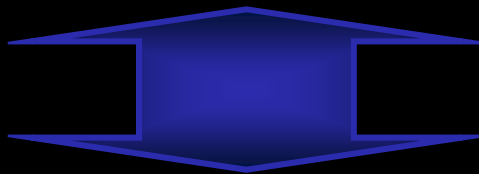
$$dV_t = df$$

BY RECALLING THE HP:

$$dV_t = df$$

... LET US COMPARE THE DETERMINISTIC COMPONENTS:

$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$

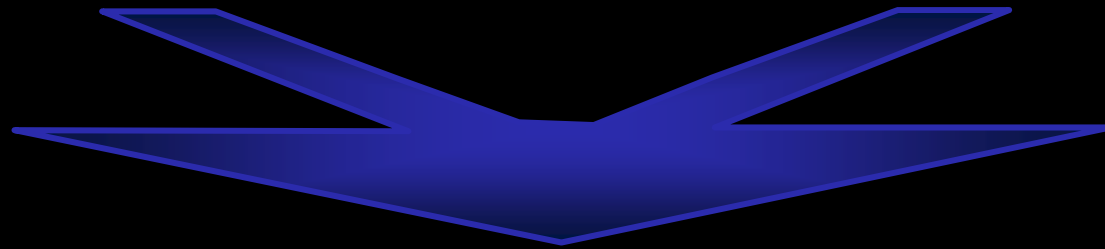


$$dV_t = \left( \frac{\partial f}{\partial S} \mu S_t + r f(S, t) - \frac{\partial f}{\partial S} r S \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$

$$\left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) = \left( \frac{\partial f}{\partial S} \mu S_t + r f(S, t) - \frac{\partial f}{\partial S} r S \right)$$



$$\left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) = \left( \frac{\partial f}{\partial S} \mu S_t + r f(S, t) - \frac{\partial f}{\partial S} r S \right)$$

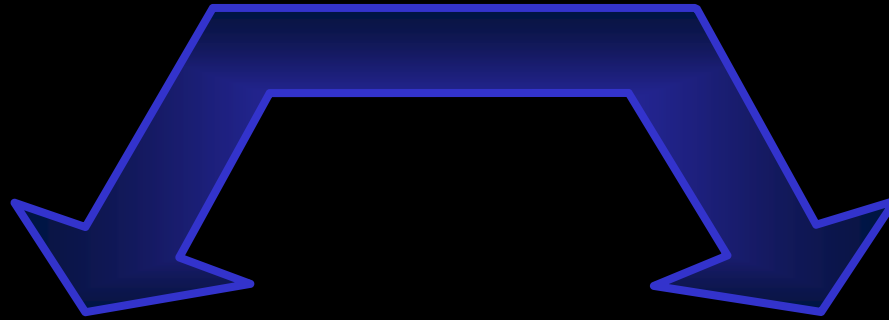


$$\left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} r S + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) = r f(S, t)$$

**... ALSO KNOWN AS BLACK-SCHOLES PDE**

... CONSIDERING THAT THE  $dZ$  COMPONENT IS THE  
SAME BOTH FOR  $dV$  AND  $df$

... CONSIDERING THAT THE  $dZ$  COMPONENT IS THE SAME BOTH FOR  $dV$  AND  $df$



**BLACK-SCHOLES PDE  
DESCRIBES**

$$f=f(S,t)$$

**AS TIME ELAPSES**

**THE DERIVATIVE CAN BE  
REPLICATED BY**

$N_S$  NUMBER OF STOCKS

$N_B$  NUMBER OF BONDS

... LET US DEFINE

$$\Theta = \frac{\partial f}{\partial t}$$

$$\Delta = \frac{\partial f}{\partial S}$$

$$\Gamma = \frac{\partial^2 f}{\partial S^2}$$

... LET US DEFINE

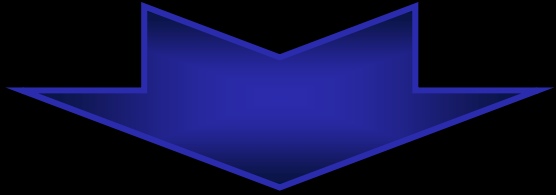
$$\Theta = \frac{\partial f}{\partial t}$$

$$\Delta = \frac{\partial f}{\partial S}$$

$$\Gamma = \frac{\partial^2 f}{\partial S^2}$$


$$dV = df$$

$$\left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} r S + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) = r f(S, t)$$


$$\left( \Theta + \Delta r S + \frac{1}{2} (\sigma S_t)^2 \Gamma \right) = r f(S, t)$$

IT IS IMPORTANT TO OBSERVE THAT WE CAN  
COMPUTE THE DIFFERENTIAL EXPRESSION  
OF  $f=f(S,t)$  BOTH WITH TAYLOR'S FORMULA  
AND WITH ITO'S LEMMA OBTAINING  
THE SAME RESULT

## COMPUTATION OF $df$ BY MEANS OF TAYLOR'S FORMULA

## COMPUTATION OF $df$ BY MEANS OF TAYLOR'S FORMULA

LET US REMEMBER THAT  $dS$  IS OF ORDER  $\sqrt{dt}$

$$dS_t = \mu S_t dt + \sigma S_t dZ_t \quad dZ_t \sim \varepsilon \sqrt{dt}$$



## COMPUTATION OF $df$ BY MEANS OF TAYLOR'S FORMULA

LET US REMEMBER THAT  $dS$  IS OF ORDER  $\sqrt{dt}$

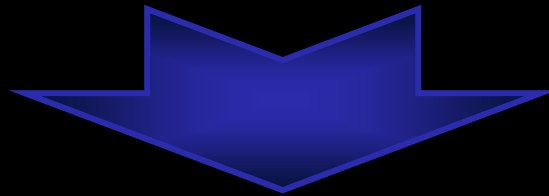
$$dS_t = \mu S_t dt + \sigma S_t dZ_t \quad dZ_t \sim \varepsilon \sqrt{dt}$$

IT IS POSSIBLE TO EXTEND TAYLOR'S FACTORIZATION TO  $o(dt)$

$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} dS + \frac{1}{2} \frac{\partial^2 f}{\partial S^2} dS^2 + o(dt)$$

## SUBSTITUTING THE DEFINITION OF $dS$ IN $df$

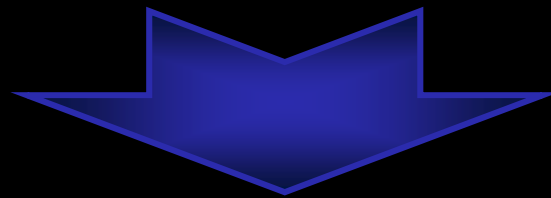
$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} dS + \frac{1}{2} \frac{\partial^2 f}{\partial S^2} dS^2 + o(dt)$$



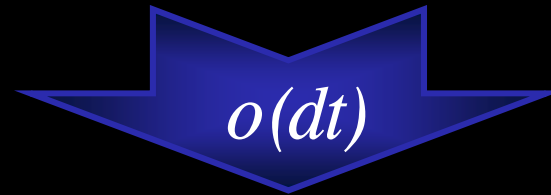
$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} (\mu S_t dt + \sigma S_t dZ_t) + \frac{1}{2} \frac{\partial^2 f}{\partial S^2} (\mu S_t dt + \sigma S_t dZ_t)^2 + o(dt)$$

LET US FOCUS ON:

$$(\mu S_t dt + \sigma S_t dZ_t)^2$$



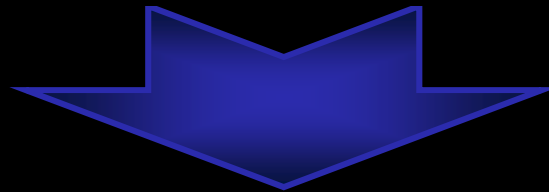
$$(\mu^2 S_t^2 dt^2 + \sigma^2 S_t^2 dt + 2\mu S_t \sigma S_t dZ_t dt)$$



$$\sigma^2 S_t^2 dt$$

## ... SIMPLIFYING

$$df = \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial S} (\mu S_t dt + \sigma S_t dZ_t) + \frac{1}{2} \sigma^2 S_t^2 dt + o(dt)$$



$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t + o(dt)$$

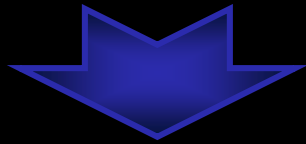
$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t + o(dt)$$

TAYLOR  
VS.  
ITO

$$df = \left( \frac{\partial f}{\partial t} + \frac{\partial f}{\partial S} \mu S_t + \frac{1}{2} (\sigma S_t)^2 \frac{\partial^2 f}{\partial S^2} \right) dt + \sigma S_t \frac{\partial f}{\partial S} dZ_t$$

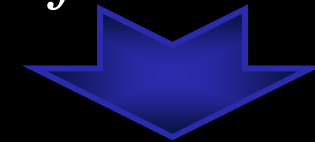
Q.E.D.

**... BUT IF TAYLOR'S  
FACTORIZATION**



**LEADS TO THE SAME  
RESULT OF ITO'S  
LEMMA**

... BUT IF ITO'S  
LEMMA HAS SHOWN  
THAT  $df = dV$



... THAT IS THE VALUE OF A  
DERIVATIVE CAN BE STUDIED  
BY MEANS OF THE VALUE OF A  
PORTFOLIO CONSTITUTED BY

$N_s$  NUMBER OF STOCKS  
 $N_B$  NUMBER OF BONDS

... SO LET US USE TAYLOR'S FACTORIZATION  
IN ORDER TO STUDY WHAT HAPPENS WHEN

$$f = f(S, t, \sigma)$$

WITHOUT LOOSING GENERALITY



## DERIVATION OF $df$ WITH TAYLOR'S FORMULA

$$df = \frac{\partial f}{\partial t}dt + \frac{\partial f}{\partial S}dS + \frac{\partial f}{\partial \sigma}d\sigma + \frac{1}{2}\frac{\partial^2 f}{\partial S^2}dS^2 + \frac{1}{2}\frac{\partial^2 f}{\partial \sigma^2}d\sigma^2 + \frac{1}{2}\frac{\partial^2 f}{\partial t^2}dt^2 + \frac{\partial f}{\partial S\partial t}dtdS + \dots + o(dt)$$

WE CAN EXPAND TAYLOR'S FACTORIZATION TO  $o(dt)$

$$df = \frac{\partial f}{\partial t}dt + \frac{\partial f}{\partial S}dS + \frac{\partial f}{\partial \sigma}d\sigma + \frac{1}{2}\frac{\partial^2 f}{\partial S^2}dS^2 + o(dt)$$

... LET US DEFINE

$$\Theta = \frac{\partial f}{\partial t}$$

$$\Delta = \frac{\partial f}{\partial S}$$

$$\nu = \frac{\partial f}{\partial \sigma}$$

$$\Gamma = \frac{\partial^2 f}{\partial S^2}$$

... LET US DEFINE

$$\Theta = \frac{\partial f}{\partial t}$$

$$\Delta = \frac{\partial f}{\partial S}$$

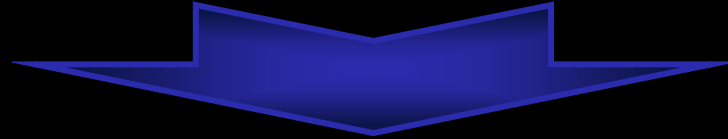
$$v = \frac{\partial f}{\partial \sigma}$$

$$\Gamma = \frac{\partial^2 f}{\partial S^2}$$


$$dV = df$$

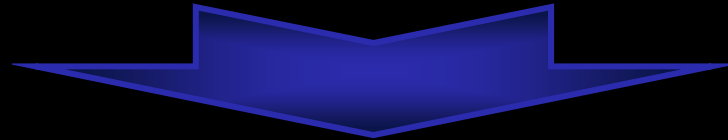
$$df = \Theta dt + \Delta dS + v d\sigma + \frac{1}{2} \Gamma dS^2 + o(dt)$$

... BECAUSE WE HAVE SHOWN THAT  $dV = df$

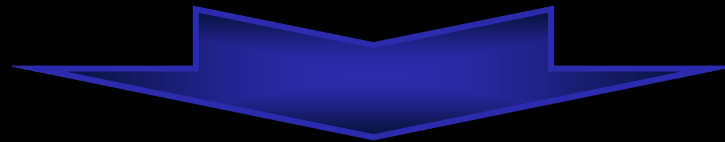


**IN ORDER TO AVOID DIFFERENCES IN THE PORTFOLIO**

... BECAUSE WE HAVE SHOWN THAT  $dV = df$

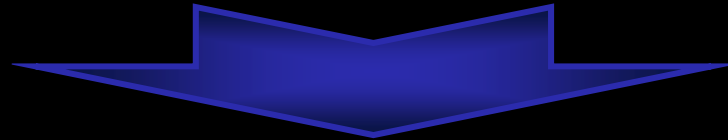


IN ORDER TO AVOID DIFFERENCES IN THE PORTFOLIO

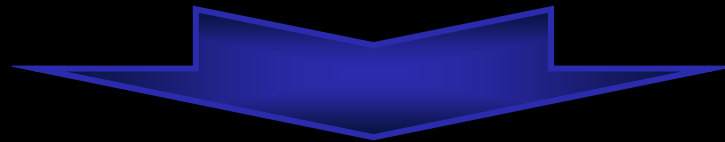


$$dV = df = 0$$

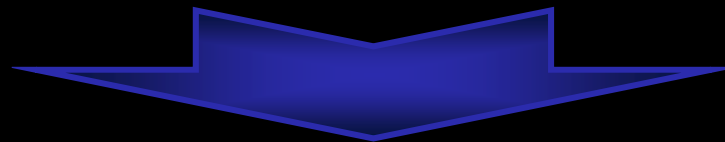
... BECAUSE WE HAVE SHOWN THAT  $dV = df$



IN ORDER TO AVOID DIFFERENCES IN THE PORTFOLIO




$$dV = df = 0$$



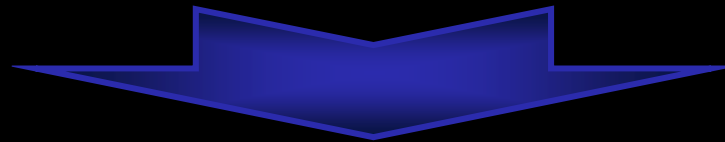
$$0 = \Theta dt + \Delta dS + v d\sigma + \frac{1}{2} \Gamma dS^2$$

...HEDGING IN PRACTICE IS BASED ON THE GREEKS


$$0 = \Theta dt + \Delta dS + v d\sigma + \frac{1}{2} \Gamma dS^2$$

## HEDGING ACTIVITY IN PRACTICE

### HP: BLACK-SCHOLES' WORLD



$$C_t = S_t N(d_1) - Ke^{-r(T-t)} N(d_2)$$

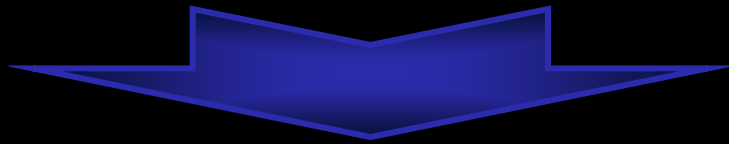
$$P_t = Ke^{-r(T-t)} N(-d_2) - S_t N(-d_1)$$

$$d_1 = \frac{\ln \frac{S_t}{K} + \left(r + \frac{\sigma^2}{2}\right)(T-t)}{\sigma\sqrt{T-t}}$$

$$d_2 = \frac{\ln \frac{S_t}{K} + \left(r - \frac{\sigma^2}{2}\right)(T-t)}{\sigma\sqrt{T-t}}$$

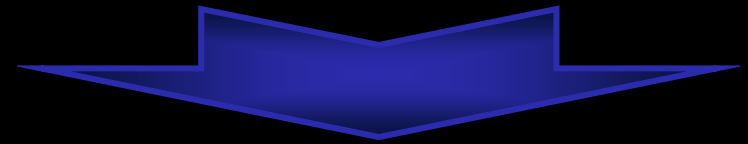


## CALL



$$\Delta_{call} = N(d_1)$$

## PUT



$$\Delta_{put} = N(d_1) - 1$$

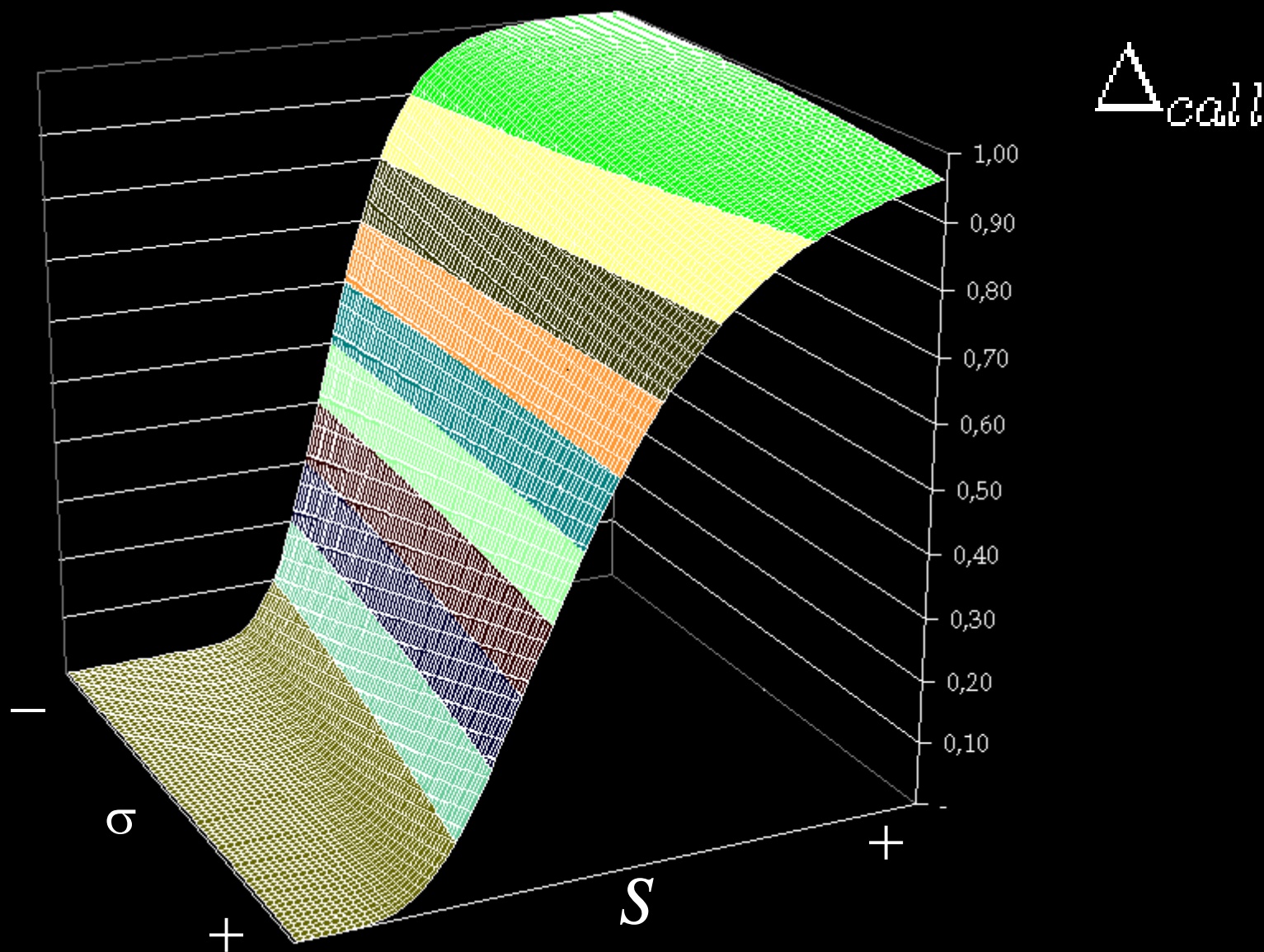
$$\Gamma = \frac{N'(d_1)}{S\sigma\sqrt{T-t}}$$

$$v = S \cdot N'(d_1)\sqrt{T-t}$$

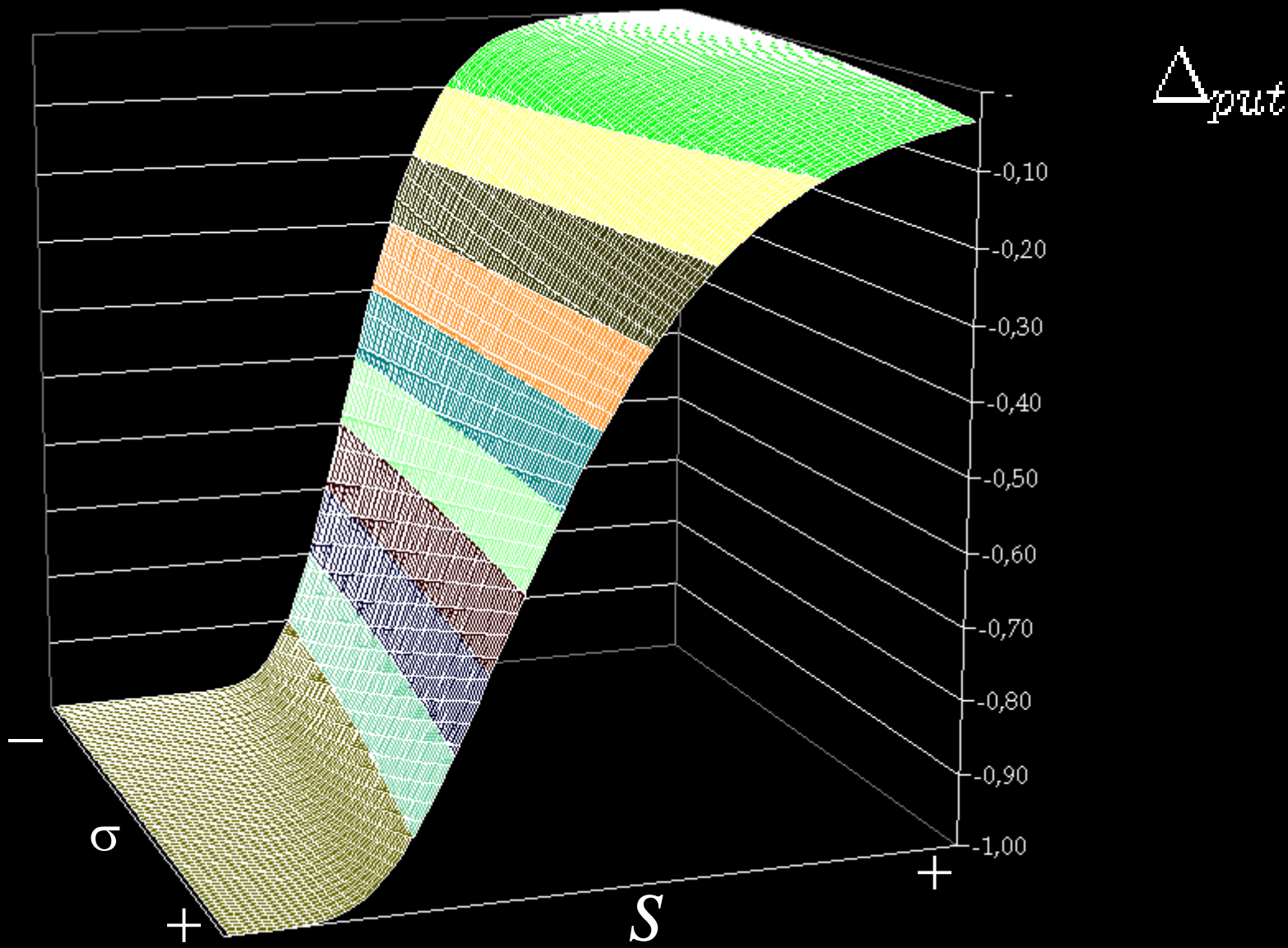
$$\Theta_{call} = (T-t)Ke^{-r(T-t)}N(d_2)$$

$$\Theta_{put} = -(T-t)Ke^{-r(T-t)}N(-d_2)$$

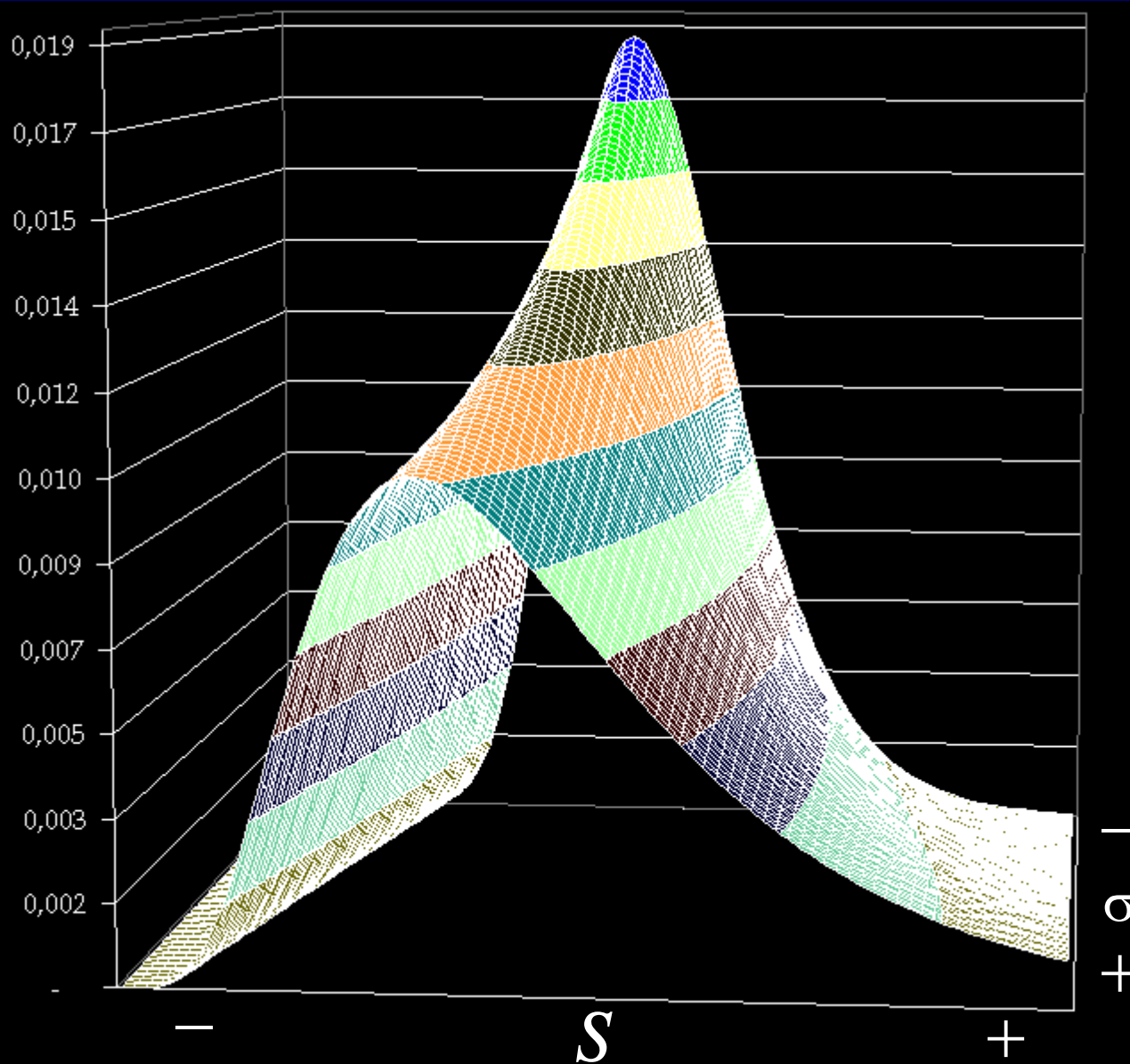
# RISK MANAGEMENT: THE GREEK LETTERS



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# RISK MANAGEMENT: THE GREEK LETTERS



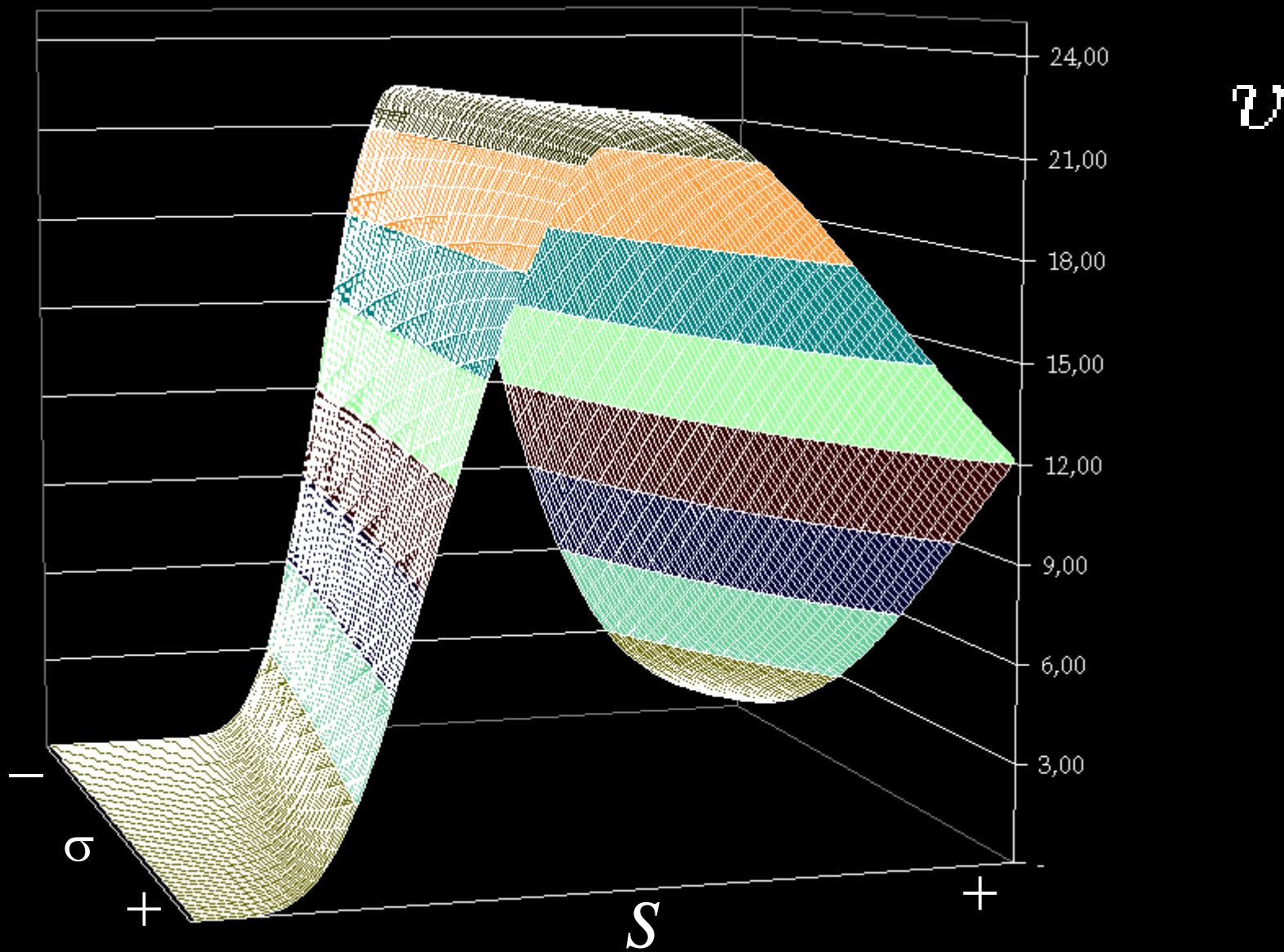
$\Gamma$

$\sigma$   
+

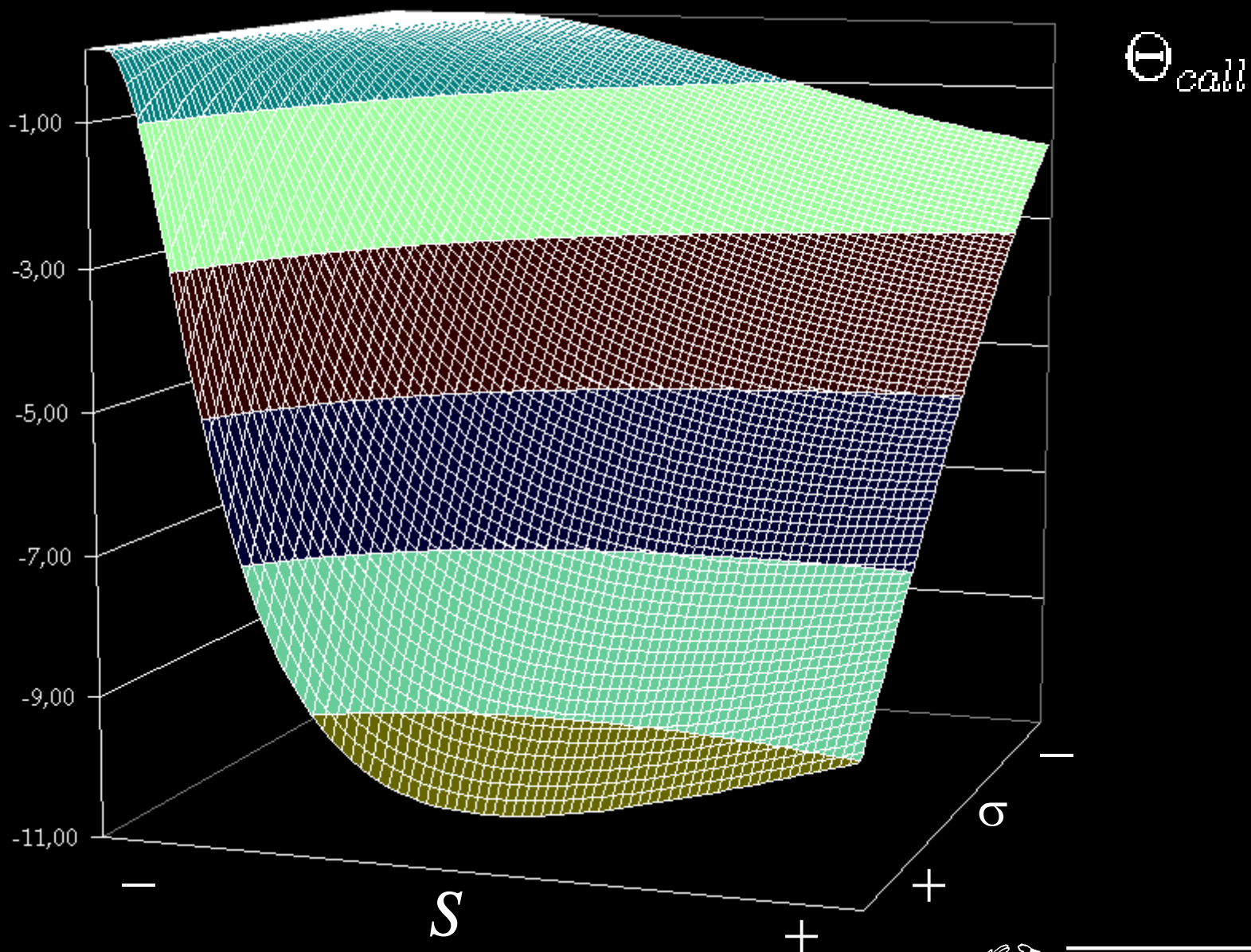
$S$   
60



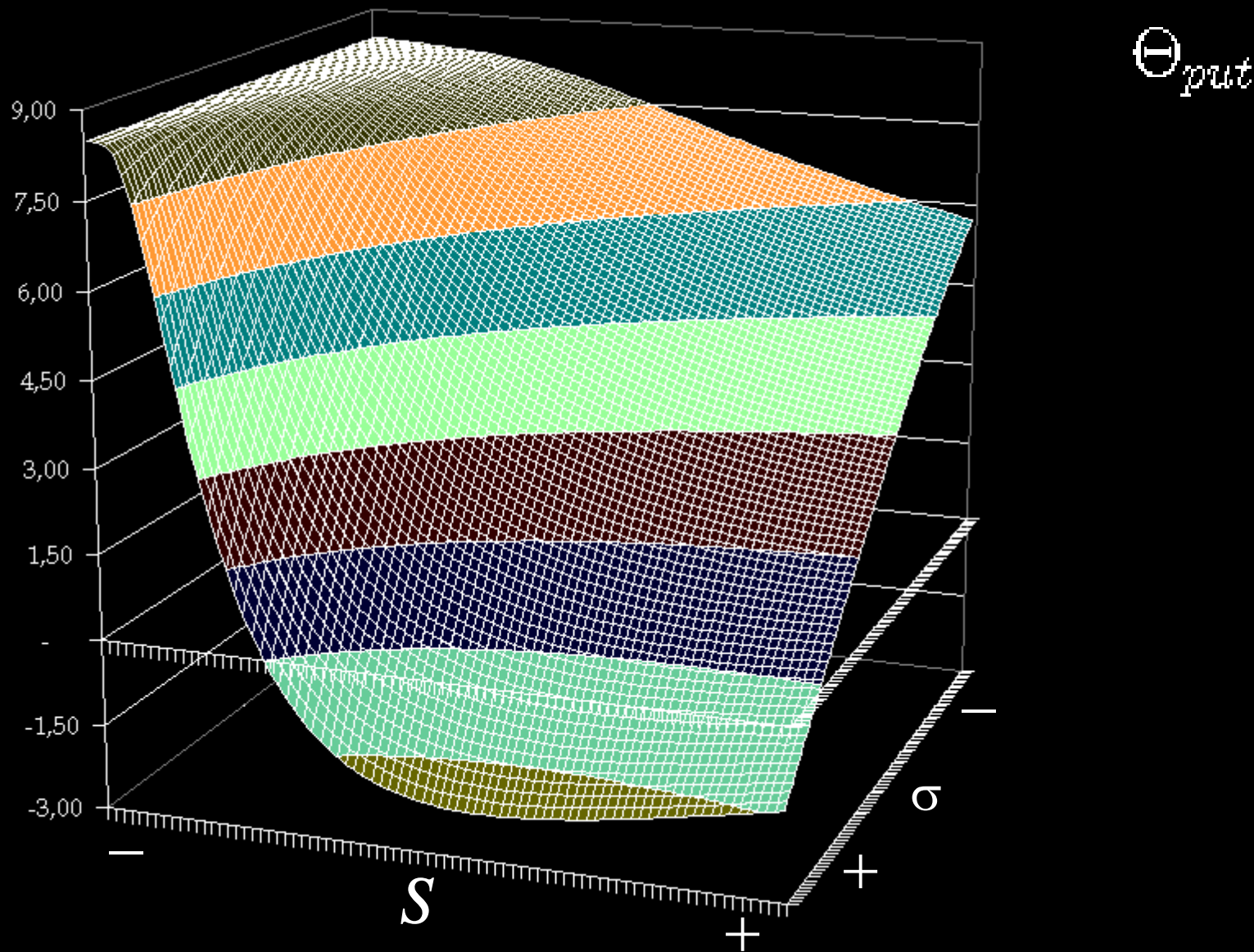
# RISK MANAGEMENT: THE GREEK LETTERS



# RISK MANAGEMENT: THE GREEK LETTERS



# RISK MANAGEMENT: THE GREEK LETTERS



## GREEK LETTERS ARE ADDITIVE

$$\text{PORFOLIO GREEK} = \sum_i w_i \text{GREEK}$$

$$\sum_i w_i = 1$$



## $\Delta$ HEDGING

COMPUTATION OF  $df$  BY MEANS OF A FIRST ORDER TAYLOR'S FORMULA

$$df \approx \Delta dS + o(dt)$$

**AT TIME  $T=0$  SHORT 1 CALL**

**AT MATURITY THE OPTION IS**

**IN – THE MONEY**

# Δ HEDGING - SHORT 1 CALL - IN – THE MONEY

Short 1000 call on 1 stock			Option and Δ			Stock and Δ				Δ Portfolio
Time Step	Time to Expiration	STOCK PRICE	Q. Opz.	Δ call	Δ call Posit.	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position
0	0,2500	100,0	(1.000)	0,564115961	(564)	564	564	1	564	-
1	0,2375	104,0	(1.000)	0,624630657	(625)	61	625	1	625	-
2	0,2250	100,4	(1.000)	0,567671079	(568)	(57)	568	1	568	-
3	0,2125	93,8	(1.000)	0,449626897	(450)	(118)	450	1	450	-
4	0,2000	103,3	(1.000)	0,613419529	(613)	163	613	1	613	-
5	0,1875	121,6	(1.000)	0,850633639	(851)	238	851	1	851	-
6	0,1750	120,9	(1.000)	0,850534322	(851)	-	851	1	851	-
7	0,1625	120,5	(1.000)	0,853571891	(854)	3	854	1	854	-
8	0,1500	122,9	(1.000)	0,88234869	(882)	28	882	1	882	-
9	0,1375	129,0	(1.000)	0,931634606	(932)	50	932	1	932	-
10	0,1250	130,2	(1.000)	0,944999861	(945)	13	945	1	945	-
11	0,1125	126,8	(1.000)	0,935342021	(935)	(10)	935	1	935	-
12	0,1000	131,7	(1.000)	0,966714307	(967)	32	967	1	967	-
13	0,0875	139,1	(1.000)	0,989168909	(989)	22	989	1	989	-
14	0,0750	162,9	(1.000)	0,999121066	(999)	10	999	1	999	-
15	0,0625	165,4	(1.000)	0,999355248	(999)	-	999	1	999	-
16	0,0500	162,1	(1.000)	0,999494634	(999)	-	999	1	999	-
17	0,0375	162,1	(1.000)	0,999624853	(1.000)	1	1.000	1	1.000	-
18	0,0250	157,1	(1.000)	0,999750027	(1.000)	-	1.000	1	1.000	-
19	0,0125	148,4	(1.000)	0,999875008	(1.000)	-	1.000	1	1.000	-
20	0,0000	150,0	(1.000)	1	(1.000)	-	1.000	1	1.000	-



# Δ HEDGING - SHORT 1 CALL - IN – THE MONEY

Delta Hedging Cash Flow						Delta Hedging portfolio "A" Value				
Stock	Option	Bank			Hedging Revenue (cost)	Replicating Portfolio			Option value	Unwind value
Dollars in Stock (flow)	Cash ex Shorting/Exercising Option	Cash	Interest (flow)	Borrow (stock)		Dollars in Stock (stock)	Bank	Portfolio Value		
56.400	10.378	46.022		46.022		56.400	(46.022)	10.378	(10.378)	-
6.344		6.344	28,8	52.395		64.997	(52.395)	12.602	(12.480)	122
(5.723)		(5.723)	32,8	46.704		57.032	(46.704)	10.327	(10.060)	267
(11.072)		(11.072)	29,2	35.662		42.223	(35.662)	6.562	(6.429)	133
16.833		16.833	22,3	52.517		63.304	(52.517)	10.787	(11.167)	(380)
28.940		28.940	32,8	81.490		103.479	(81.490)	21.989	(24.517)	(2.528)
-		-	50,9	81.541		102.880	(81.541)	21.339	(23.677)	(2.338)
361		361	51,0	81.953		102.901	(81.953)	20.948	(23.089)	(2.141)
3.442		3.442	51,2	85.446		108.417	(85.446)	22.971	(24.957)	(1.986)
6.452		6.452	53,4	91.952		120.274	(91.952)	28.322	(30.315)	(1.993)
1.692		1.692	57,5	93.702		123.026	(93.702)	29.324	(31.207)	(1.883)
(1.268)		(1.268)	58,6	92.493		118.532	(92.493)	26.039	(27.818)	(1.779)
4.216		4.216	57,8	96.766		127.392	(96.766)	30.626	(32.385)	(1.759)
3.060		3.060	60,5	99.886		137.543	(99.886)	37.657	(39.460)	(1.804)
1.629		1.629	62,4	101.578		162.729	(101.578)	61.152	(63.145)	(1.994)
-		-	63,5	101.641		165.235	(101.641)	63.593	(65.609)	(2.015)
-		-	63,5	101.705		161.986	(101.705)	60.282	(62.317)	(2.036)
162		162	63,6	101.931		162.108	(101.931)	60.178	(62.235)	(2.057)
-		-	63,7	101.994		157.110	(101.994)	55.116	(57.196)	(2.080)
-		-	63,8	102.058		148.442	(102.058)	46.384	(48.486)	(2.102)
-	(100.000)	-	63,8	102.122	(2.122)	149.961	(102.122)	47.839	(49.961)	(2.122)

**AT TIME  $T=0$  SHORT 1 CALL**

**AT MATURITY THE OPTION IS  
OUT – THE MONEY**

# Δ HEDGING - SHORT 1 CALL - OUT – THE MONEY

Short 1000 call on 1 stock			Option and Δ			Stock and Δ				Δ Portfolio
Time Step	Time to Expiration	STOCK PRICE	Q. Opz.	Δ call	Δ call Posit.	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position
0	0,2500	100,0	(1.000)	0,564115961	(564)	564	564	1	564	-
1	0,2375	107,1	(1.000)	0,669595731	(670)	106	670	1	670	-
2	0,2250	98,7	(1.000)	0,539965684	(540)	(130)	540	1	540	-
3	0,2125	98,6	(1.000)	0,535439952	(535)	(5)	535	1	535	-
4	0,2000	98,1	(1.000)	0,52274553	(523)	(12)	523	1	523	-
5	0,1875	100,9	(1.000)	0,572217366	(572)	49	572	1	572	-
6	0,1750	103,8	(1.000)	0,623229667	(623)	51	623	1	623	-
7	0,1625	89,9	(1.000)	0,346231134	(346)	(277)	346	1	346	-
8	0,1500	83,0	(1.000)	0,201859233	(202)	(144)	202	1	202	-
9	0,1375	77,9	(1.000)	0,110027376	(110)	(92)	110	1	110	-
10	0,1250	74,6	(1.000)	0,061492554	(61)	(49)	61	1	61	-
11	0,1125	76,9	(1.000)	0,072830535	(73)	12	73	1	73	-
12	0,1000	70,2	(1.000)	0,016432088	(16)	(57)	16	1	16	-
13	0,0875	68,9	(1.000)	0,007800759	(8)	(8)	8	1	8	-
14	0,0750	69,5	(1.000)	0,005051823	(5)	(3)	5	1	5	-
15	0,0625	69,9	(1.000)	0,002681681	(3)	(2)	3	1	3	-
16	0,0500	64,8	(1.000)	7,23394E-05	-	(3)	-	1	-	-
17	0,0375	62,8	(1.000)	1,05616E-06	-	-	-	1	-	-
18	0,0250	63,0	(1.000)	3,36141E-09	-	-	-	1	-	-
19	0,0125	64,5	(1.000)	2,6642E-15	-	-	-	1	-	-
20	0,0000	66,7	(1.000)	0	-	-	-	1	-	-

# Δ HEDGING - SHORT 1 CALL - OUT – THE MONEY

Delta Hedging Cash Flow						Delta Hedging portfolio "A" Value				
Stock	Option	Bank			Hedging Revenue (cost)	Replicating Portfolio			Option value	Unwind value
Dollars in Stock (Flow)	Cash ex Shorting/Exercising Option	Cash	Interest (Flow)	Borrow (stock)		Dollars in Stock (stock)	Bank	Portfolio Value		
56.400	10.378	46.022		46.022		56.400	(46.022)	10.378	(10.378)	-
11.355		11.355	28,8	57.406		71.772	(57.406)	14.366	(14.505)	(139)
(12.837)		(12.837)	35,9	44.605		53.324	(44.605)	8.719	(9.141)	(422)
(493)		(493)	27,9	44.140		52.762	(44.140)	8.622	(8.790)	(168)
(1.177)		(1.177)	27,6	42.991		51.282	(42.991)	8.291	(8.201)	91
4.945		4.945	26,9	47.962		57.721	(47.962)	9.759	(9.464)	295
5.294		5.294	30,0	53.286		64.674	(53.286)	11.388	(10.883)	504
(24.908)		(24.908)	33,3	28.411		31.113	(28.411)	2.702	(3.783)	(1.081)
(11.953)		(11.953)	17,8	16.476		16.768	(16.476)	292	(1.662)	(1.370)
(7.166)		(7.166)	10,3	9.321		8.568	(9.321)	(753)	(711)	(1.465)
(3.655)		(3.655)	5,8	5.672		4.550	(5.672)	(1.122)	(328)	(1.450)
923		923	3,5	6.598		5.615	(6.598)	(983)	(392)	(1.376)
(4.001)		(4.001)	4,1	2.601		1.123	(2.601)	(1.478)	(62)	(1.540)
(551)		(551)	1,6	2.051		551	(2.051)	(1.499)	(25)	(1.525)
(208)		(208)	1,3	1.844		347	(1.844)	(1.497)	(15)	(1.511)
(140)		(140)	1,2	1.705		210	(1.705)	(1.496)	(7)	(1.502)
(195)		(195)	1,1	1.512		-	(1.512)	(1.512)	(0)	(1.512)
-		-	0,9	1.513		-	(1.513)	(1.513)	(0)	(1.513)
-		-	0,9	1.514		-	(1.514)	(1.514)	0	(1.514)
-		-	0,9	1.515		-	(1.515)	(1.515)	-	(1.515)
-		-	0,9	1.516	(1.516)	-	(1.516)	(1.516)	-	(1.516)

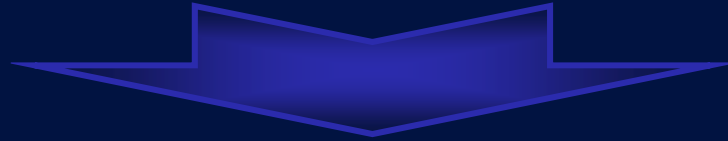
## $\Delta$ - $\Gamma$ HEDGING

COMPUTATION OF  $df$  BY MEANS OF A SECOND ORDER TAYLOR'S FORMULA

$$df \approx \Delta dS + \frac{1}{2} \Gamma dS^2 + o(dt)$$

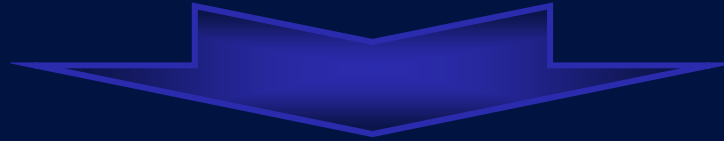


AT TIME  $T=0$  SHORT 1 CALL



LET US BUILD OUR PORTFOLIO  
IN ORDER TO BE  $\Delta$  NEUTRAL

AT TIME  $T=0$  SHORT 1 CALL

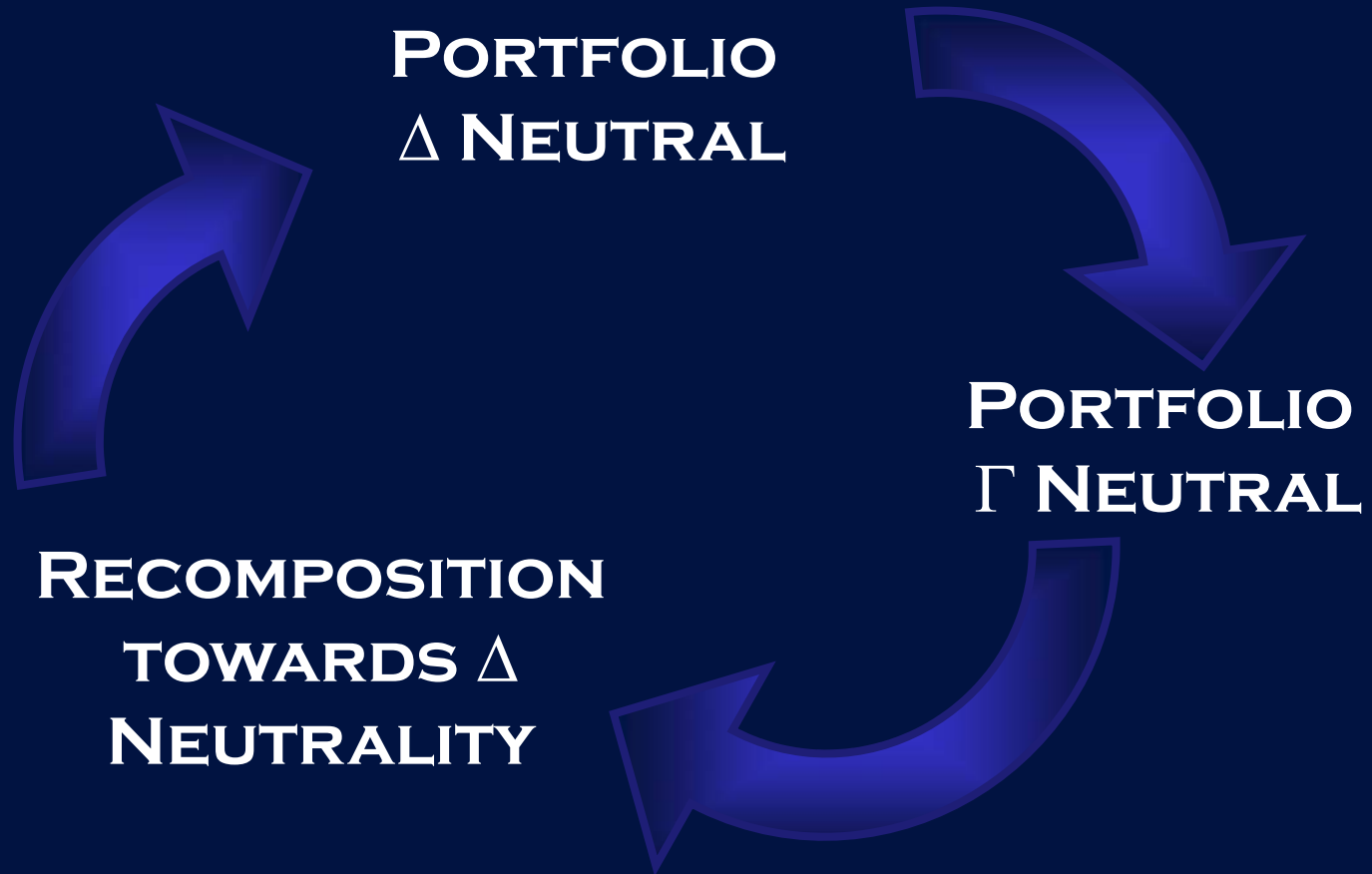


LET US BUILD OUR PORTFOLIO  
IN ORDER TO BE  $\Delta$  NEUTRAL



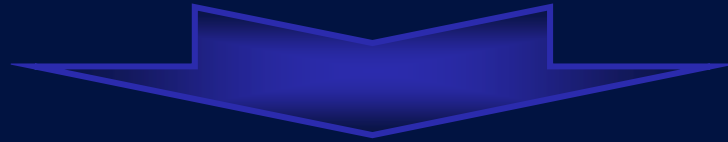
HOW CAN WE BUILD OUR PORTFOLIO  
IN ORDER TO BE ALSO  $\Gamma$  NEUTRAL

... LET US FOLLOW AN ITERATIVE LOGIC

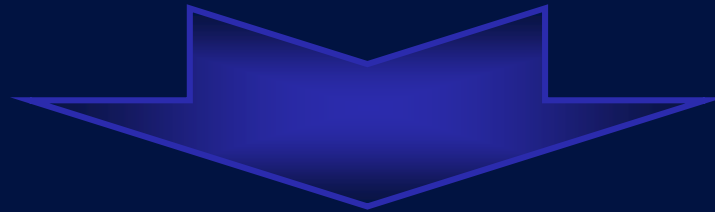


... THIS LOGIC IS CORRECT BECAUSE A  
STOCK'S  $\Gamma$  IS 0

... THIS LOGIC IS CORRECT BECAUSE A  
STOCK'S  $\Gamma$  IS 0



... IN ORDER TO LET OUR PORTFOLIO BE  
ALSO  $\Gamma$  NEUTRAL ...



... WE NEED ANOTHER OPTION

... WHAT KIND OF OPTION?



... AN OPTION THAT MATCHES THE  
SHORTED OPTION'S  $\Gamma$

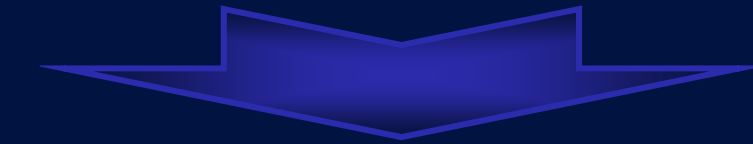
**... WHAT KIND OF OPTION?**



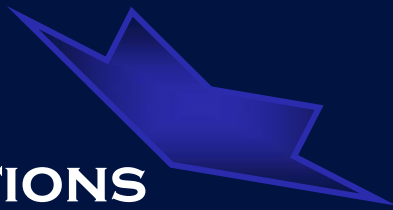
**... AN OPTION THAT MATCHES THE  
SHORTED OPTION'S  $\Gamma$**

**... AND THAT WOULD NOT CAUSE TOO  
MANY 'DEFORMATIONS' TO THE SHORTED  
OPTION'S DELTA**

... WHAT KIND OF OPTION?



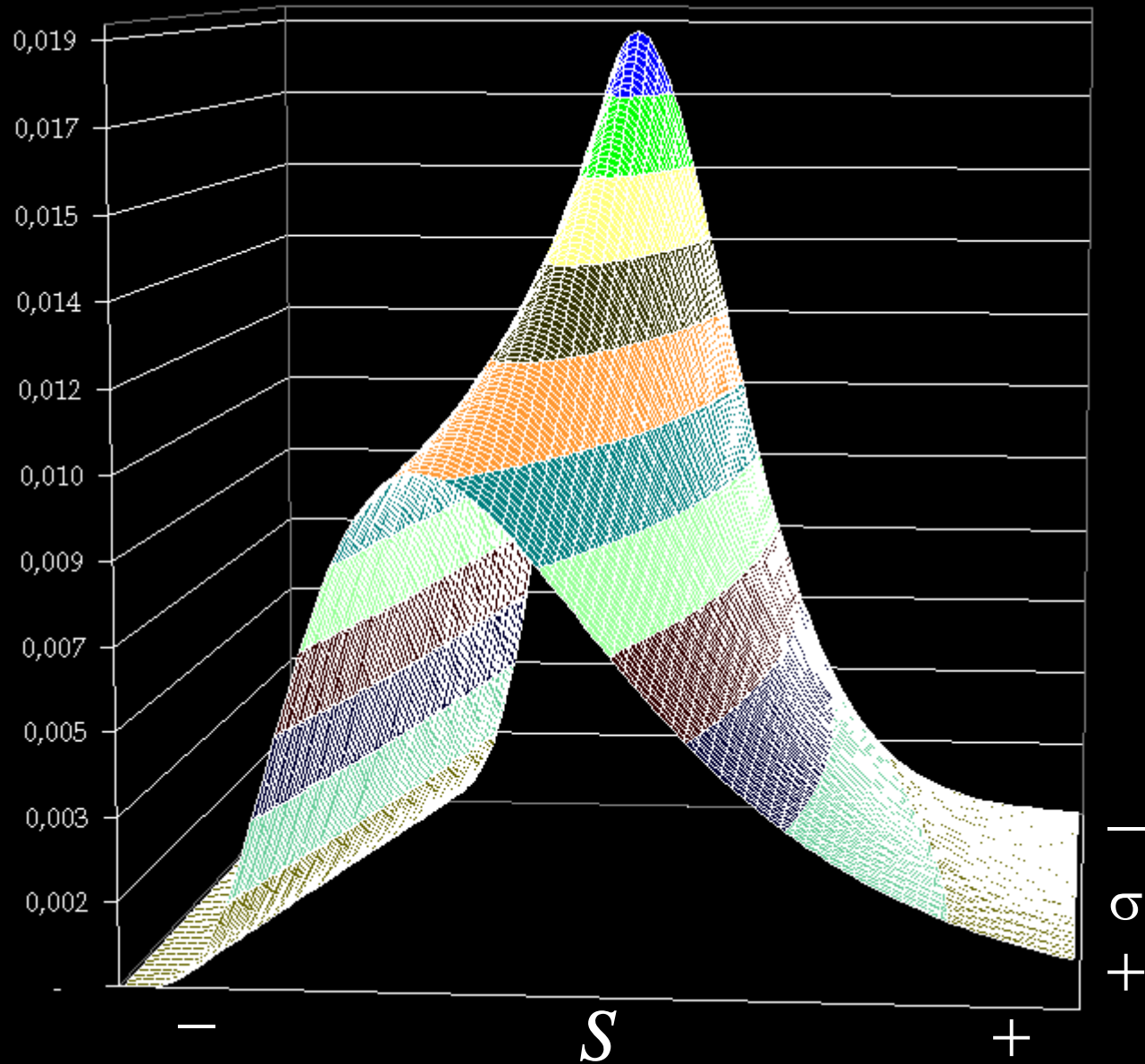
... SOME REMARKS



ATM OPTIONS  
HAVE THE  
BIGGEST  $\Gamma$



# INVESTOR EDUCATION



$\Gamma$

+



**... WHAT KIND OF OPTION?**



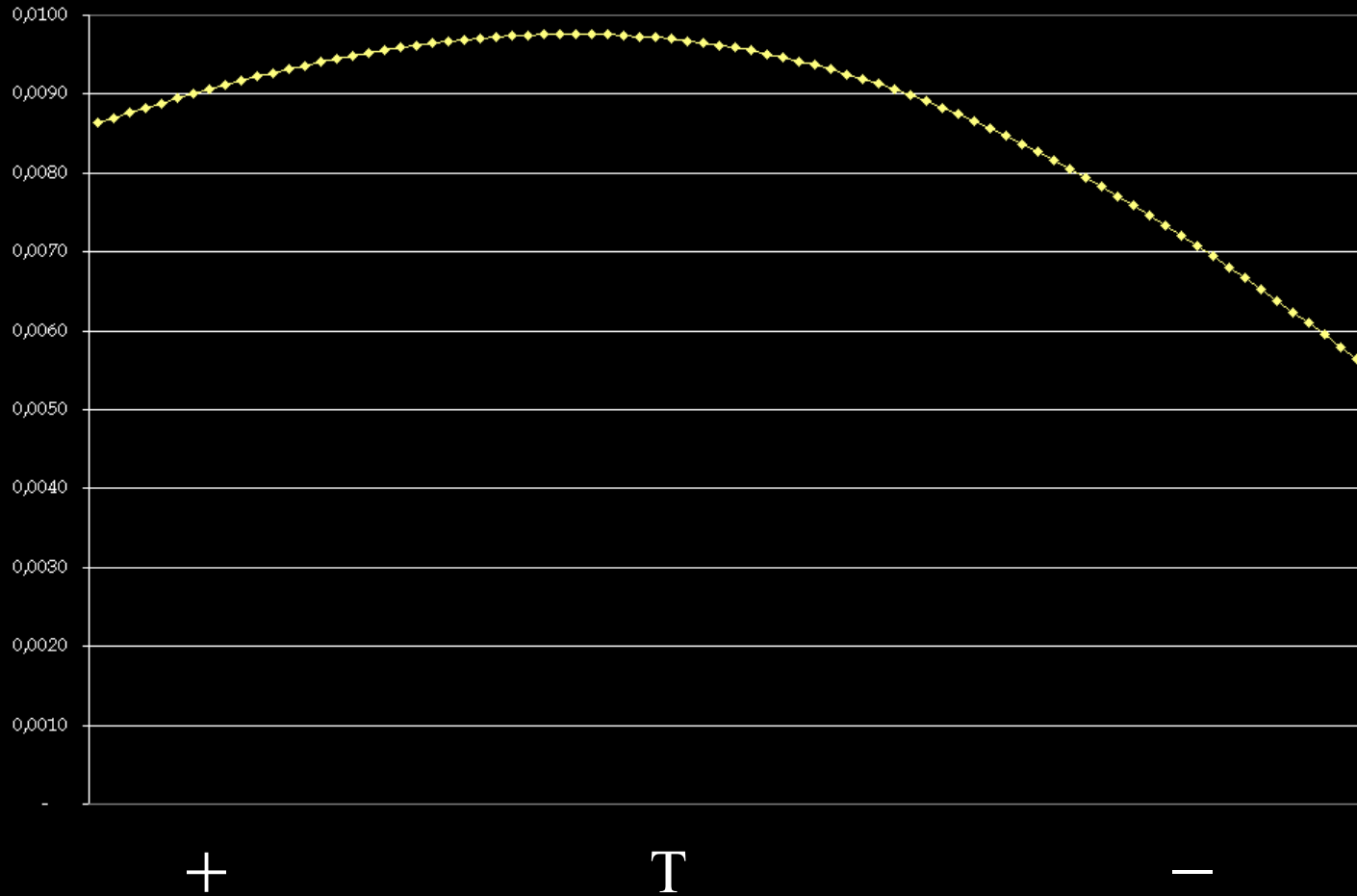
**... SOME REMARKS**



**$\Gamma$  OF AN OPTION  
FUNDAMENTALLY  
DECREASES AS TIME  
ELAPSES**

# INVESTOR EDUCATION

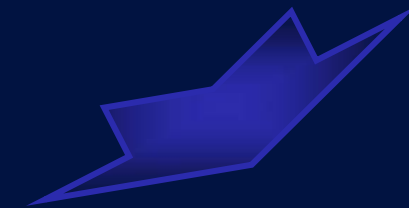
$\Gamma$



... WHAT KIND OF OPTION?

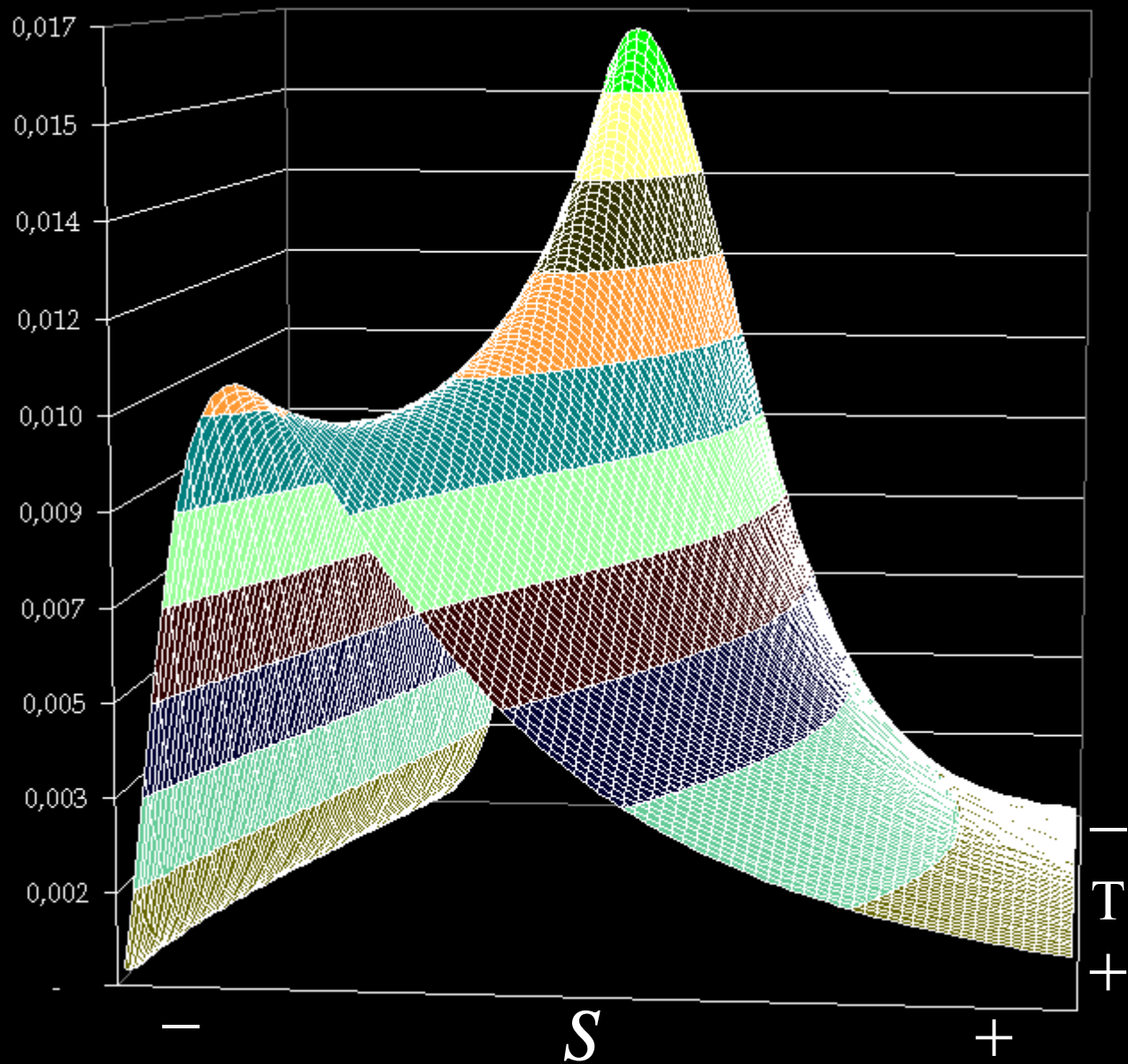


... SOME REMARKS



$\Gamma$  UNDERGOES SOME  
DEFORMATIONS  
RELATED TO  
MONEYNESS AS TIME  
VARIES

# INVESTOR EDUCATION



# $\Delta - \Gamma$ HEDGING

---

ATM OPTIONS  
HAVE THE  
BIGGEST  $\Gamma$

$\Gamma$  OF AN OPTION  
FUNDAMENTALLY  
DECREASES AS TIME  
ELAPSES

$\Gamma$  UNDERGOES SOME  
DEFORMATIONS  
RELATED TO  
MONEYNESS AS TIME  
VARIES



LET US SELECT SHORT TERM AND ATM OPTIONS

# $\Delta - \Gamma$ HEDGING

---

ATM OPTIONS  
HAVE THE  
BIGGEST  $\Gamma$

$\Gamma$  OF AN OPTION  
FUNDAMENTALLY  
DECREASES AS TIME  
ELAPSES

$\Gamma$  UNDERGOES SOME  
DEFORMATIONS  
RELATED TO  
MONEYNESS AS TIME  
VARIES



LET US SELECT SHORT TERM AND ATM OPTIONS



LET US DINAMICALLY RECOMPOSE THE  
PORTFOLIO WITH LONG TERM AND ATM  
OPTIONS

**LET US SELECT SHORT TERM AND ATM  
OPTIONS**

**TRADE-OFF:**

- **TRANSACTION COSTS**
- **TRADING STRATEGIES**
- **RISK LIMITS**

**LET US DINAMICALLY RECOMPOSE THE  
PORTFOLIO WITH LONG TERM AND ATM  
OPTIONS**



TIME  $T=0$

1 SHORT CALL (W)

LET US DEFINE A  $\Delta$  NEUTRAL PORTFOLIO 'A'

1 LONG OPTION (Z)

$$\Delta_A = 0$$

$$\Gamma_A = N * \Gamma_W$$

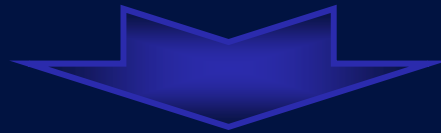
TIME  $T=0$

**PORTFOLIO B = PORTFOLIO A + N \* Z**

**... WHAT ABOUT THE  
GREEK LETTERS OF B?**

TIME  $T=0$

$$\Delta_B = \Delta_A + N \Delta_Z$$



$$\Delta_B = N \Delta_Z$$

TIME  $T=0$

$$\Gamma_B = \Gamma_A + N \Gamma_Z$$



$$\Gamma_B = N_W \Gamma_W + N_Z \Gamma_Z$$

... IN ORDER TO OBTAIN  $\Gamma_B = 0$

$$\Gamma_B = N_W \Gamma_W + N_Z \Gamma_Z$$



$$0 = N_W \Gamma_W + N_Z \Gamma_Z$$

... IN ORDER TO OBTAIN  $\Gamma_B = 0$

$$\Gamma_B = N_W \Gamma_W + N_Z \Gamma_Z$$

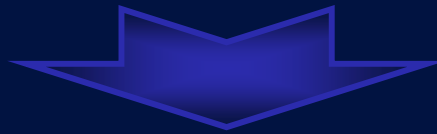


$$0 = N_W \Gamma_W + N_Z \Gamma_Z$$



$$N_Z = - \frac{N_W \Gamma_W}{\Gamma_Z}$$

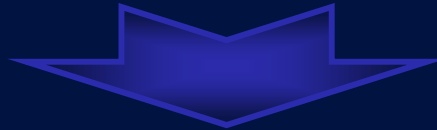
... THAT IS IN ORDER TO HAVE A  $\Gamma$   
NEUTRAL PORTFOLIO



YOU SHOULD BUY  
OPTIONS Z

$$N_Z = - \frac{\Gamma_w}{\Gamma_Z}$$

... BUT IT IS NOT THE WHOLE STORY

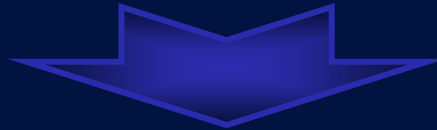


THE NEW PORTFOLIO B WILL NOT BE  $\Delta$  NEUTRAL

$$\Delta_B = N \Delta_Z$$

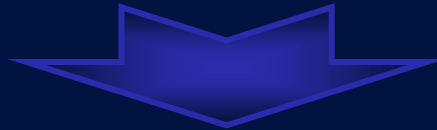


... BUT IT IS NOT THE WHOLE STORY



THE NEW PORTFOLIO B WILL NOT BE  $\Delta$  NEUTRAL

$$\Delta_B = N \Delta_Z$$



LET US REBALANCE THE PORTFOLIO IN ORDER  
TO OBTAIN THIS RESULT:

$$\Delta_c = 0$$

## KURPIEL & RONCALLI (1998)

$\Delta - \Gamma$  HEDGING REFERRED TO TIME HORIZONS  
OF 5, 1, 1/2 DAYS DOES NOT SUPPLY SUBSTANTIAL  
ADVANTAGES IN COMPARISON WITH  $\Delta$  HEDGING

TIME  $T=0$

SHORT 1 CALL (W)

LET US DEFINE A PORTFOLIO  $\Delta$  NEUTRAL 'A'

LONG 1 CALL (Z) WITH  $T_z > T_w$  ;  $K_z > K_w$

LET US HOLD THE OPTION 'Z' UNTIL  
MATURITY

AT MATURITY THE OPTION 'W' IS  
IN – THE MONEY

# $\Delta - \Gamma$ HEDGING - SHORT 1 CALL - IN - THE MONEY

Short 1000 call on 1 stock			Option and $\Delta$			Stock and $\Delta$				$\Delta$ Portfolio
Time Step	Time to Expiration	STOCK PRICE	Q. Opz.	$\Delta$ call	$\Delta$ call Posit.	Stock to Buy/(Sell)	Warehouse	$\Delta$ Stock	$\Delta$ Stock Posit.	Total $\Delta$ position
0	0,2500	100,0	(1.000)	0,564115961	(564)	564	564	1	564	-
1	0,2375	102,0	(1.000)	0,593648325	(594)	30	594	1	594	-
2	0,2250	101,9	(1.000)	0,591419714	(591)	(3)	591	1	591	-
3	0,2125	104,3	(1.000)	0,629740916	(630)	39	630	1	630	-
4	0,2000	105,9	(1.000)	0,655754583	(656)	26	656	1	656	-
5	0,1875	109,6	(1.000)	0,713190152	(713)	57	713	1	713	-
6	0,1750	109,2	(1.000)	0,710239361	(710)	(3)	710	1	710	-
7	0,1625	112,7	(1.000)	0,765213522	(765)	55	765	1	765	-
8	0,1500	112,1	(1.000)	0,762277787	(762)	(3)	762	1	762	-
9	0,1375	114,0	(1.000)	0,795097794	(795)	33	795	1	795	-
10	0,1250	116,0	(1.000)	0,828994045	(829)	34	829	1	829	-
11	0,1125	103,8	(1.000)	0,629405621	(629)	(200)	629	1	629	-
12	0,1000	97,7	(1.000)	0,482184607	(482)	(147)	482	1	482	-
13	0,0875	99,4	(1.000)	0,522140486	(522)	40	522	1	522	-
14	0,0750	92,6	(1.000)	0,317477734	(317)	(205)	317	1	317	-
15	0,0625	93,2	(1.000)	0,315146981	(315)	(2)	315	1	315	-
16	0,0500	98,6	(1.000)	0,47968815	(480)	165	480	1	480	-
17	0,0375	101,6	(1.000)	0,591235554	(591)	111	591	1	591	-
18	0,0250	104,7	(1.000)	0,737926695	(738)	147	738	1	738	-
19	0,0125	108,3	(1.000)	0,927247903	(927)	189	927	1	927	-
20	0,0000	120,1	(1.000)	1	(1.000)	73	1.000	1	1.000	-

# Δ – Γ HEDGING - SHORT 1 CALL - IN – THE MONEY

	Portfolio B = Portfolio A + II Option						
Γ Portfolio "A"	Γ Portfolio "B"						Δ Port. "B"
Γ portafolio = Γ I Option* n.a.z. Underlying	II Option			n. II Option Buy	Γ II Option Tot	Γ portafolio "B"	Total Δ position
	II Option value	d <sub>1</sub>	Γ II Option				
(15,70)	8,532035235	-0,021383	0,015528736	1.011	15,70263	-	496
(15,56)	9,252966775	0,047578	0,015593814	998	15,5621	-	517
(16,03)	8,927916787	0,036606	0,016022921	1.000	16,02778	-	514
(15,66)	9,931752237	0,128265	0,015959581	981	15,65784	-	539
(15,49)	10,53940858	0,189663	0,016016933	967	15,49118	-	555
(14,29)	12,45786614	0,339697	0,015333912	932	14,29063	-	589
(14,93)	11,86551334	0,322986	0,015990036	934	14,92771	-	584
(13,46)	13,85860752	0,477377	0,015071693	893	13,45713	-	609
(14,19)	13,09617795	0,457377	0,015878178	894	14,18792	-	603
(13,38)	14,05627045	0,55154	0,015501083	863	13,38009	-	611
(12,33)	15,14677459	0,657847	0,014924919	826	12,32786	-	614
(21,67)	6,98437869	0,050779	0,021689614	999	21,66644	-	519
(25,78)	3,874139145	-0,319605	0,023112366	1.115	25,7778	-	417
(27,07)	4,158819334	-0,242518	0,024624308	1.099	27,07001	-	444
(28,11)	1,658383337	-0,754865	0,021897225	1.284	28,10892	-	289
(30,49)	1,48799424	-0,780121	0,023041342	1.323	30,48717	-	288
(36,12)	2,582609126	-0,418841	0,029625236	1.219	36,11725	-	411
(39,46)	3,192341541	-0,217637	0,034269965	1.151	39,45535	-	476
(39,31)	3,991776369	0,037942	0,039296274	1.000	39,31016	-	515
(22,82)	5,305213614	0,438792	0,042324222	539	22,82201	-	361
-	15,20266822	2,445826	0,002983796	-	-	-	-

# $\Delta - \Gamma$ HEDGING - SHORT 1 CALL - IN - THE MONEY

Portfolio "C" = Port. "B" + Stock f( $\Delta$  hedge of "B")

$\Delta$ Port. "B"	Stock and $\Delta$ Portfolio				$\Delta$ Portfolio "C"
Total $\Delta$ position	Stock to Buy/(Sell)	Warehouse	$\Delta$ Stock	$\Delta$ Stock Posit.	Total $\Delta$ position
496	(496)	(496)	1	(496)	-
517	(21)	(517)	1	(517)	-
514	3	(514)	1	(514)	-
539	(25)	(539)	1	(539)	-
555	(16)	(555)	1	(555)	-
589	(34)	(589)	1	(589)	-
584	5	(584)	1	(584)	-
609	(25)	(609)	1	(609)	-
603	6	(603)	1	(603)	-
611	(8)	(611)	1	(611)	-
614	(3)	(614)	1	(614)	-
519	95	(519)	1	(519)	-
417	102	(417)	1	(417)	-
444	(27)	(444)	1	(444)	-
289	155	(289)	1	(289)	-
288	1	(288)	1	(288)	-
411	(123)	(411)	1	(411)	-
476	(65)	(476)	1	(476)	-
515	(39)	(515)	1	(515)	-
361	154	(361)	1	(361)	-
-	361	-	1	-	-

# $\Delta - \Gamma$ HEDGING - SHORT 1 CALL - IN - THE MONEY

quantitative composition of the "C" Portfolio, value of $\Delta$ & $\Gamma$						
Stock		Short Opt.	Option for $\Gamma$		Delta e Gamma	
Buy/sell	Warehouse	Short Opt.	Buy/sell	Warehouse	$\Delta$ portfolio C	$\Gamma$ portfolio C
68	68	(1.000)	1.011	1.011	-	-
9	77	(1.000)	(13)	998	-	-
-	77	(1.000)	2	1.000	-	-
14	91	(1.000)	(19)	981	-	-
10	101	(1.000)	(14)	967	-	-
23	124	(1.000)	(35)	932	-	-
2	126	(1.000)	2	934	-	-
30	156	(1.000)	(41)	893	-	-
3	159	(1.000)	1	894	-	-
25	184	(1.000)	(30)	863	-	-
31	215	(1.000)	(37)	826	-	-
(105)	110	(1.000)	173	999	-	-
(45)	65	(1.000)	116	1.115	-	-
13	78	(1.000)	(16)	1.099	-	-
(50)	28	(1.000)	184	1.284	-	-
(1)	27	(1.000)	39	1.323	-	-
42	69	(1.000)	(104)	1.219	-	-
46	115	(1.000)	(68)	1.151	-	-
108	223	(1.000)	(151)	1.000	-	-
343	566	(1.000)	(461)	539	-	-
434	1.000	(1.000)	(539)	-	-	-



# $\Delta - \Gamma$ HEDGING - SHORT 1 CALL - IN - THE MONEY

Delta Gamma Hedging Cash Flow						
Stock	Option	Opt. for $\Gamma$	Bank			Hedging Revenue (cost)
Dollars in Stock (Flow)	Cash ex Shorting/Exercising Option	Dollars in Option (Flow)	Cash	Interest (Flow)	Borrow (stock)	
6.800	10.378	8.628	5.050		5.050	
918		(122)	795	3,2	5.848	
-		21	21	3,7	5.873	
1.460		(191)	1.269	3,7	7.146	
1.059		(147)	912	4,5	8.063	
2.521		(439)	2.082	5,0	10.150	
218		19	237	6,3	10.394	
3.382		(564)	2.818	6,5	13.218	
336		9	345	8,3	13.572	
2.849		(427)	2.422	8,5	16.003	
3.595		(563)	3.032	10,0	19.044	
(10.897)		1.208	(9.689)	11,9	9.367	
(4.396)		451	(3.945)	5,9	5.427	
1.292		(67)	1.226	3,4	6.656	
(4.628)		306	(4.322)	4,2	2.338	
(93)		59	(34)	1,5	2.305	
4.142		(269)	3.873	1,4	6.180	
4.675		(217)	4.459	3,9	10.643	
11.312		(603)	10.709	6,7	21.358	
37.133		(2.446)	34.686	13,4	56.058	
52.139	(100.000)	(8.198)	43.941	35,0	100.034	

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LET US HOLD THE 'Z' OPTION UNTIL  
MATURITY

AT MATURITY THE OPTION 'W' IS  
OUT – THE MONEY

# Δ HEDGING - SHORT 1 CALL - OUT — THE MONEY

Short 1000 call on 1 stock			Option and Δ			Stock and Δ				Δ Portfolio
Time Step	Time to Expiration	STOCK PRICE	Q. Opz.	Δ call	Δ call Posit.	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position
0	0,2500	100,0	(1.000)	0,564115961	(564)	564	564	1	564	-
1	0,2375	106,1	(1.000)	0,654729124	(655)	91	655	1	655	-
2	0,2250	104,2	(1.000)	0,627365416	(627)	(28)	627	1	627	-
3	0,2125	104,9	(1.000)	0,639023423	(639)	12	639	1	639	-
4	0,2000	99,0	(1.000)	0,540155862	(540)	(99)	540	1	540	-
5	0,1875	97,9	(1.000)	0,517323489	(517)	(23)	517	1	517	-
6	0,1750	93,3	(1.000)	0,422696428	(423)	(94)	423	1	423	-
7	0,1625	87,2	(1.000)	0,292594163	(293)	(130)	293	1	293	-
8	0,1500	79,5	(1.000)	0,144979436	(145)	(148)	145	1	145	-
9	0,1375	79,7	(1.000)	0,135689732	(136)	(9)	136	1	136	-
10	0,1250	82,2	(1.000)	0,160714285	(161)	25	161	1	161	-
11	0,1125	87,2	(1.000)	0,239512401	(240)	79	240	1	240	-
12	0,1000	78,3	(1.000)	0,074592914	(75)	(165)	75	1	75	-
13	0,0875	73,1	(1.000)	0,021769947	(22)	(53)	22	1	22	-
14	0,0750	79,2	(1.000)	0,05288132	(53)	31	53	1	53	-
15	0,0625	79,0	(1.000)	0,035901243	(36)	(17)	36	1	36	-
16	0,0500	84,3	(1.000)	0,072705946	(73)	37	73	1	73	-
17	0,0375	84,3	(1.000)	0,044170375	(44)	(29)	44	1	44	-
18	0,0250	78,1	(1.000)	0,001029286	(1)	(43)	1	1	1	-
19	0,0125	74,7	(1.000)	1,09986E-07	-	(1)	-	1	-	-
20	0,0000	71,5	(1.000)	0	-	-	-	1	-	-

# Δ HEDGING - SHORT 1 CALL - OUT – THE MONEY

	Portfolio B = Portfolio A + II Option						
Γ Portfolio "A"	Γ Portfolio "B"						Δ Port. "B"
Γ portafolio =	II Option			n. II Option Buy	Γ II Option Tot	Γ portafolio "B"	Total Δ position
Γ I Option n.a.z. Underlying	II Option value	d <sub>1</sub>	Γ II Option:				
(15,70)	8,532035235	-0,021383	0,015528736	1.011	15,70263	-	496
(14,20)	11,50385049	0,20525	0,014695255	966	14,2025	-	560
(15,26)	10,14867469	0,128089	0,015552089	982	15,26498	-	540
(15,44)	10,26284595	0,152333	0,015815246	976	15,43546	-	546
(17,89)	6,976736039	-0,102274	0,017351704	1.031	17,88561	-	472
(18,76)	6,201205895	-0,164556	0,017939034	1.046	18,7625	-	454
(20,03)	4,133050684	-0,402387	0,018178071	1.102	20,02836	-	378
(19,53)	2,172498556	-0,748035	0,016498971	1.184	19,53189	-	269
(14,80)	0,749388353	-1,247614	0,011414948	1.296	14,79729	-	137
(14,73)	0,65845741	-1,293547	0,01117497	1.318	14,73167	-	129
(16,78)	0,796600892	-1,196629	0,01277235	1.314	16,78149	-	152
(21,23)	1,339000259	-0,935054	0,016697048	1.271	21,22699	-	222
(11,38)	0,262019159	-1,638052	0,007932318	1.435	11,38223	-	73
(4,81)	0,056296405	-2,183316	0,003179027	1.513	4,808971	-	22
(9,95)	0,15339148	-1,813143	0,006580083	1.512	9,948043	-	53
(7,99)	0,091417259	-1,984494	0,005141739	1.553	7,985569	-	37
(14,67)	0,195110623	-1,67581	0,009293286	1.578	14,66809	-	74
(11,44)	0,101824554	-1,893685	0,007045	1.624	11,44363	-	47
(0,56)	0,002827193	-2,998713	0,000588448	952	0,560244	-	1
(0,00)	1,29371E-05	-4,25525	7,90033E-06	18	0,000141	-	-
-	0	-6,843081	6,77257E-12	-	-	-	-

# Δ HEDGING - SHORT 1 CALL - OUT – THE MONEY

Portfolio "C" = Port. "B" + Stock f(Δ hedge of "B")					
Δ Port. "B"	Stock and Δ Portfolio				Δ Portfolio "C"
Total Δ position	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position
496	(496)	(496)	1	(496)	-
560	(64)	(560)	1	(560)	-
540	20	(540)	1	(540)	-
546	(6)	(546)	1	(546)	-
472	74	(472)	1	(472)	-
454	18	(454)	1	(454)	-
378	76	(378)	1	(378)	-
269	109	(269)	1	(269)	-
137	132	(137)	1	(137)	-
129	8	(129)	1	(129)	-
152	(23)	(152)	1	(152)	-
222	(70)	(222)	1	(222)	-
73	149	(73)	1	(73)	-
22	51	(22)	1	(22)	-
53	(31)	(53)	1	(53)	-
37	16	(37)	1	(37)	-
74	(37)	(74)	1	(74)	-
47	27	(47)	1	(47)	-
1	46	(1)	1	(1)	-
-	1	-	1	-	-
-	-	-	1	-	-

# Δ HEDGING - SHORT 1 CALL - OUT – THE MONEY

quantitative composition of the “C” Portfolio, value of Δ & Γ						
Stock		Short Opt.	Option for Γ		Delta e Gamma	
Buy/sell	Warehouse	Short Opt.	Buy/sell	Warehouse	Δ portfolio C	Γ portfolio C
68	68	(1.000)	1.011	1.011	-	-
27	95	(1.000)	(45)	966	-	-
(8)	87	(1.000)	15	982	-	-
6	93	(1.000)	(6)	976	-	-
(25)	68	(1.000)	55	1.031	-	-
(5)	63	(1.000)	15	1.046	-	-
(18)	45	(1.000)	56	1.102	-	-
(21)	24	(1.000)	82	1.184	-	-
(16)	8	(1.000)	112	1.296	-	-
(1)	7	(1.000)	22	1.318	-	-
2	9	(1.000)	(4)	1.314	-	-
9	18	(1.000)	(43)	1.271	-	-
(16)	2	(1.000)	164	1.435	-	-
(2)	-	(1.000)	78	1.513	-	-
-	-	(1.000)	(1)	1.512	-	-
(1)	(1)	(1.000)	41	1.553	-	-
-	(1)	(1.000)	25	1.578	-	-
(2)	(3)	(1.000)	46	1.624	-	-
3	-	(1.000)	(672)	952	-	-
-	-	(1.000)	(934)	18	-	-
-	-	(1.000)	(18)	-	-	-

# Δ HEDGING - SHORT 1 CALL - OUT — THE MONEY

Delta Gamma Hedging Cash Flow						
Stock	Option	Opt. for $\Gamma$	Bank			Hedging Revenue (cost)
Dollars in Stock (Flow)	Cash ex Shorting/Exercise Option	Dollars in Option (Flow)	Cash	Interest (Flow)	Borrow (stock)	
6.800	10.378	8.628	5.050		5.050	
2.864		(515)	2.349	3,2	7.402	
(833)		153	(680)	4,6	6.727	
629		(57)	572	4,2	7.303	
(2.476)		382	(2.093)	4,6	5.214	
(490)		94	(396)	3,3	4.822	
(1.680)		231	(1.449)	3,0	3.376	
(1.832)		178	(1.654)	2,1	1.725	
(1.272)		84	(1.188)	1,1	538	
(80)		14	(65)	0,3	473	
164		(3)	161	0,3	634	
785		(57)	728	0,4	1.363	
(1.253)		43	(1.210)	0,9	153	
(146)		4	(142)	0,1	11	
-		(0)	(0)	0,0	11	
(79)		4	(75)	0,0	(64)	
-		5	5	(0,0)	(59)	
(169)		5	(164)	(0,0)	(223)	
234		(2)	232	(0,1)	9	
-		(0)	(0)	0,0	9	
-	-	-	-	0,0	9	(9)

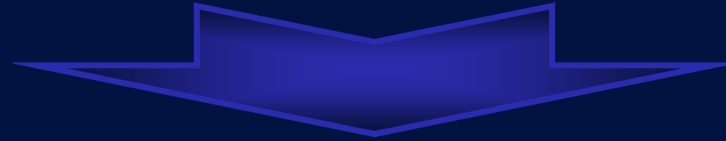
$\Delta - \Gamma - \Theta$  HEDGING

COMPUTATION OF  $df$  BY MEANS OF A SECOND ORDER TAYLOR'S FORMULA, PAYING ATTENTION TO VOLATILITY

$$df \approx \Delta dS + \frac{1}{2} \Gamma dS^2 + \frac{\partial f}{\partial \sigma} d\sigma + o(dt)$$

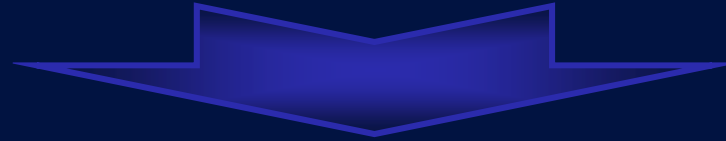


AT TIME  $T=0$  SHORT 1 CALL



LET US BUILD OUR PORTFOLIO  
IN ORDER TO BE  $\Delta$  NEUTRAL

AT TIME  $T=0$  SHORT 1 CALL

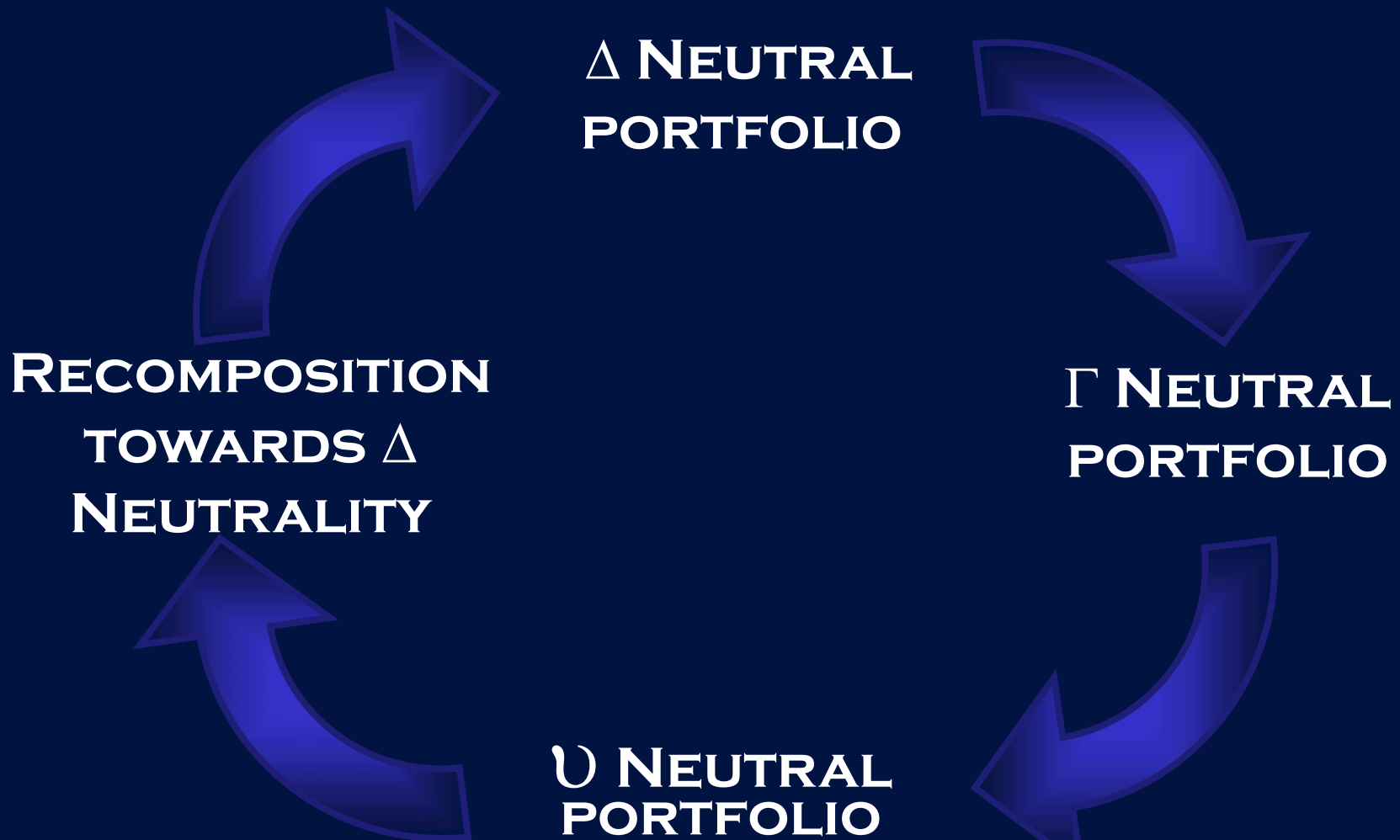


LET US BUILD OUR PORTFOLIO  
IN ORDER TO BE  $\Delta$  NEUTRAL



HOW CAN WE BUILD OUR PORTFOLIO IN  
ORDER TO BE ALSO  $\Gamma - \psi$  NEUTRAL

... LET US FOLLOW AN ITERATIVE LOGIC



... THIS LOGIC **IS NOT** CORRECT



... IF  $\Gamma - \Theta$  OF A STOCK IS 0

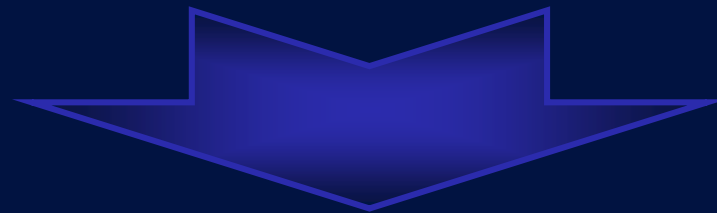
... UNFORTUNATELY THE  
OPTION'S  $\Gamma$  **IS NOT** 0

... THIS LOGIC **IS NOT** CORRECT



... IF  $\Gamma - \Theta$  OF A STOCK IS 0

... UNFORTUNATELY THE  
OPTION'S  $\Gamma$  **IS NOT** 0



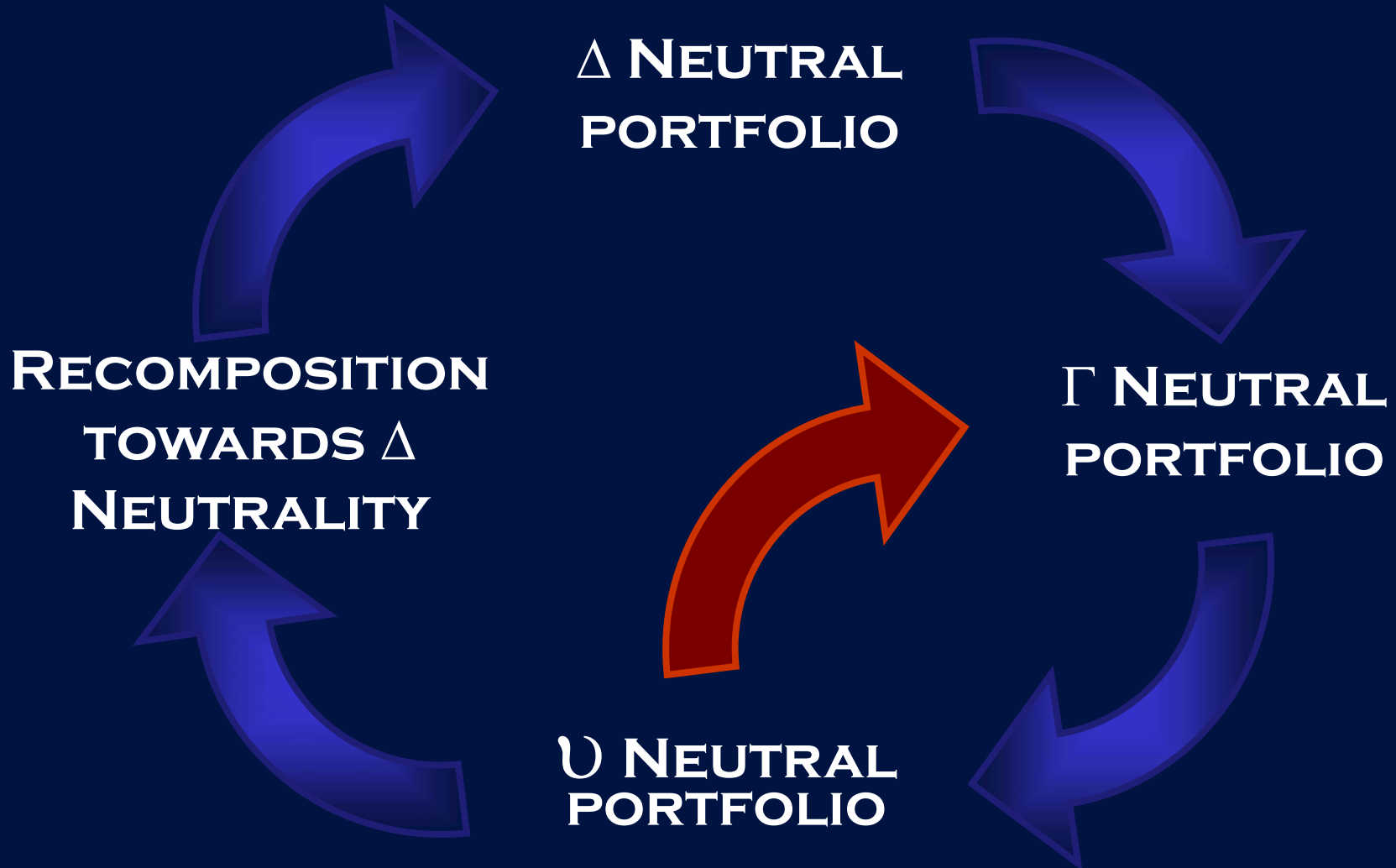
... WE NEED ANOTHER OPTION

... THEN WE WANT TO OBTAIN A JOINTLY  
 $\Gamma - \Theta$  NEUTRAL PORTFOLIO

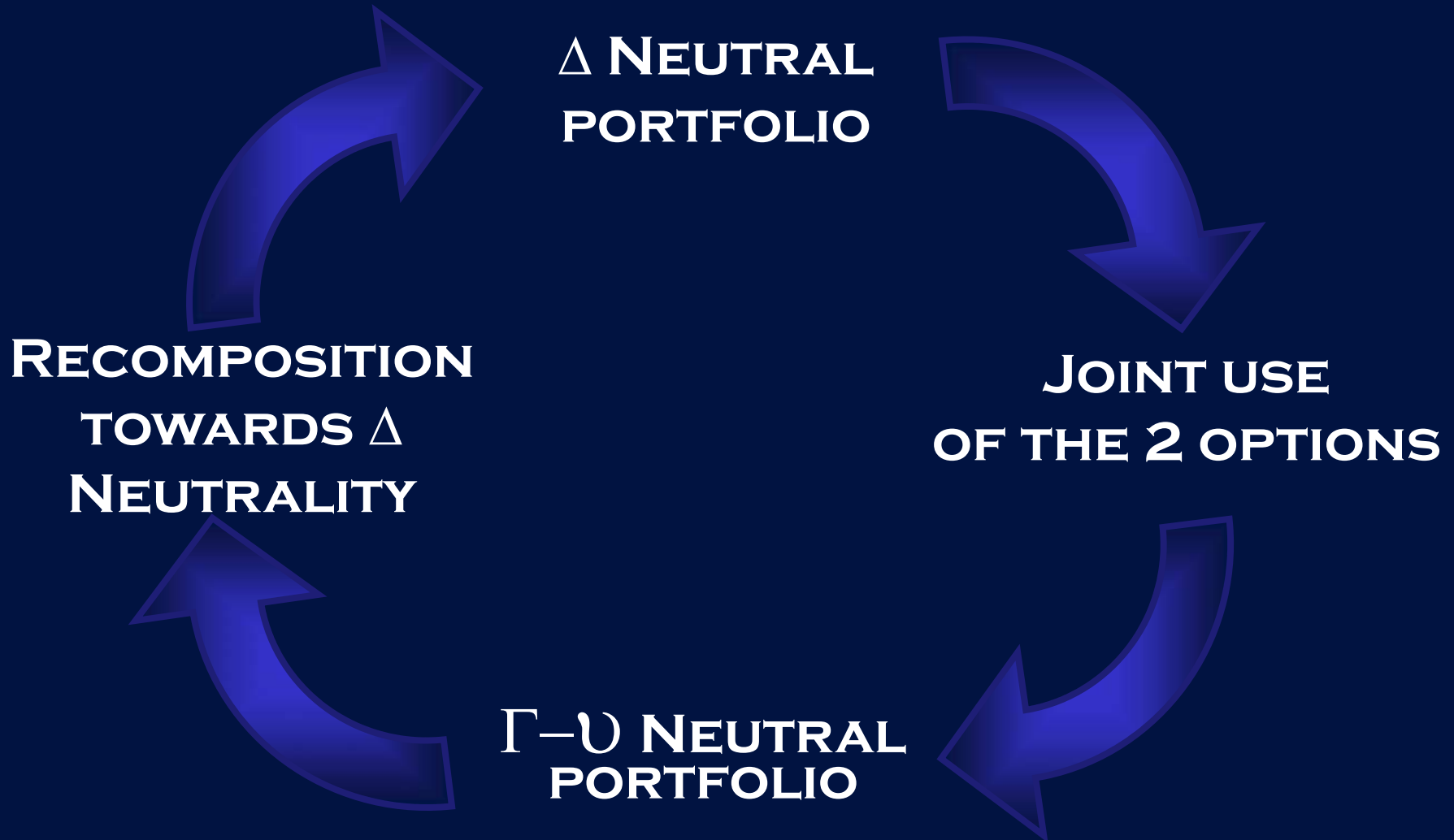


... OTHERWISE WE START A LOOP  
WITHOUT SOLUTION

... IT FOLLOWS THE 'VICIOUS' LOOP



... IT FOLLOWS THE 'VIRTUOUS' LOOP



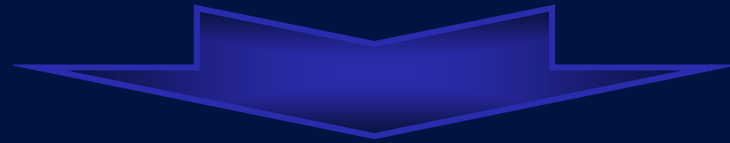


... WHAT KIND OF OPTIONS?



... AN OPTION THAT MATCHES THE  $\Gamma - \Theta$   
'SHORTED' OPTION

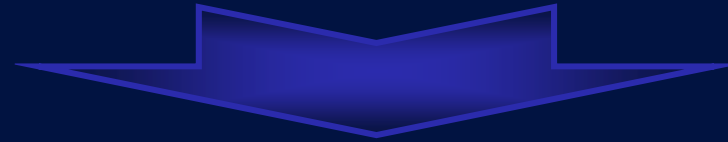
**... WHAT KIND OF OPTIONS?**



**... AN OPTION THAT MATCHES THE  $\Gamma - \Theta$   
'SHORTED' OPTION**

**... AND THAT DOES NOT CAUSE TOO  
MANY 'DEFORMATIONS' TO THE DELTA  
OF THE 'SHORTED' OPTION**

... WHAT KIND OF OPTIONS?

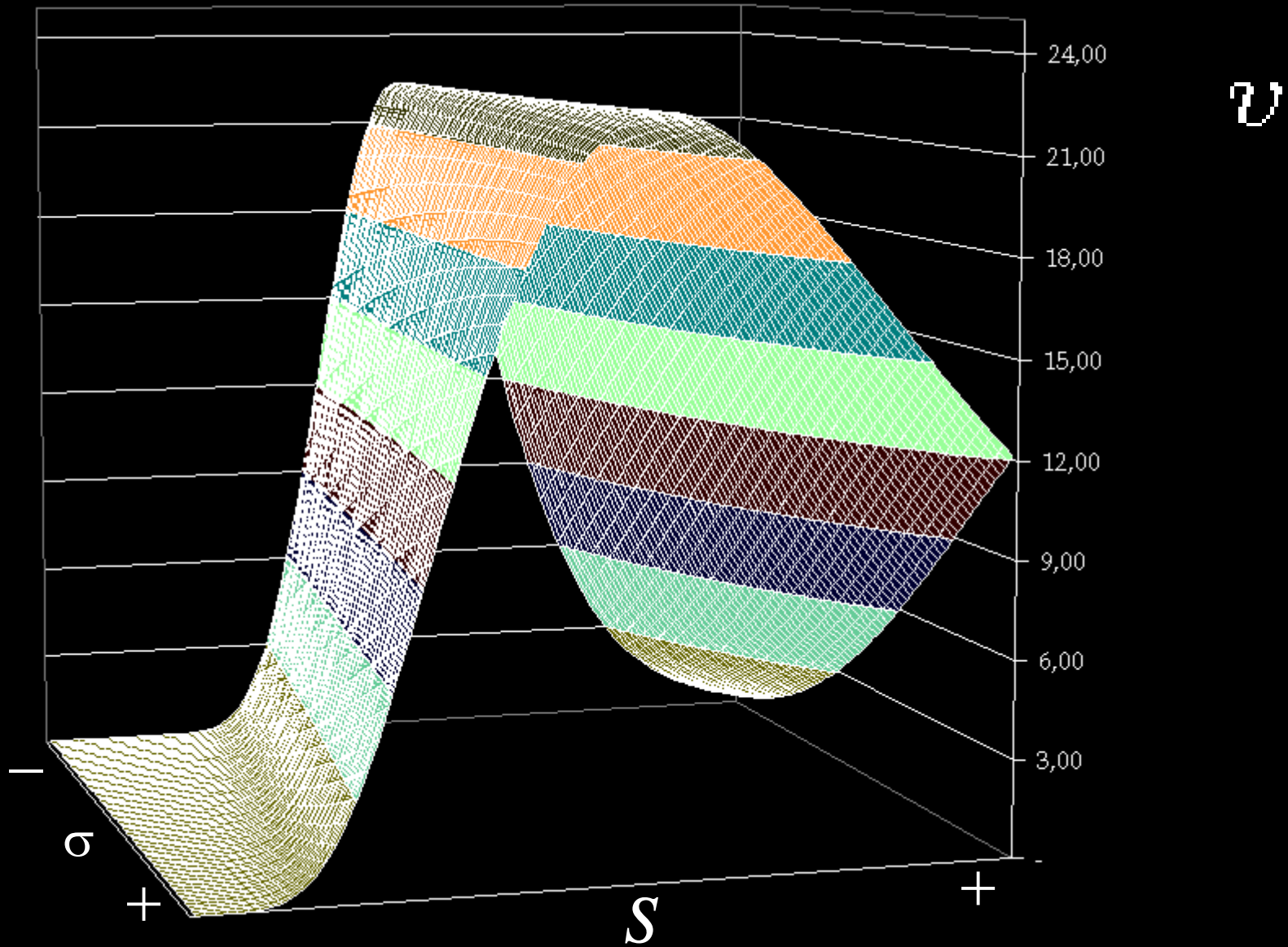


... SOME REMARKS



ATM OPTIONS  
HAVE THE  
BIGGEST  $\cup$

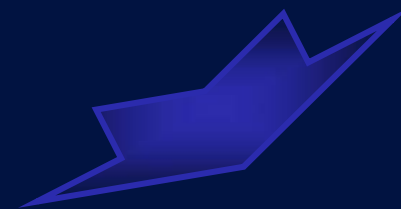
# $\Delta - \Gamma - \Theta$ HEDGING



... WHAT KIND OF OPTION?

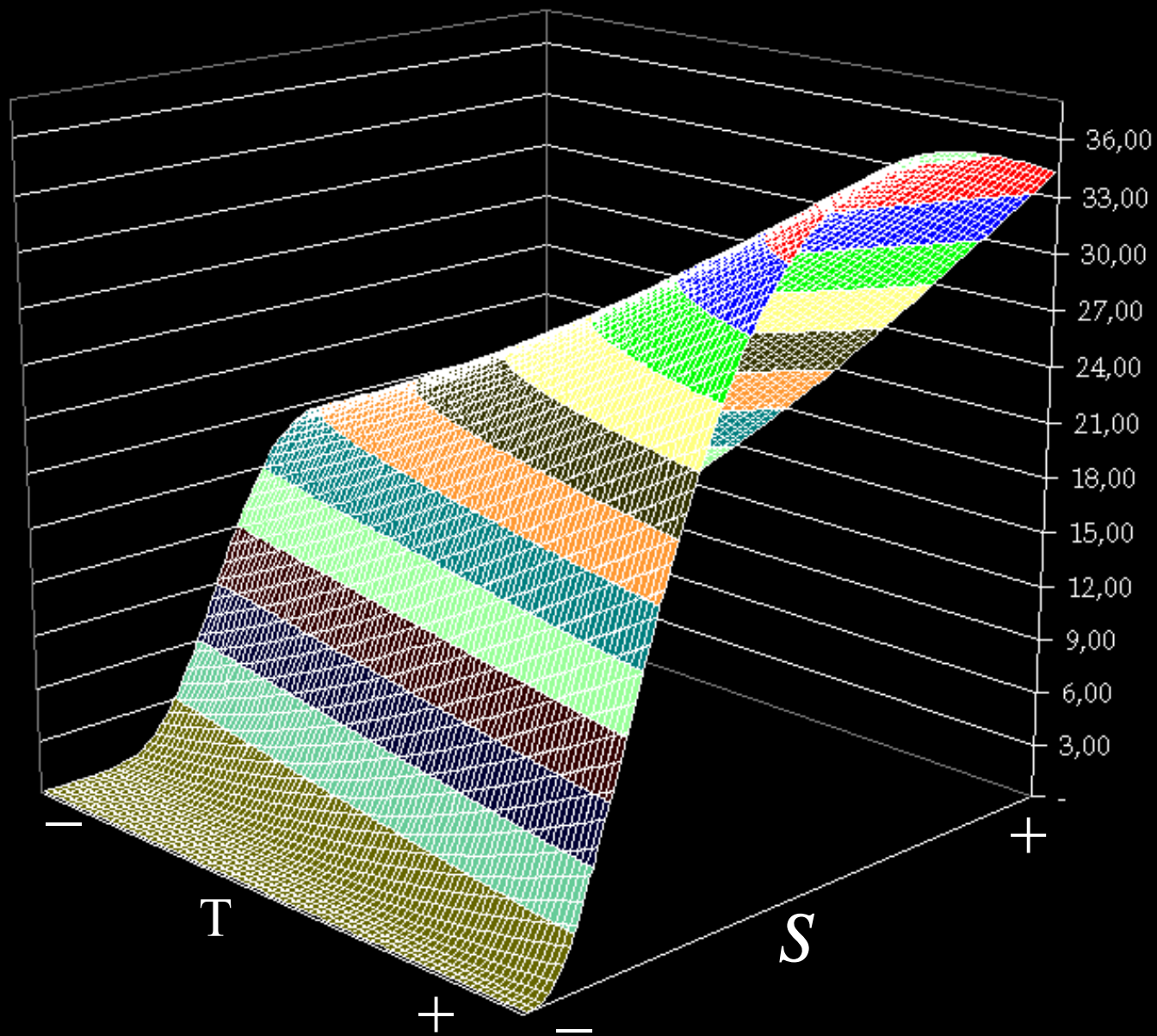


... SOME REMARKS



$\Theta$  OF AN OPTION  
FUNDAMENTALLY  
DECREASES AS TIME  
ELAPSES

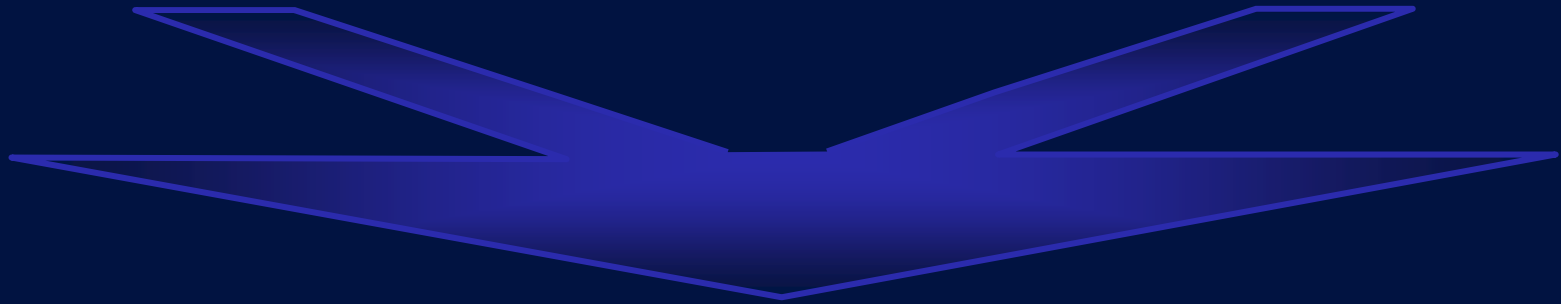
# $\Delta - \Gamma - \Theta$ HEDGING



$\Theta$

ATM OPTIONS HAVE  
THE BIGGEST  $\Theta$

$\Theta$  OF AN OPTION  
FUNDAMENTALLY  
DECREASES AS TIME  
ELAPSES



LET US DINAMICALLY RECOMPOSE THE  
PORTFOLIO WITH LONG TERM AND ATM  
OPTIONS

**LET US DINAMICALLY RECOMPOSE THE  
PORTFOLIO WITH LONG TERM AND ATM  
OPTIONS**

LET US  
CONSIDER

- **TRANSACTION COSTS**
- **TRADING STRATEGIES**
- **RISK LIMITS**
- **.....**



TIME  $T=0$

SHORT 1 CALL (W)

LET US DEFINE A  $\Delta$  NEUTRAL PORTFOLIO 'A'

LONG 1 OPTION (Z)

LONG 1 OPTION (Y)

$$\Delta_A = 0$$

$$\Gamma_A = N * \Gamma_W$$

TIME  $T=0$

PORTFOLIO B = PORT. A +  $N^*$  Z +  $N^*$  Y

... GREEK LETTERS OF B?

TIME T=0

$$\Delta_B = \Delta_A + N_Z \Delta_Z + N_Y \Delta_Y$$



$$\Delta_B = N_Z \Delta_Z + N_Y \Delta_Y$$

TIME  $T=0$

$$\Gamma_B = n_w \Gamma_w + n_z \Gamma_z + n_y \Gamma_y$$

GIVEN THAT:

$$\Gamma_A = N_w \Gamma_w$$

TIME  $T=0$

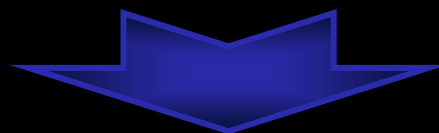
$$V_B = n_w V_w + n_z V_z + n_y V_B$$

GIVEN THAT:

$$U_A = N_w U_w$$

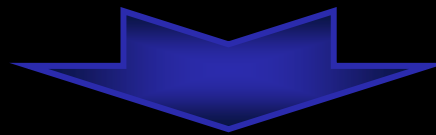
... IN ORDER TO OBTAIN  $\Gamma_B = \mathcal{V}_B = 0$

... THAT IS A  $\Gamma - \mathcal{V}$  NEUTRAL PORTFOLIO



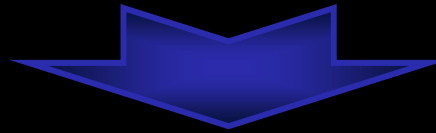
$$\left\{ \begin{array}{l} 0 = n_w \Gamma_w + n_z \Gamma_z + n_y \Gamma_y \\ 0 = n_w \mathcal{V}_w + n_z \mathcal{V}_z + n_y \mathcal{V}_y \end{array} \right.$$

$$\begin{cases} 0 = n_w \Gamma_w + n_z \Gamma_z + n_y \Gamma_y \\ 0 = n_w \nu_w + n_z \nu_z + n_y \nu_y \end{cases}$$



$$\begin{cases} n_z = \frac{-n_w \Gamma_w - n_y \Gamma_y}{\Gamma_z} \end{cases}$$

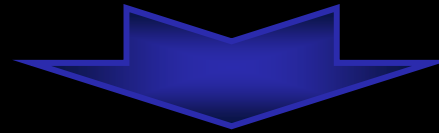
$$\left\{ \begin{array}{l} n_z = \frac{-n_w \Gamma_w - n_y \Gamma_y}{\Gamma_z} \end{array} \right.$$



$$\left\{ \begin{array}{l} 0 = n_w v_w + \frac{-n_w \Gamma_w - n_y \Gamma_y}{\Gamma_z} v_z + n_y v_y \end{array} \right.$$

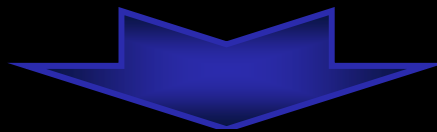


$$\left\{ \begin{array}{l} 0 = n_w v_w + \frac{-n_w \Gamma_w - n_y \Gamma_y}{\Gamma_z} v_z + n_y v_y \end{array} \right.$$



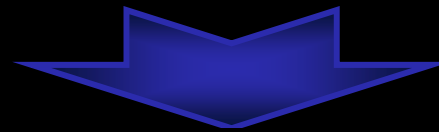
$$\left\{ \begin{array}{l} 0 = n_w v_w \Gamma_z - n_w \Gamma_w v_z - n_y \Gamma_y v_z + n_y v_y \Gamma_z \end{array} \right.$$

$$\left\{ \begin{array}{l} 0 = n_w v_w \Gamma_z - n_w \Gamma_w v_z - n_y \Gamma_y v_z + n_y v_y \Gamma_z \\ \hline \end{array} \right.$$



$$\left\{ \begin{array}{l} -n_w v_w \Gamma_z + n_w \Gamma_w v_z = n_y (v_y \Gamma_z - \Gamma_y v_z) \\ \hline \end{array} \right.$$

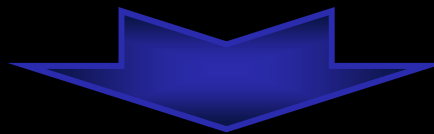
$$\left\{ \begin{array}{l} -n_w v_w \Gamma_z + n_w \Gamma_w v_z = n_y (v_y \Gamma_z - \Gamma_y v_z) \end{array} \right.$$



$$\left\{ \begin{array}{l} n_y = \frac{-n_w v_w \Gamma_z + n_w \Gamma_w v_z}{(v_y \Gamma_z - \Gamma_y v_z)} \end{array} \right.$$

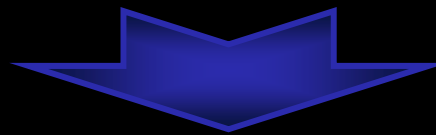
# $\Delta - \Gamma - \nu$ HEDGING TROUGH FORMULAS

$$\left\{ \begin{array}{l} n_y = \frac{-n_w \nu_w \Gamma_z + n_w \Gamma_w \nu_z}{(\nu_y \Gamma_z - \Gamma_y \nu_z)} \\ n_z = \frac{-n_w \Gamma_w - n_y \Gamma_y}{\Gamma_z} \end{array} \right.$$



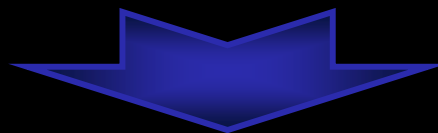
$$\left\{ \begin{array}{l} n_z = \frac{-n_w \Gamma_w - \left( \frac{-n_w \nu_w \Gamma_z + n_w \Gamma_w \nu_z}{(\nu_y \Gamma_z - \Gamma_y \nu_z)} \right) \Gamma_y}{\Gamma_z} \end{array} \right.$$

$$\left\{ \begin{array}{l} \nu_z = \frac{-n_w \Gamma_w - \left( \frac{-n_w \nu_w \Gamma_z + n_w \Gamma_w \nu_z}{(\nu_y \Gamma_z - \Gamma_y \nu_z)} \right) \Gamma_y}{\Gamma_z} \end{array} \right.$$



$$\left\{ \begin{array}{l} \nu_z = -\frac{n_w \Gamma_w}{\Gamma_z} - \left( \frac{-n_w \nu_w \Gamma_z + n_w \Gamma_w \nu_z}{(\nu_y \Gamma_z - \Gamma_y \nu_z)} \right) \frac{\Gamma_y}{\Gamma_z} \end{array} \right.$$

... IN ORDER TO OBTAIN  $\Gamma_B = \nu_B = 0$

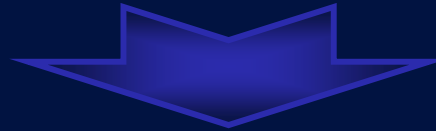


IT IS NECESSARY TO NEGOTIATE

$$n_z = -\frac{n_w \Gamma_w}{\Gamma_z} - \left( \frac{-n_w \nu_w \Gamma_z + n_w \Gamma_w \nu_z}{(\nu_y \Gamma_z - \Gamma_y \nu_z)} \right) \frac{\Gamma_y}{\Gamma_z} \quad \text{Z OPTIONS}$$

$$n_y = \frac{-n_w \nu_w \Gamma_z + n_w \Gamma_w \nu_z}{(\nu_y \Gamma_z - \Gamma_y \nu_z)} \quad \text{Y OPTIONS}$$

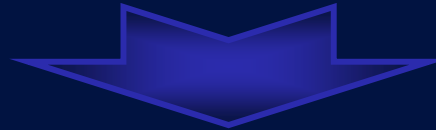
... BUT IT IS NOT THE WHOLE STORY



THE NEW PORTFOLIO B WILL NOT BE  $\Delta$  NEUTRAL

$$\Delta_B = N_Z \Delta_Z + N_Y \Delta_Y$$

... BUT IT IS NOT THE WHOLE STORY



THE NEW PORTFOLIO B WILL NOT BE  $\Delta$  NEUTRAL

$$\Delta_B = N_Z \Delta_Z + N_Y \Delta_Y$$



LET US REBALANCE THE PORTFOLIO IN ORDER TO  
OBTAIN THE FOLLOWING RESULT:

$$\Delta_C = 0$$



## KURPIEL & RONCALLI (1998)

$\Delta - \Gamma - \psi$  HEDGING REFERRED TO TIME HORIZONS OF  
5, 1, 1/2 DAYS SUPPLIES SUBSTANTIAL ADVANTAGES  
IN PARTICULAR UNDER STOCHASTIC VOLATILITY

**LET US HOLD THE OPTION 'Z' UNTIL  
MATURITY**

**AT MATURITY THE OPTION 'W' IS  
OUT – THE MONEY**

# Δ - Γ - υ HEDGING

Short 1000 call on 1 stock			Option and Δ			Stock and Δ				Δ Portfolio	Γ Portfolio "A"	υ Portfolio "A"
Time Step	Time to Expiration	STOCK PRICE	Q. Opz.	Δ call	Δ call Posit.	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position	Γ portfolio = Γ I Option*n.az. Underlying	υ portfolio = υ I Option*n.az. Underlying
0	0,2500	100,0	(1.000)	0,564	(564)	564	564	1	564	-	(15,70)	(19.628)
1	0,2375	99,6	(1.000)	0,557	(557)	(7)	557	1	557	-	(16,22)	(19.120)
2	0,2250	101,0	(1.000)	0,577	(577)	20	577	1	577	-	(16,30)	(18.697)
3	0,2125	107,8	(1.000)	0,683	(683)	106	683	1	683	-	(14,28)	(17.643)
4	0,2000	109,0	(1.000)	0,701	(701)	18	701	1	701	-	(14,19)	(16.847)
5	0,1875	109,1	(1.000)	0,706	(706)	5	706	1	706	-	(14,52)	(16.208)
6	0,1750	108,7	(1.000)	0,703	(703)	(3)	703	1	703	-	(15,17)	(15.681)
7	0,1625	103,6	(1.000)	0,621	(621)	(82)	621	1	621	-	(18,17)	(15.857)
8	0,1500	93,6	(1.000)	0,414	(414)	(207)	414	1	414	-	(21,48)	(14.107)
9	0,1375	91,9	(1.000)	0,370	(370)	(44)	370	1	370	-	(22,12)	(12.855)
10	0,1250	86,2	(1.000)	0,234	(234)	(136)	234	1	234	-	(20,12)	(9.342)
11	0,1125	87,6	(1.000)	0,249	(249)	15	249	1	249	-	(21,56)	(9.307)
12	0,1000	87,9	(1.000)	0,239	(239)	(10)	239	1	239	-	(22,28)	(8.610)
13	0,0875	83,6	(1.000)	0,133	(133)	(106)	133	1	133	-	(17,40)	(5.325)
14	0,0750	92,0	(1.000)	0,303	(303)	170	303	1	303	-	(27,69)	(8.797)
15	0,0625	95,0	(1.000)	0,370	(370)	67	370	1	370	-	(31,80)	(8.962)
16	0,0500	91,5	(1.000)	0,235	(235)	(135)	235	1	235	-	(30,01)	(6.277)
17	0,0375	88,6	(1.000)	0,117	(117)	(118)	117	1	117	-	(22,96)	(3.378)
18	0,0250	91,5	(1.000)	0,142	(142)	25	142	1	142	-	(31,01)	(3.245)
19	0,0125	90,8	(1.000)	0,045	(45)	(97)	45	1	45	-	(18,83)	(970)
20	0,0000	87,5	(1.000)	0,000	-	(45)	-	1	-	-	-	-

# Δ – Γ – υ HEDGING

portfolio B = portfolio A + II option + III option

Γ-υ Portfolio "B"

Δ Port. "B"

II Option			III Option											
II Option value	Γ II option	υ II option	III Option value	Γ III option	υ III option	n. II option Buy/sell	n. III option buy/sell	Γ II option Tot	Γ III option Tot	υ II option Tot	υ III option Tot	Γ portfolio "B"	υ portfolio "B"	Total Δ position
8,5320	0,0155	20,3815	10,8995	0,0149	20,5532	2.022	(1.051)	31	(16)	41.219	(21.591)	-	-	396
8,0880	0,0160	19,8035	10,4330	0,0154	20,0694	2.033	(1.053)	32	(16)	40.253	(21.133)	-	-	388
8,4726	0,0162	19,5841	10,9321	0,0154	19,6781	2.015	(1.056)	33	(16)	39.471	(20.774)	-	-	394
11,9678	0,0150	19,6378	14,9784	0,0136	18,7267	1.903	(1.053)	29	(14)	37.361	(19.718)	-	-	435
12,3611	0,0151	19,0413	15,4827	0,0135	17,9868	1.880	(1.054)	28	(14)	35.800	(18.953)	-	-	435
12,1542	0,0155	18,4611	15,3176	0,0137	17,3926	1.873	(1.056)	29	(15)	34.577	(18.369)	-	-	429
11,5627	0,0162	17,9031	14,7232	0,0143	16,9039	1.877	(1.060)	30	(15)	33.603	(17.922)	-	-	420
8,3385	0,0183	17,2177	11,0967	0,0169	17,0414	1.984	(1.074)	36	(18)	34.153	(18.296)	-	-	385
3,6873	0,0192	13,6472	5,4801	0,0200	15,3406	2.240	(1.073)	43	(21)	30.564	(16.458)	-	-	280
2,9088	0,0191	12,1340	4,5198	0,0206	14,1752	2.311	(1.072)	44	(22)	28.047	(15.192)	-	-	250
1,3645	0,0160	8,1671	2,3963	0,0195	10,8369	2.516	(1.034)	40	(20)	20.552	(11.210)	-	-	165
1,4154	0,0170	8,1778	2,5330	0,0206	10,8703	2.529	(1.046)	43	(22)	20.683	(11.376)	-	-	170
1,2554	0,0172	7,4960	2,3531	0,0213	10,2705	2.584	(1.048)	45	(22)	19.373	(10.763)	-	-	160
0,5252	0,0124	4,3301	1,1807	0,0180	7,0894	2.811	(966)	35	(17)	12.172	(6.847)	-	-	92
1,5434	0,0214	7,9223	2,9890	0,0251	10,6184	2.591	(1.105)	55	(28)	20.527	(11.730)	-	-	182
1,9092	0,0249	8,4316	3,6923	0,0275	10,8487	2.551	(1.157)	64	(32)	21.510	(12.547)	-	-	200
0,8656	0,0207	5,4135	2,0986	0,0272	8,5335	2.899	(1.103)	60	(30)	15.693	(9.416)	-	-	128
0,3133	0,0141	2,7735	1,0744	0,0243	5,9569	3.248	(945)	46	(23)	9.008	(5.630)	-	-	63
0,3420	0,0179	2,8077	1,3338	0,0300	6,2870	3.467	(1.032)	62	(31)	9.735	(6.490)	-	-	59
0,1031	0,0113	1,1613	0,7943	0,0293	4,5360	3.342	(642)	38	(19)	3.881	(2.911)	-	-	11
0,0008	0,0005	0,0221	0,1448	0,0152	1,4579	-	-	-	-	-	-	-	-	-

# $\Delta - \Gamma - \cup$ HEDGING

portfolio "C" = Port. "B" + Stock f( $\Delta$ hedge of "B")					
$\Delta$ Port. "B"	Stock and $\Delta$ Portfolio				$\Delta$ Portfolio "C"
Total $\Delta$ position	Stock to Buy/(Sell)	Warehouse	$\Delta$ Stock	$\Delta$ Stock Posit.	Total $\Delta$ position
396	(396)	(396)	1	(396)	-
388	8	(388)	1	(388)	-
394	(6)	(394)	1	(394)	-
435	(41)	(435)	1	(435)	-
435	-	(435)	1	(435)	-
429	6	(429)	1	(429)	-
420	9	(420)	1	(420)	-
385	35	(385)	1	(385)	-
280	105	(280)	1	(280)	-
250	30	(250)	1	(250)	-
165	85	(165)	1	(165)	-
170	(5)	(170)	1	(170)	-
160	10	(160)	1	(160)	-
92	68	(92)	1	(92)	-
182	(90)	(182)	1	(182)	-
200	(18)	(200)	1	(200)	-
128	72	(128)	1	(128)	-
63	65	(63)	1	(63)	-
59	4	(59)	1	(59)	-
11	48	(11)	1	(11)	-
-	11	-	1	-	-

# Δ – Γ – υ HEDGING

quantitative composition of the “C” Portfolio, value of Δ, Γ & υ

Stock		Short Opt.	Option for Γ		Option for υ		Delta e Gamma		Vega
Buy/sell	Warehouse	Short Opt.	Buy/sell	Warehouse	Buy/sell	Warehouse	Δ portfolio C	Γ portfolio C	υ portfolio C
168	168	(1.000)	2.022	2.022	(1.051)	(1.051)	-	-	-
1	169	(1.000)	10	2.033	(2)	(1.053)	-	-	-
14	183	(1.000)	(17)	2.015	(3)	(1.056)	-	-	-
65	248	(1.000)	(113)	1.903	3	(1.053)	-	-	-
18	266	(1.000)	(22)	1.880	(1)	(1.054)	-	-	-
11	277	(1.000)	(7)	1.873	(2)	(1.056)	-	-	-
6	283	(1.000)	4	1.877	(4)	(1.060)	-	-	-
(47)	236	(1.000)	107	1.984	(13)	(1.074)	-	-	-
(102)	134	(1.000)	256	2.240	1	(1.073)	-	-	-
(14)	120	(1.000)	72	2.311	1	(1.072)	-	-	-
(51)	69	(1.000)	205	2.516	37	(1.034)	-	-	-
10	79	(1.000)	13	2.529	(12)	(1.046)	-	-	-
-	79	(1.000)	55	2.584	(1)	(1.048)	-	-	-
(38)	41	(1.000)	227	2.811	82	(966)	-	-	-
80	121	(1.000)	(220)	2.591	(139)	(1.105)	-	-	-
49	170	(1.000)	(40)	2.551	(52)	(1.157)	-	-	-
(63)	107	(1.000)	348	2.899	53	(1.103)	-	-	-
(53)	54	(1.000)	349	3.248	158	(945)	-	-	-
29	83	(1.000)	219	3.467	(87)	(1.032)	-	-	-
(49)	34	(1.000)	(125)	3.342	391	(642)	-	-	-
(34)	-	(1.000)	(3.342)	-	642	-	-	-	-

# Δ - Γ - U HEDGING

Delta Gamma Vega Hedging Cash Flow							
Stock	Option	Opt for Γ	Opt for U	Bank			Hedging Revenue (cost)
Dollars in Stock (Flow)	Cash ex Shorting/Exercising Option	Dollars in Option (Flow)	Dollars in Option (Flow)	Cash	Interest (Flow)	Borrow (stock)	
16.800	10.378	17.255	(11.450)	12.228		12.228	
100		83	(26)	156	7,6	12.392	
1.414		(145)	(30)	1.239	7,7	13.638	
7.009		(1.352)	41	5.698	8,5	19.345	
1.961		(277)	(12)	1.673	12,1	21.029	
1.200		(87)	(37)	1.076	13,1	22.119	
652		46	(60)	638	13,8	22.771	
(4.871)		889	(149)	(4.131)	14,2	18.654	
(9.545)		944	5	(8.596)	11,7	10.069	
(1.287)		209	5	(1.073)	6,3	9.002	
(4.396)		280	89	(4.027)	5,6	4.981	
876		18	(30)	864	3,1	5.848	
-		69	(3)	66	3,7	5.918	
(3.178)		119	97	(2.962)	3,7	2.959	
7.363		(340)	(415)	6.608	1,9	9.569	
4.653		(76)	(192)	4.385	6,0	13.961	
(5.763)		301	112	(5.350)	8,7	8.619	
(4.695)		109	170	(4.416)	5,4	4.209	
2.653		75	(116)	2.612	2,6	6.824	
(4.449)		(13)	310	(4.152)	4,3	2.676	
(2.976)	-	-	93	(2.883)	1,7	(205)	205

LET US HOLD THE OPTION 'Z' UNTIL  
MATURITY

AT MATURITY THE OPTION 'W' IS  
IN – THE MONEY



# Δ - Γ - υ HEDGING

Short 1000 call on 1 stock			Option and Δ			Stock and Δ				Δ Portfolio	Γ Portfolio "A"	υ Portfolio "A"
Time Step	Time to Expiration	STOCK PRICE	Q. Opz.	Δ call	Δ call Posit.	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position	Γ portfolio = Γ I option * n.az. Underlying	υ portfolio = υ I option * n.az. Underlying
0	0,2500	100,0	(1.000)	0,564	(564)	564	564	1	564	-	(15,70)	(19.628)
1	0,2375	102,9	(1.000)	0,607	(607)	43	607	1	607	-	(15,28)	(19.202)
2	0,2250	96,9	(1.000)	0,508	(508)	(99)	508	1	508	-	(17,31)	(18.291)
3	0,2125	94,2	(1.000)	0,456	(456)	(52)	456	1	456	-	(18,23)	(17.176)
4	0,2000	92,4	(1.000)	0,417	(417)	(39)	417	1	417	-	(18,87)	(16.091)
5	0,1875	91,9	(1.000)	0,402	(402)	(15)	402	1	402	-	(19,41)	(15.368)
6	0,1750	97,1	(1.000)	0,499	(499)	97	499	1	499	-	(19,60)	(16.181)
7	0,1625	98,0	(1.000)	0,512	(512)	13	512	1	512	-	(20,16)	(15.723)
8	0,1500	107,3	(1.000)	0,688	(688)	176	688	1	688	-	(16,96)	(14.659)
9	0,1375	107,6	(1.000)	0,697	(697)	9	697	1	697	-	(17,45)	(13.898)
10	0,1250	113,8	(1.000)	0,801	(801)	104	801	1	801	-	(13,82)	(11.186)
11	0,1125	105,2	(1.000)	0,660	(660)	(141)	660	1	660	-	(20,72)	(12.905)
12	0,1000	105,8	(1.000)	0,677	(677)	17	677	1	677	-	(21,42)	(11.989)
13	0,0875	107,5	(1.000)	0,721	(721)	44	721	1	721	-	(21,09)	(10.668)
14	0,0750	110,8	(1.000)	0,800	(800)	79	800	1	800	-	(18,42)	(8.488)
15	0,0625	118,9	(1.000)	0,928	(928)	128	928	1	928	-	(9,17)	(4.049)
16	0,0500	128,5	(1.000)	0,989	(989)	61	989	1	989	-	(1,89)	(782)
17	0,0375	128,1	(1.000)	0,995	(995)	6	995	1	995	-	(1,03)	(317)
18	0,0250	126,1	(1.000)	0,998	(998)	3	998	1	998	-	(0,47)	(93)
19	0,0125	129,5	(1.000)	1,000	(1.000)	2	1.000	1	1.000	-	(0,00)	(0)
20	0,0000	135,4	(1.000)	1,000	(1.000)	-	1.000	1	1.000	-	-	-

# Δ - Γ - υ HEDGING

] Portfolio B = Portfolio A + II Option + III Option:

Γ-υ Portfolio "B"														Δ Port. "B"	
II Option			III Option												
II Option value	Γ II option	υ II option	III Option value	Γ III option	υ III option	n. II option Buy/sell	n. III option buy/sell	Γ II option Tot	Γ III option Tot	υ II option Tot	υ III option Tot	Γ portfolio "B"	υ portfolio "B"	Total Δ position	
8,5320	0,0155	20,3815	10,8995	0,0149	20,5532	2,022	(1,051)	31	(16)	41,219	(21,591)	-	-	396	
9,7225	0,0154	20,3963	12,3193	0,0145	20,1679	1,982	(1,052)	31	(15)	40,426	(21,224)	-	-	413	
6,5788	0,0166	18,5301	8,7069	0,0164	19,2663	2,084	(1,055)	35	(17)	38,614	(20,323)	-	-	358	
5,2071	0,0170	16,9797	7,1031	0,0173	18,1947	2,142	(1,055)	36	(18)	36,374	(19,197)	-	-	324	
4,3079	0,0172	15,6141	6,0409	0,0179	17,1595	2,190	(1,055)	38	(19)	34,192	(18,102)	-	-	298	
3,9135	0,0175	14,7975	5,5943	0,0184	16,4811	2,216	(1,057)	39	(19)	32,785	(17,417)	-	-	285	
5,5771	0,0185	16,3570	7,7242	0,0183	17,2915	2,120	(1,069)	39	(20)	34,674	(18,493)	-	-	335	
5,6346	0,0191	16,0207	7,8617	0,0188	16,8732	2,114	(1,075)	40	(20)	33,864	(18,141)	-	-	336	
10,0788	0,0179	16,7351	13,1938	0,0158	15,9604	1,898	(1,072)	34	(17)	31,762	(17,102)	-	-	398	
9,8899	0,0185	16,0717	13,0655	0,0162	15,2678	1,887	(1,076)	35	(17)	30,323	(16,425)	-	-	390	
13,5852	0,0162	14,3971	17,3239	0,0132	12,7919	1,709	(1,049)	28	(14)	24,608	(13,423)	-	-	389	
7,7618	0,0212	14,7012	10,7844	0,0189	14,3646	1,951	(1,098)	41	(21)	28,678	(15,773)	-	-	357	
7,6759	0,0222	13,9702	10,7993	0,0194	13,5542	1,931	(1,106)	43	(21)	26,975	(14,986)	-	-	346	
8,2416	0,0227	13,1200	11,5999	0,0191	12,4028	1,858	(1,106)	42	(21)	24,383	(13,716)	-	-	334	
9,9227	0,0218	11,7366	13,6940	0,0171	10,5019	1,688	(1,078)	37	(18)	19,806	(11,318)	-	-	310	
15,6275	0,0149	7,8992	20,1172	0,0102	6,2860	1,230	(902)	18	(9)	9,718	(5,669)	-	-	225	
24,0642	0,0059	3,0260	28,9788	0,0036	2,2120	646	(530)	4	(2)	1,955	(1,173)	-	-	101	
23,5122	0,0050	2,0470	28,4795	0,0029	1,5131	412	(349)	2	(1)	844	(528)	-	-	57	
21,3530	0,0048	1,4442	26,3520	0,0028	1,1223	193	(165)	1	(0)	278	(185)	-	-	25	
24,6183	0,0010	0,2100	29,6596	0,0008	0,2379	2	(1)	0	(0)	0	(0)	-	-	1	
30,4471	0,0000	0,0002	35,4896	0,0000	0,0045	-	-	-	-	-	-	-	-	-	

# Δ – Γ – U HEDGING

portfolio "C" = Port. "B" + Stock f(Δ hedge of "B")					
Δ Port. "B"	Stock and Δ Portfolio				Δ Portfolio "C"
Total Δ position	Stock to Buy/(Sell)	Warehouse	Δ Stock	Δ Stock Posit.	Total Δ position
396	(396)	(396)	1	(396)	-
413	(17)	(413)	1	(413)	-
358	55	(358)	1	(358)	-
324	34	(324)	1	(324)	-
298	26	(298)	1	(298)	-
285	13	(285)	1	(285)	-
335	(50)	(335)	1	(335)	-
336	(1)	(336)	1	(336)	-
398	(62)	(398)	1	(398)	-
390	8	(390)	1	(390)	-
389	1	(389)	1	(389)	-
357	32	(357)	1	(357)	-
346	11	(346)	1	(346)	-
334	12	(334)	1	(334)	-
310	24	(310)	1	(310)	-
225	85	(225)	1	(225)	-
101	124	(101)	1	(101)	-
57	44	(57)	1	(57)	-
25	32	(25)	1	(25)	-
1	24	(1)	1	(1)	-
-	1	-	1	-	-

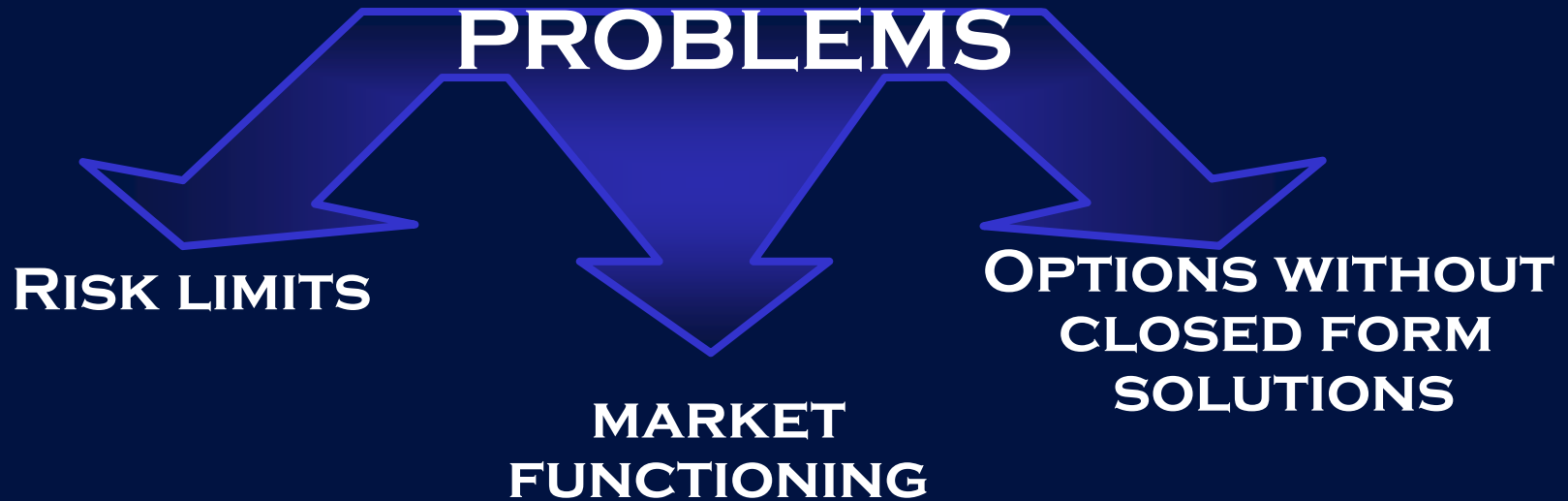
# Δ – Γ – υ HEDGING

quantitative composition of the “C” Portfolio, value of Δ & Γ & υ									
Stock		Short Opt.	Option for Γ		Option for υ		Delta e Gamma		Vega
Buy/sell	Warehouse	Short Opt.	Buy/sell	Warehouse	Buy/sell	Warehouse	Δ portfolio C	Γ portfolio C	υ portfolio C
168	168	(1.000)	2.022	2.022	(1.051)	(1.051)	-	-	-
26	194	(1.000)	(40)	1.982	(2)	(1.052)	-	-	-
(44)	150	(1.000)	102	2.084	(3)	(1.055)	-	-	-
(18)	132	(1.000)	58	2.142	(0)	(1.055)	-	-	-
(13)	119	(1.000)	48	2.190	0	(1.055)	-	-	-
(2)	117	(1.000)	26	2.216	(2)	(1.057)	-	-	-
47	164	(1.000)	(96)	2.120	(13)	(1.069)	-	-	-
12	176	(1.000)	(6)	2.114	(6)	(1.075)	-	-	-
114	290	(1.000)	(216)	1.898	4	(1.072)	-	-	-
17	307	(1.000)	(11)	1.887	(4)	(1.076)	-	-	-
105	412	(1.000)	(177)	1.709	26	(1.049)	-	-	-
(109)	303	(1.000)	241	1.951	(49)	(1.098)	-	-	-
28	331	(1.000)	(20)	1.931	(8)	(1.106)	-	-	-
56	387	(1.000)	(72)	1.858	(0)	(1.106)	-	-	-
103	490	(1.000)	(171)	1.688	28	(1.078)	-	-	-
213	703	(1.000)	(457)	1.230	176	(902)	-	-	-
185	888	(1.000)	(584)	646	372	(530)	-	-	-
50	938	(1.000)	(234)	412	182	(349)	-	-	-
35	973	(1.000)	(220)	193	183	(165)	-	-	-
26	999	(1.000)	(191)	2	164	(1)	-	-	-
1	1.000	(1.000)	(2)	-	1	-	-	-	-

# Δ - Γ - U HEDGING

Delta Gamma Vega Hedging Cash Flow							
Stock	Option	Opt. for $\Gamma$	Opt. for $U$	Bank			Hedging Revenue (cost)
Dollars in Stock (Flow)	Cash ex Shorting/Exercising Option	Dollars in Option (Flow)	Dollars in Option (Flow)	Cash	Interest (Flow)	Borrow (stock)	
16.800	10.378	17.255	(11.450)	12.228		12.228	
2.674		(393)	(23)	2.259	7,6	14.494	
(4.264)		670	(22)	(3.616)	9,1	10.888	
(1.695)		304	(2)	(1.393)	6,8	9.502	
(1.201)		205	1	(994)	5,9	8.514	
(184)		101	(10)	(94)	5,3	8.425	
4.565		(534)	(98)	3.933	5,3	12.364	
1.176		(34)	(45)	1.097	7,7	13.468	
12.238		(2.176)	48	10.110	8,4	23.586	
1.830		(111)	(55)	1.664	14,7	25.265	
11.950		(2.411)	459	9.998	15,8	35.278	
(11.471)		1.874	(525)	(10.122)	22,1	25.178	
2.963		(152)	(82)	2.728	15,7	27.922	
6.021		(597)	(2)	5.422	17,5	33.361	
11.417		(1.696)	386	10.106	20,9	43.489	
25.319		(7.146)	3.538	21.711	27,2	65.227	
23.774		(14.061)	10.769	20.482	40,8	85.750	
6.406		(5.492)	5.170	6.084	53,6	91.888	
4.413		(4.693)	4.834	4.554	57,4	96.499	
3.367		(4.690)	4.860	3.537	60,3	100.096	
135	(100.000)	-	49	185	62,6	100.343	(343)

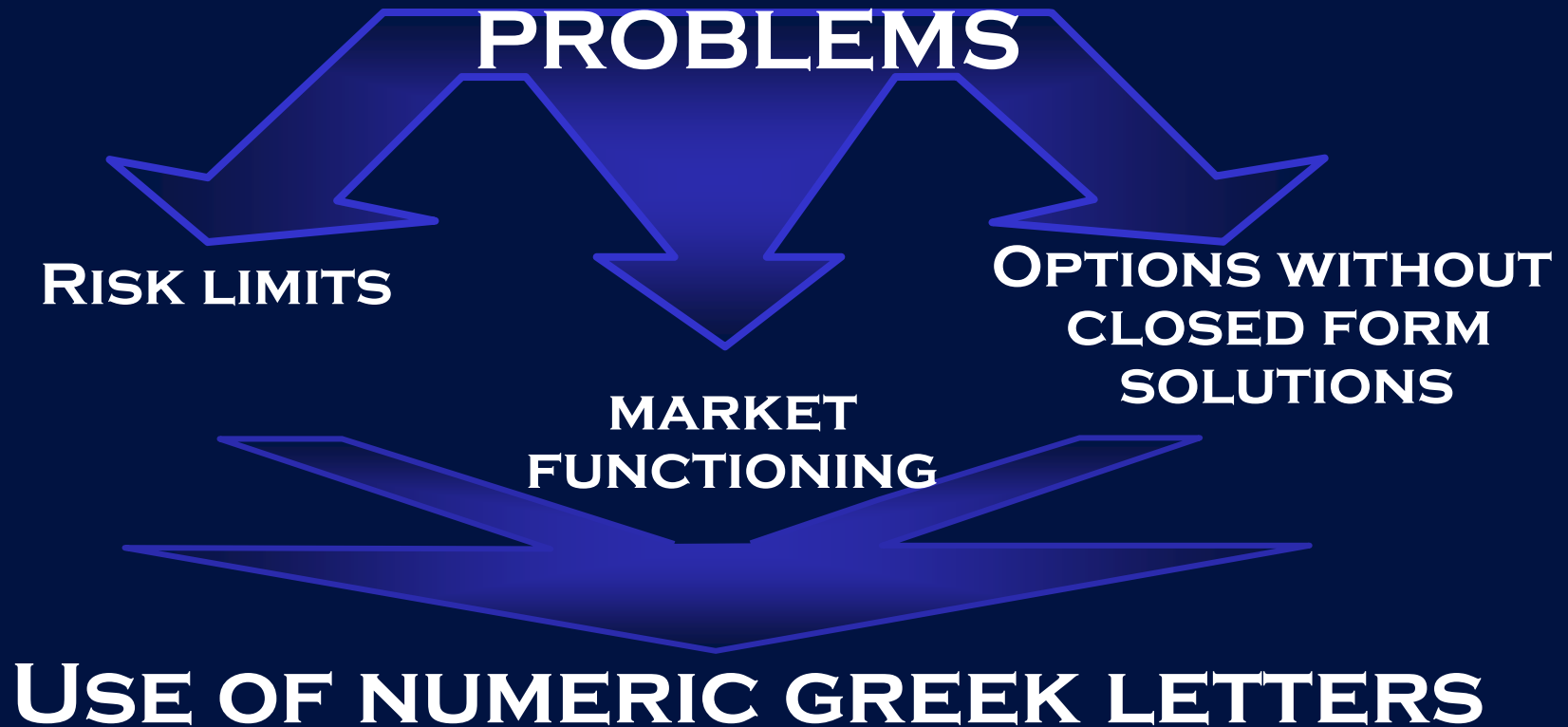
## RISK MANAGEMENT OF A FINANCIAL INSTITUTION



# HEDGING OF A FINANCIAL INSTITUTION

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## RISK MANAGEMENT OF A FINANCIAL INSTITUTION



## WHAT IS A NUMERIC GREEK LETTER?

$$\Delta = \frac{1}{2}(\Delta_{+1\%} + \Delta_{-1\%})$$

$$\Gamma = \frac{1}{2}(\Gamma_{+1\%} + \Gamma_{-1\%})$$

$$v = \frac{1}{2}(v_{+1\%} + v_{-1\%})$$

... LET US LEAVE OUT THE OTHERS BECAUSE THEY ARE NOT SO IMPORTANT



## FINANCIAL INSTITUTIONS DEFINE SOME BOUNDS IN TERMS OF GREEK LETTERS WITH REFERENCE TO:

- SECURITY
- MARKET

## SOME DEFINITIONS

- **ANOMALOUS EXERCISE**
- **PAYMENT BY PHYSICAL DELIVERY**
- **PAYMENT BY CASH SETTLEMENT**

**ANOMALOUS EXERCISE**

**THE HOLDER OF THE OPTION CAN  
PARTIALLY EXERCISE HIS RIGHT**

**PAYMENT BY PHYSICAL**

**SETTLEMENT**

**THE HOLDER OF THE OPTION MUST  
DELIVER THE UNDERLYING  
SECURITY**

## CASH SETTLEMENT

**THE HOLDER OF THE OPTION MUST  
DELIVER THE DIFFERENTIAL BY  
*CASH***

**SOME REMARKS**

**CASH  
SETTLEMENT**

**MICROSTRUCTURE  
ELEMENTS OF THE  
MARKET**

**KNOCK-IN TERMS**

**SOME REMARKS**

**CASH  
SETTLEMENT**

**MICROSTRUCTURE  
ELEMENTS OF THE  
MARKET**

**KNOCK-IN TERMS**



**RISK MANAGEMENT  
OF A FINANCIAL INSTITUTION**



SOME REMARKS

CASH  
SETTLEMENT

MICROSTRUCTURE  
ELEMENTS OF THE  
MARKET

KNOCK-IN TERMS



RISK MANAGEMENT  
OF A FINANCIAL INSTITUTION



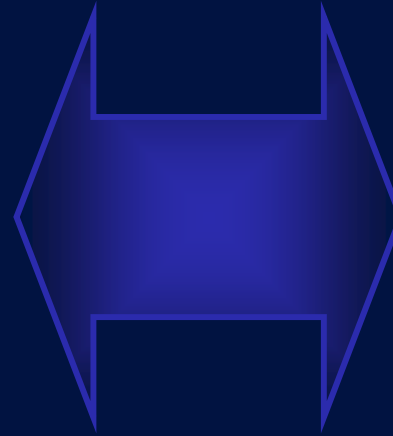
CASES OF MICROMANIPULATION



# HEDGING OF A FINANCIAL INSTITUTION

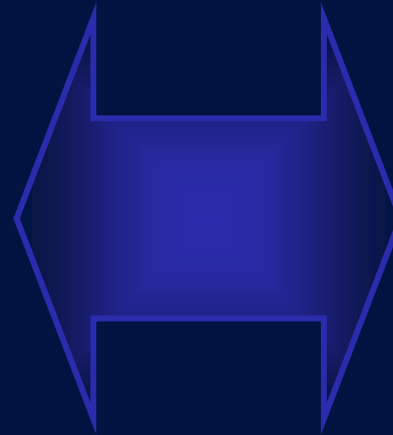
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**RISK MANAGEMENT  
OF A FINANCIAL  
INSTITUTION**



**COVERED  
WARRANT**

**RISK MANAGEMENT  
OF A FINANCIAL  
INSTITUTION**



**REVERSE  
CONVERTIBLE/  
DISCOUNT  
CERTIFICATE**

# HEDGING OF A FINANCIAL INSTITUTION

---

**RISK MANAGEMENT  
OF A  
FINANCIAL INSTITUTION**



**COVERED  
WARRANT**

**RISK MANAGEMENT  
OF A  
FINANCIAL INSTITUTION**

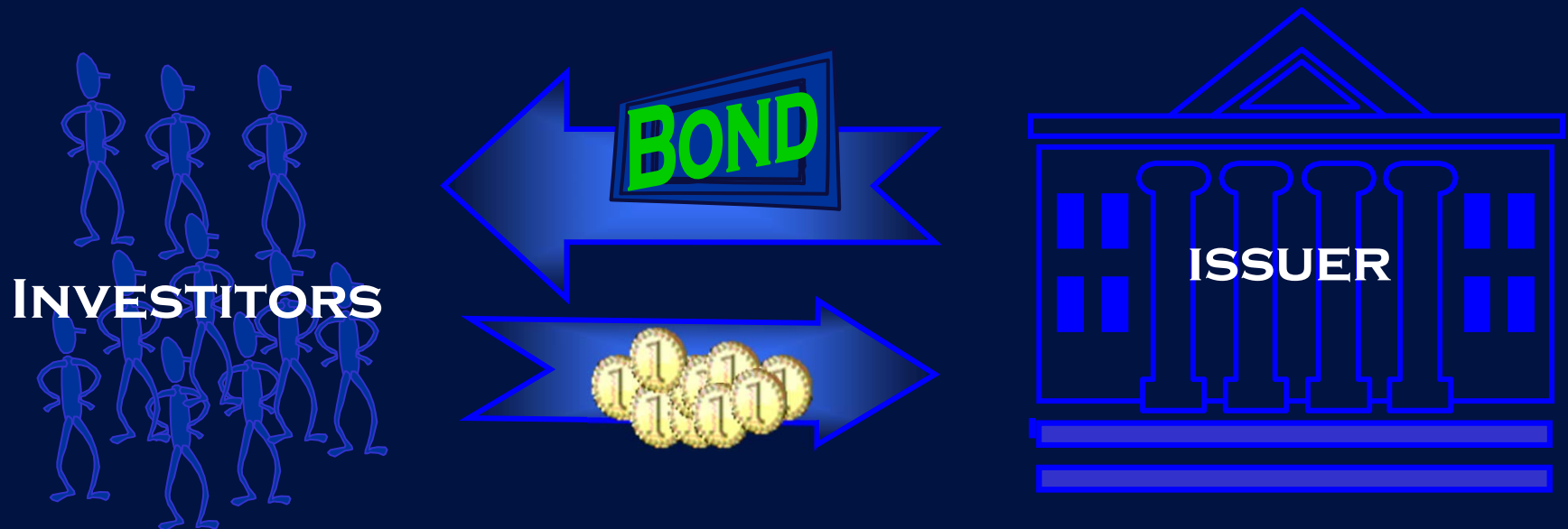


**REVERSE  
CONVERTIBLE**

## ... SOME INTRODUCTORY REMARKS ...

## THE ISSUE

HOW THE PRODUCT IS SOLD

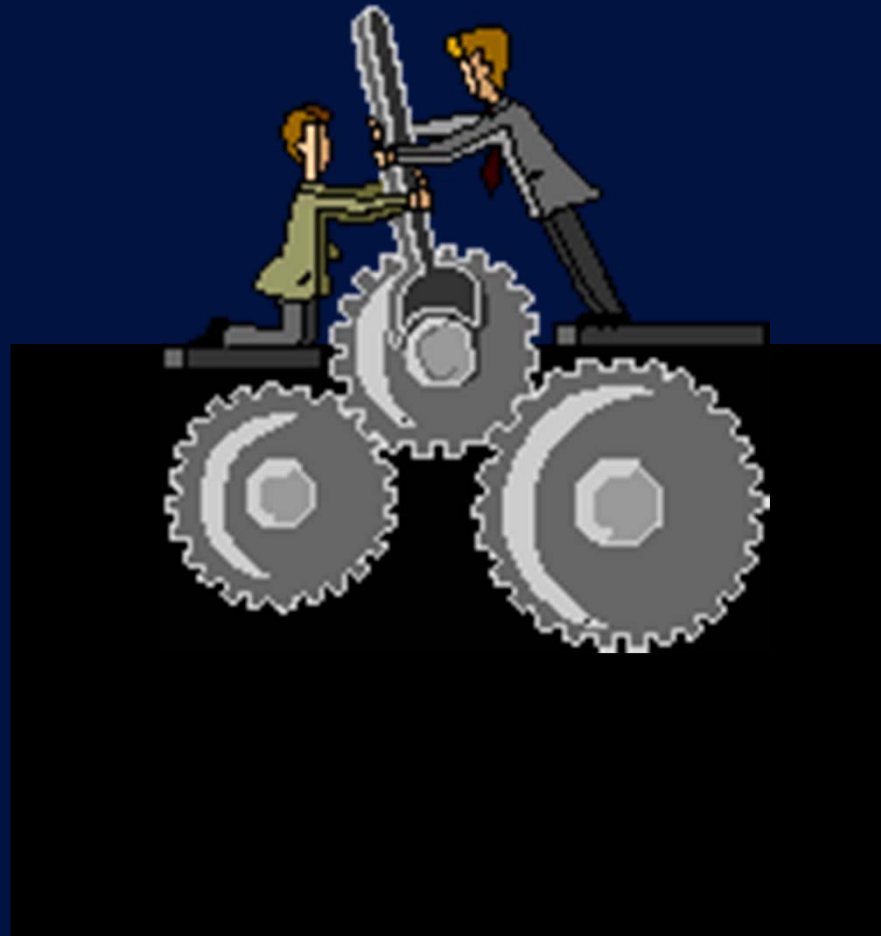


# UNBUNDLING

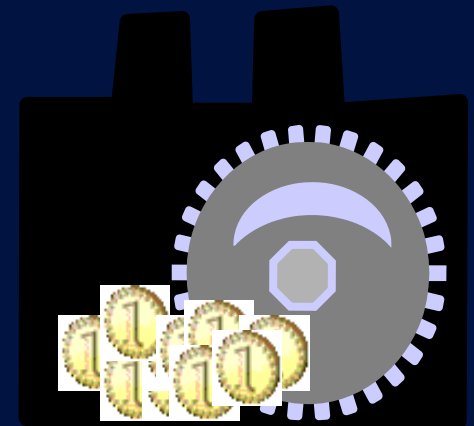
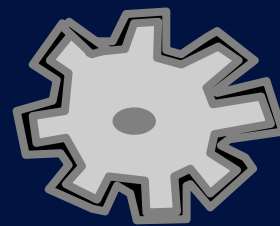
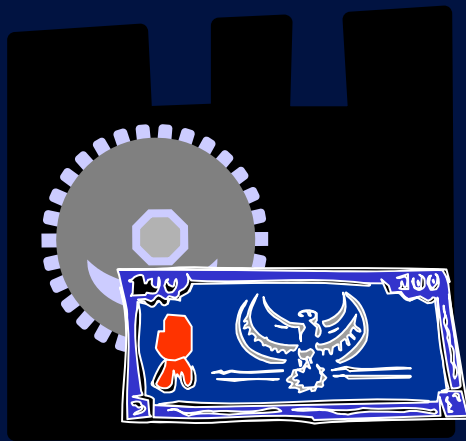


# REVERSE CONVERTIBLE - UNBUNDLING

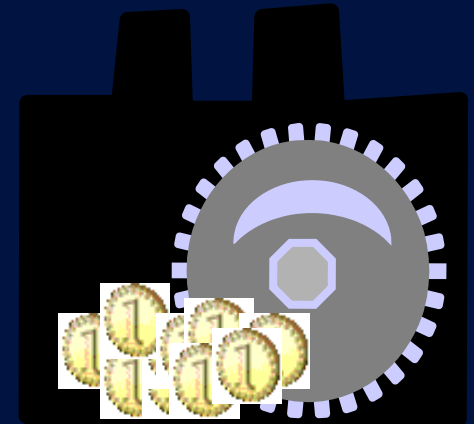
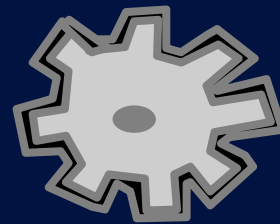
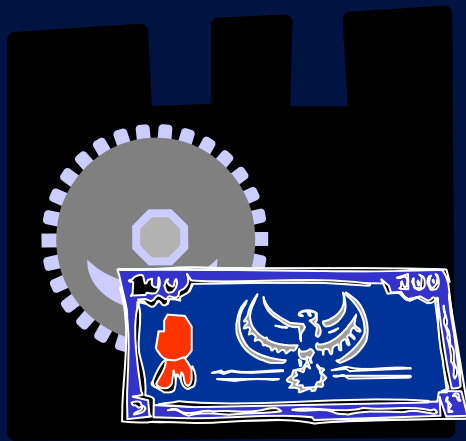
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# REVERSE CONVERTIBLE - UNBUNDLING

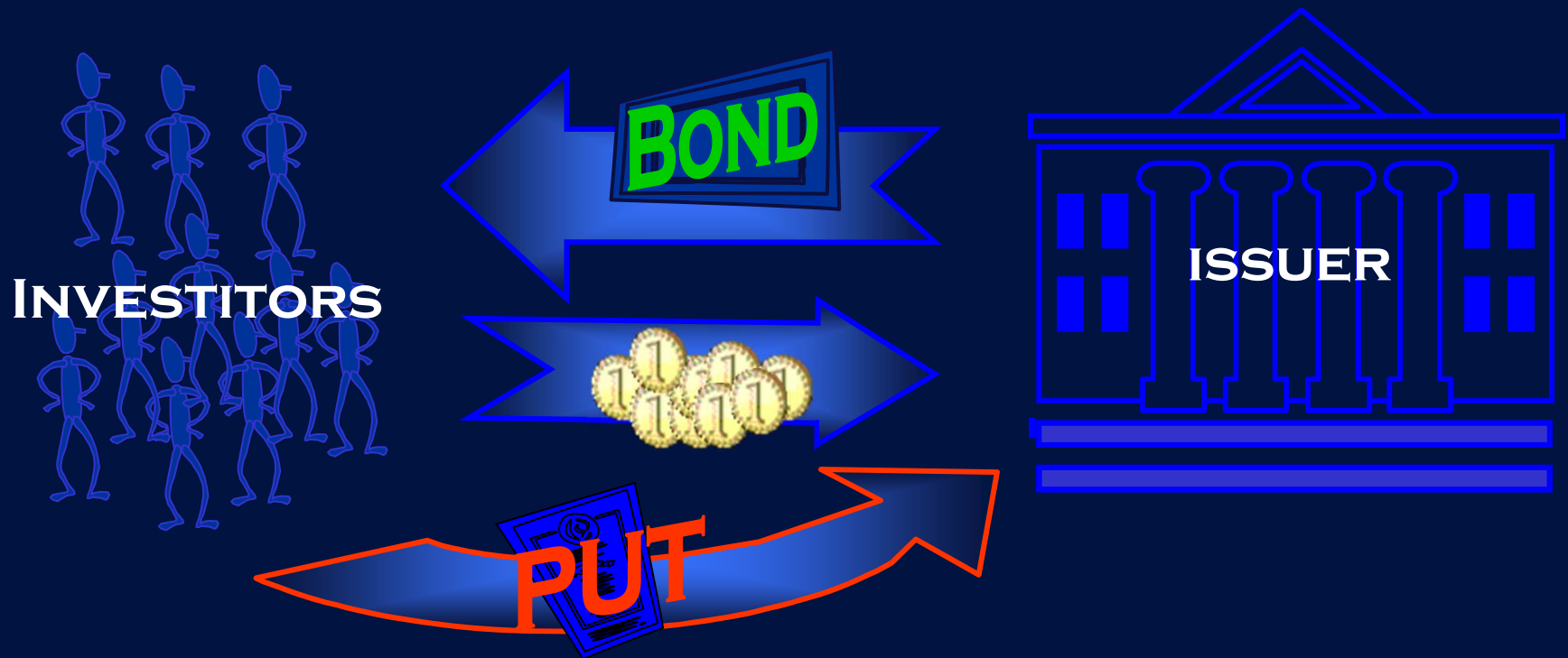


# INVESTOR SHORTS A PUT



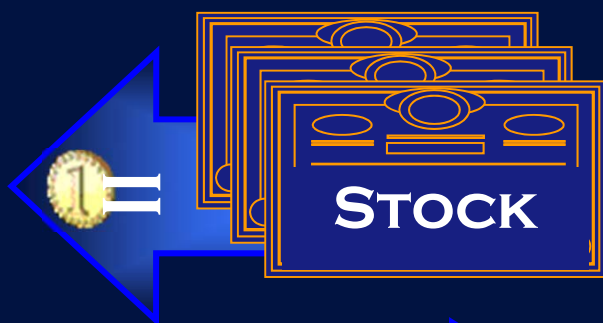


## THE ISSUE



# PUT SHORTING

OBLIGATION  
AT EXPIRY



# THE STRUCTURE

# REVERSE CONVERTIBLE – THE STRUCTURE

**MONEY PAID  
BY INVESTORS**



==



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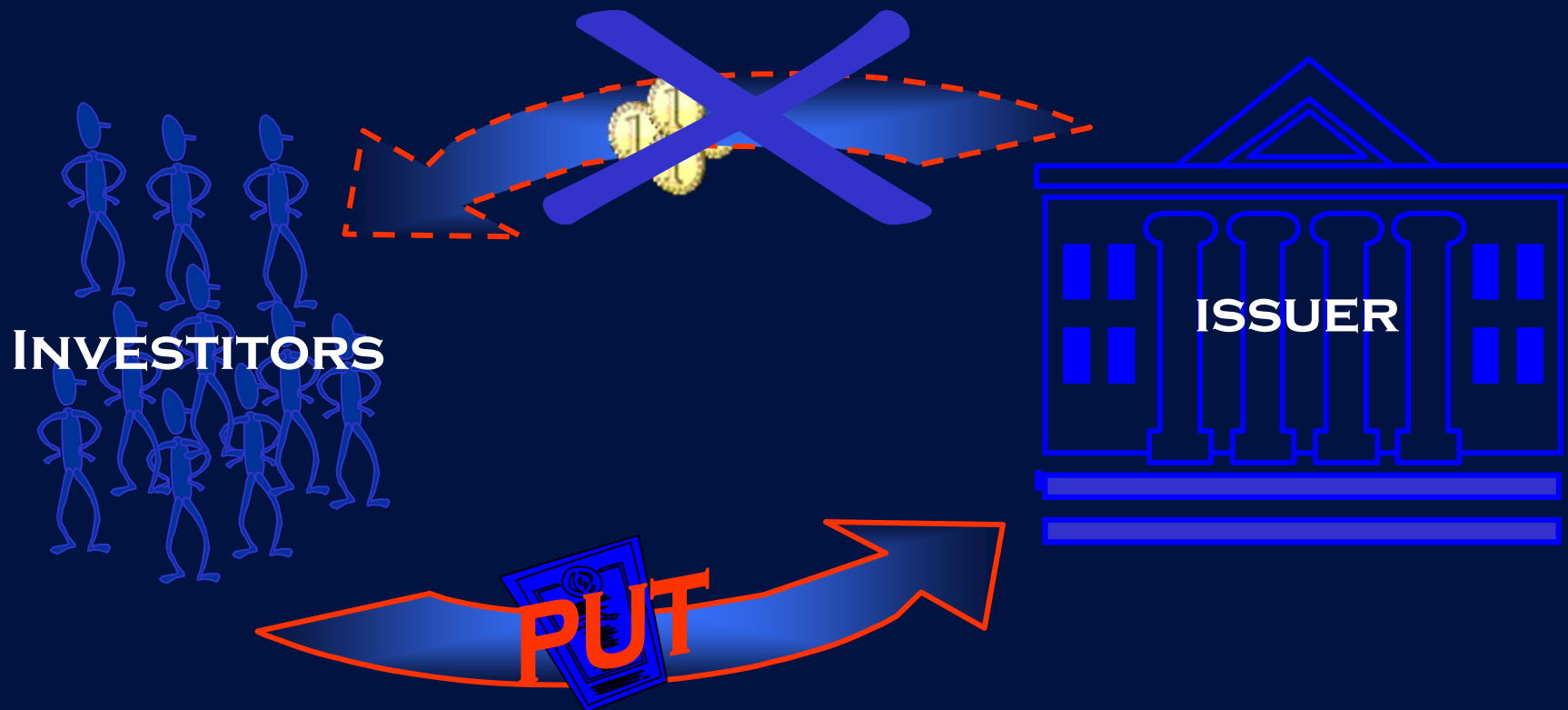


**FACE VALUE**

**N.STOCKS UNDERLYING THE PUT  
X  
STRIKE PRICE (K) OF THE PUT**

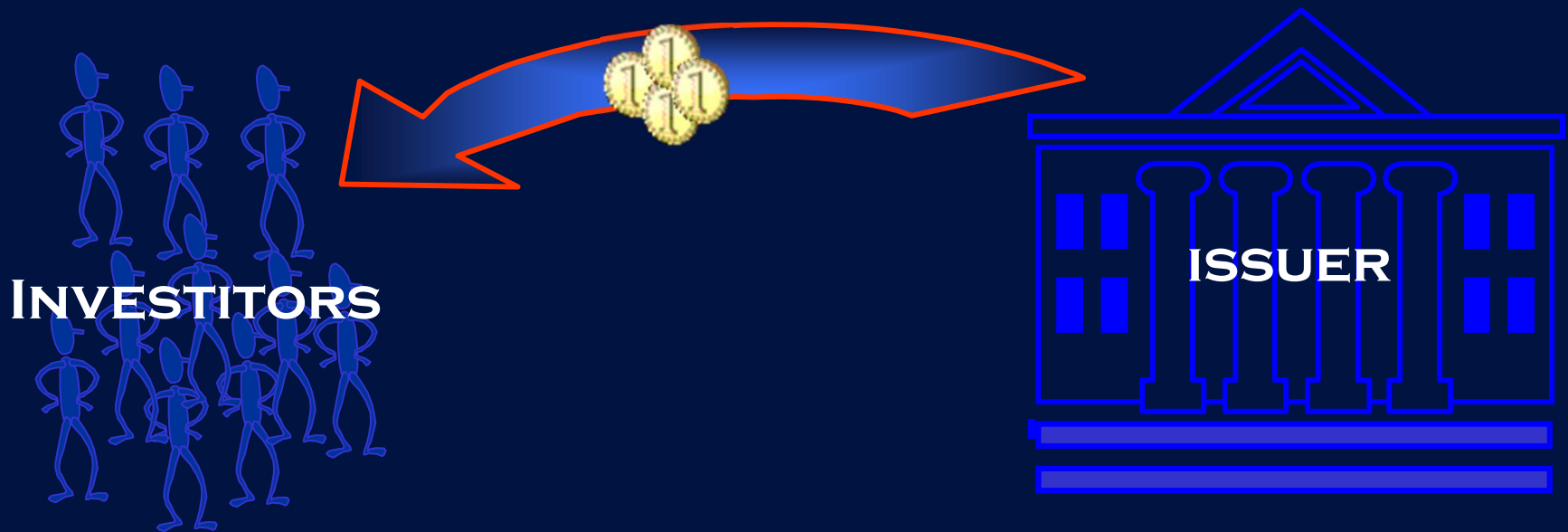
# REVERSE CONVERTIBLE – THE STRUCTURE

THE PUT PREMIUM IS NOT RECEIVED BY INVESTORS WHEN  
BUYING THE PRODUCT



# REVERSE CONVERTIBLE – THE STRUCTURE

.....BUT AT THE EXPIRY DATE  
IN THE FORM OF A MAXI-COUPON

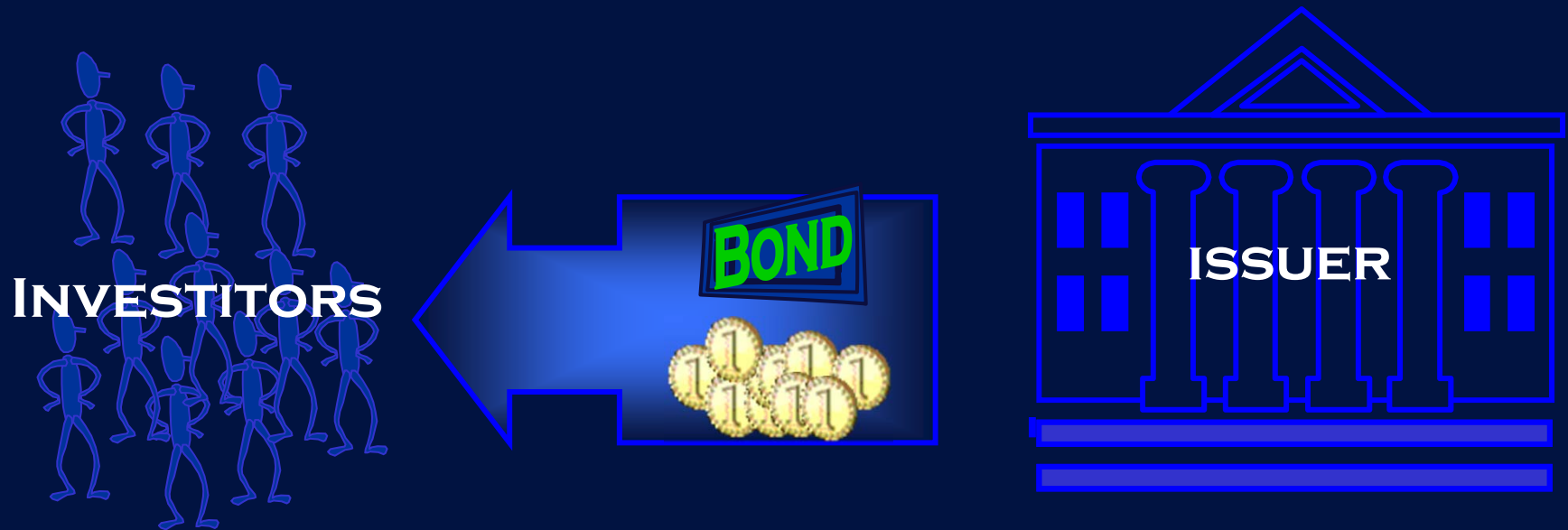


**EXPIRY DATE:**

**OPTION IS OUT-THE-MONEY**

## EXPIRY DATE

OPTION OUT-OF-THE MONEY



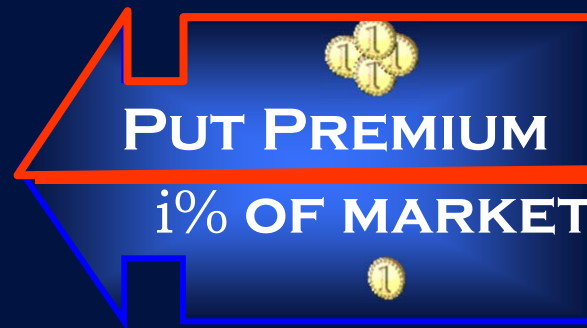


## EXPIRY DATE

OPTION OUT-OF THE MONEY



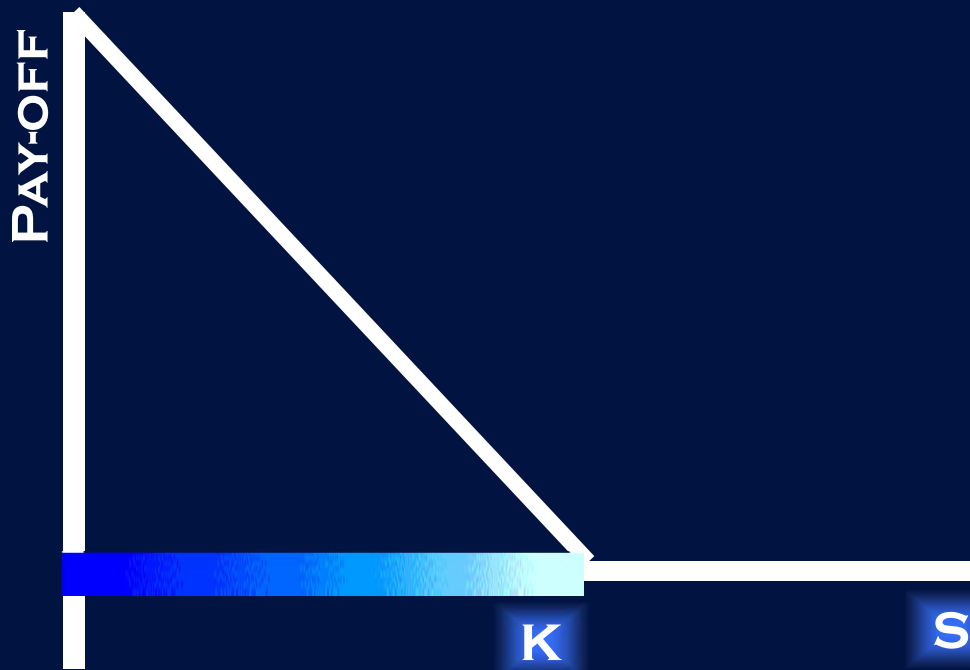
## MAXI-COUPON



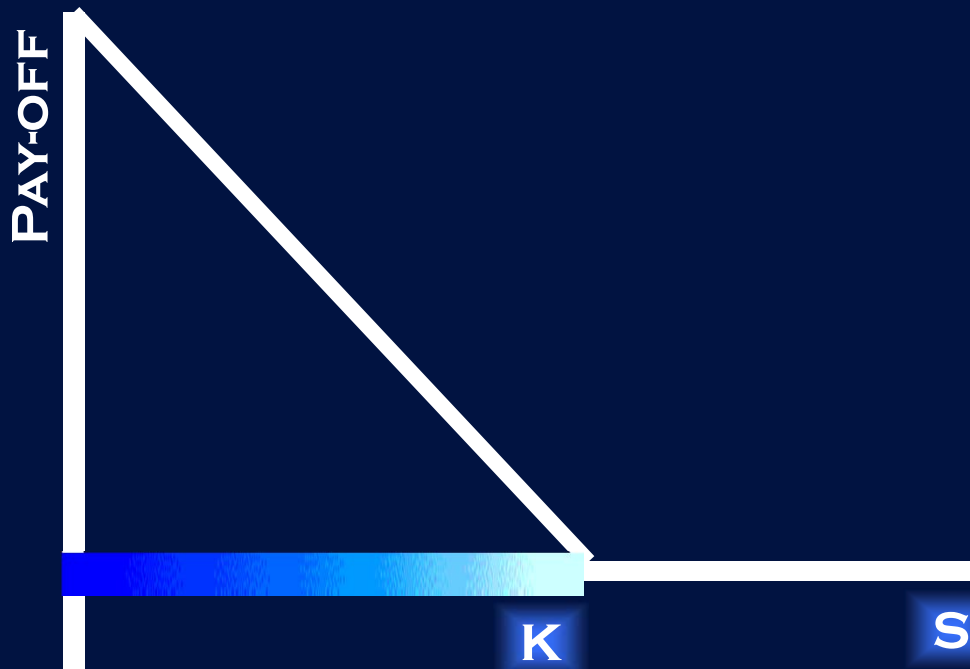
**EXPIRY DATE:  
OPTION IS IN-THE-MONEY**

ISSUER IS LONG PUT.....

# REVERSE CONVERTIBLE AND PUT OPTION

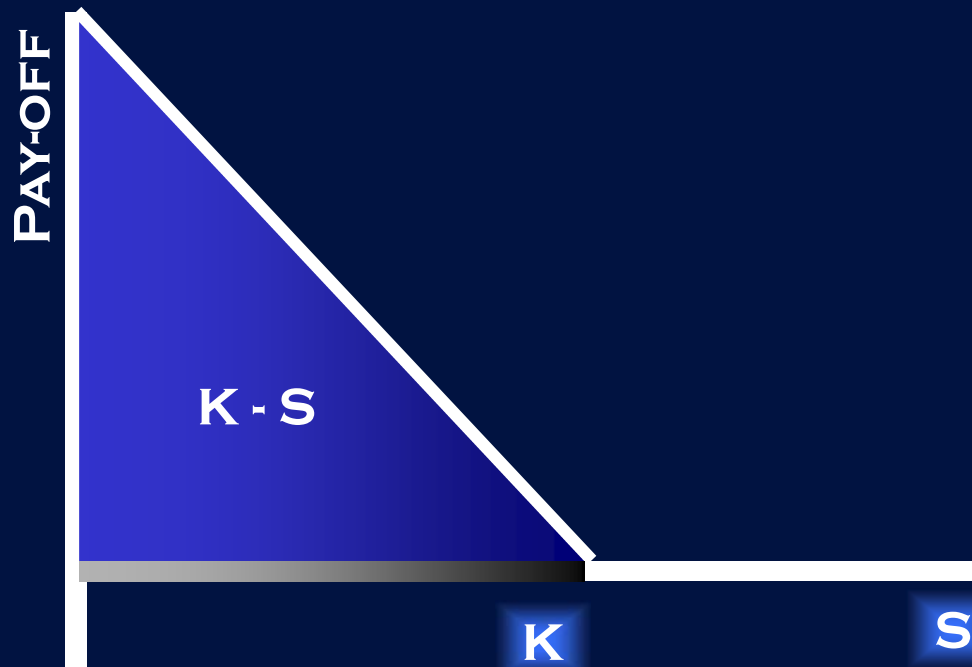


# REVERSE CONVERTIBLE AND PUT OPTION

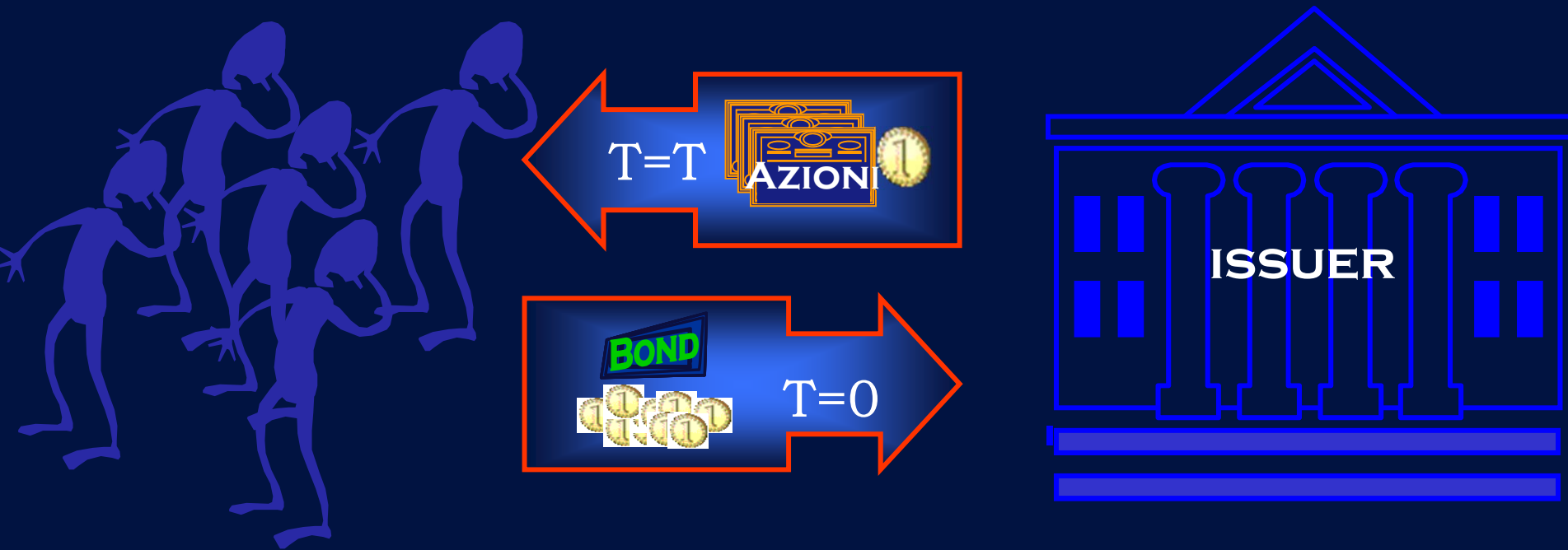


**EXERCISE THE OPTION**

# REVERSE CONVERTIBLE AND PUT OPTION

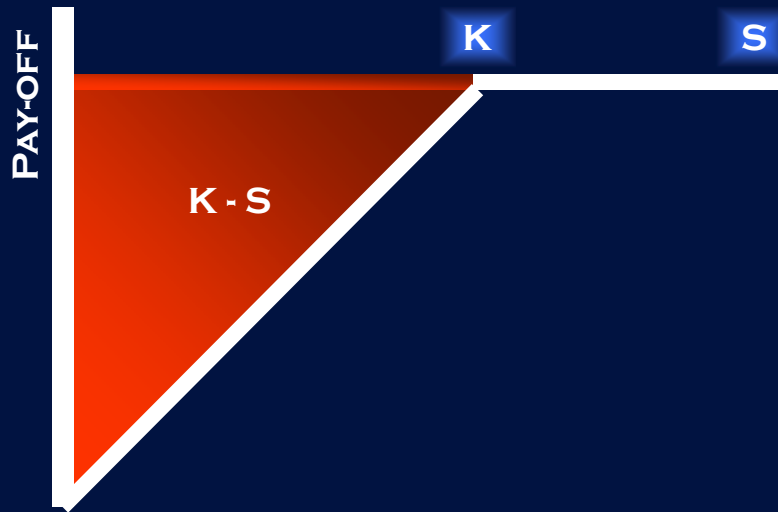
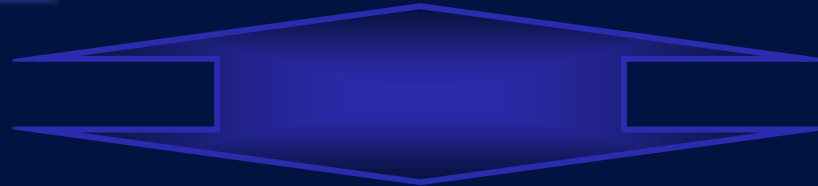
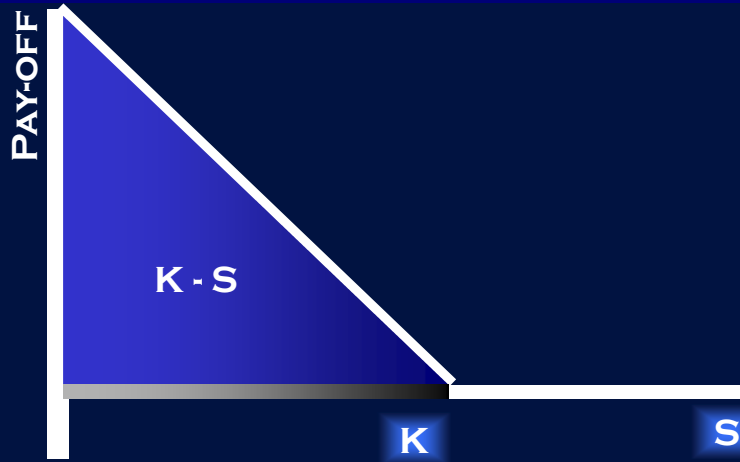


# REVERSE CONVERTIBLE – EXPIRY DATE



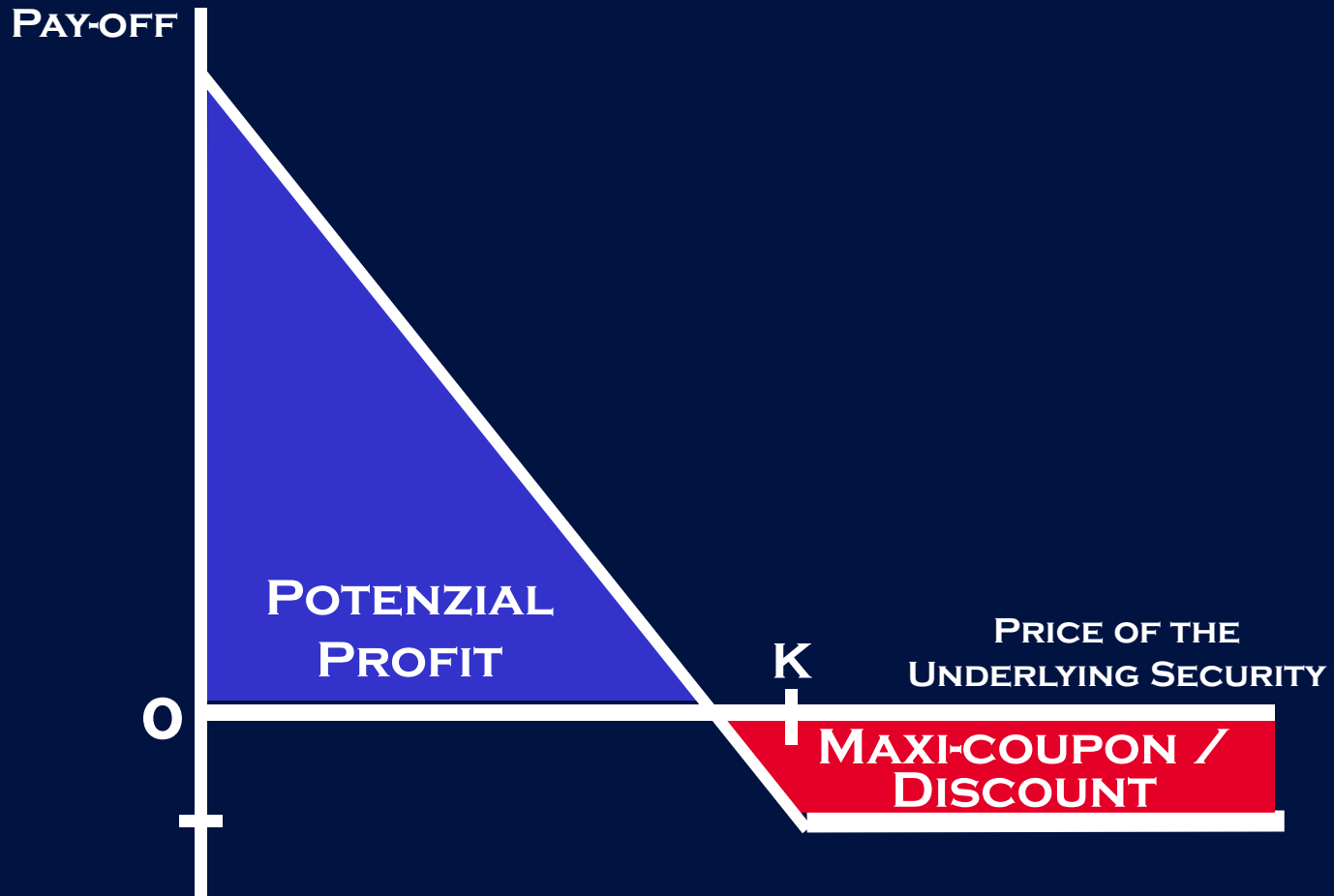


# REVERSE CONVERTIBLE AND PUT OPTION



**... SOME FURTHER  
REMARKS ...**

## 1. ISSUER'S PROFIT OR LOSS



# REVERSE CONVERTIBLE

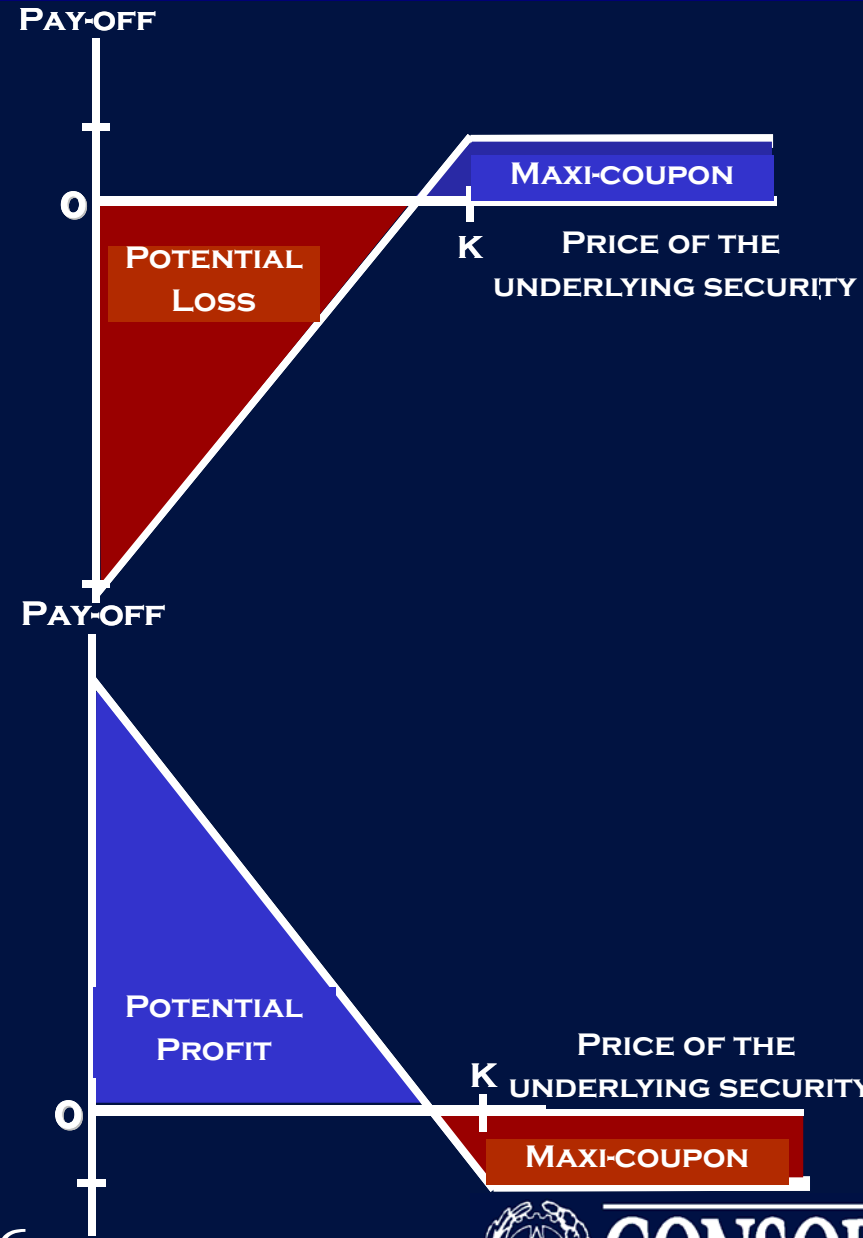
INVESTORS



ISSUER



MARCELLO MINENNA



196



CONSOB

## 2.

### THE PAY-OFF'S COMPUTATION METHOD

ARE BASED ON

NOT VERY LIQUID PRICES

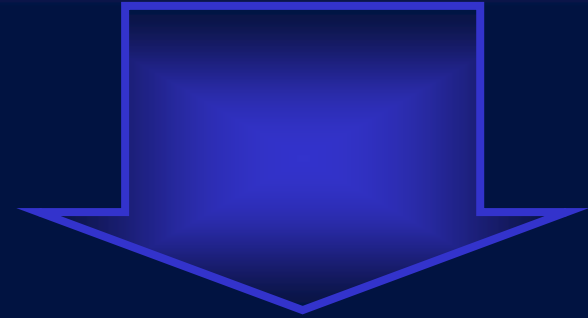
AS AN EXAMPLE:

OPENING AND CLOSING PRICES

## 3. TIPOLOGY OF STRUCTURE



**PLAIN VANILLA**



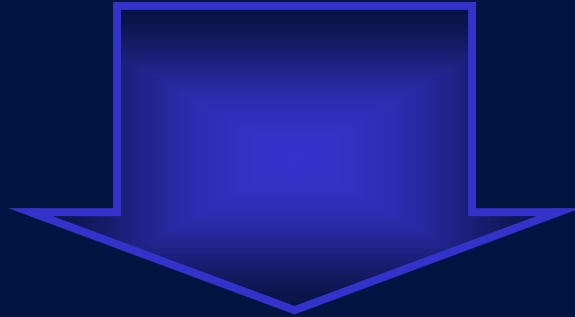
**KNOCK-IN**



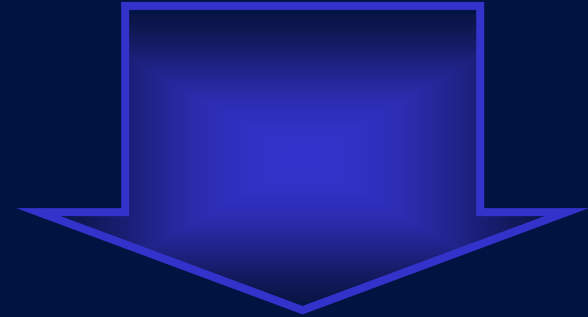
### **SETTLEMENT:**

- CASH
- PHYSICAL DELIVERY

## 4. HEDGING CHOICES OF FINANCIAL INSTITUTIONS



**THEY DON'T HEDGE  
THEMSELVES**



**THEY HEDGE  
THEMSELVES**

4.  
THE ISSUER **DOES NOT**  
HEDGE THE FINANCIAL RISK  
CONNECTED TO THE  
REVERSE BECAUSE ...



**... BECAUSE HE IS  
AN OPTION'S BUYER ...**

**... AND BECAUSE  
HE HAS FIXED  
THE PRICE**

# REVERSE CONVERTIBLE

## 1. ISSUER'S PROFIT OR LOSS



## 2. THE PAY-OFF'S COMPUTATION METHOD

ARE BASED ON

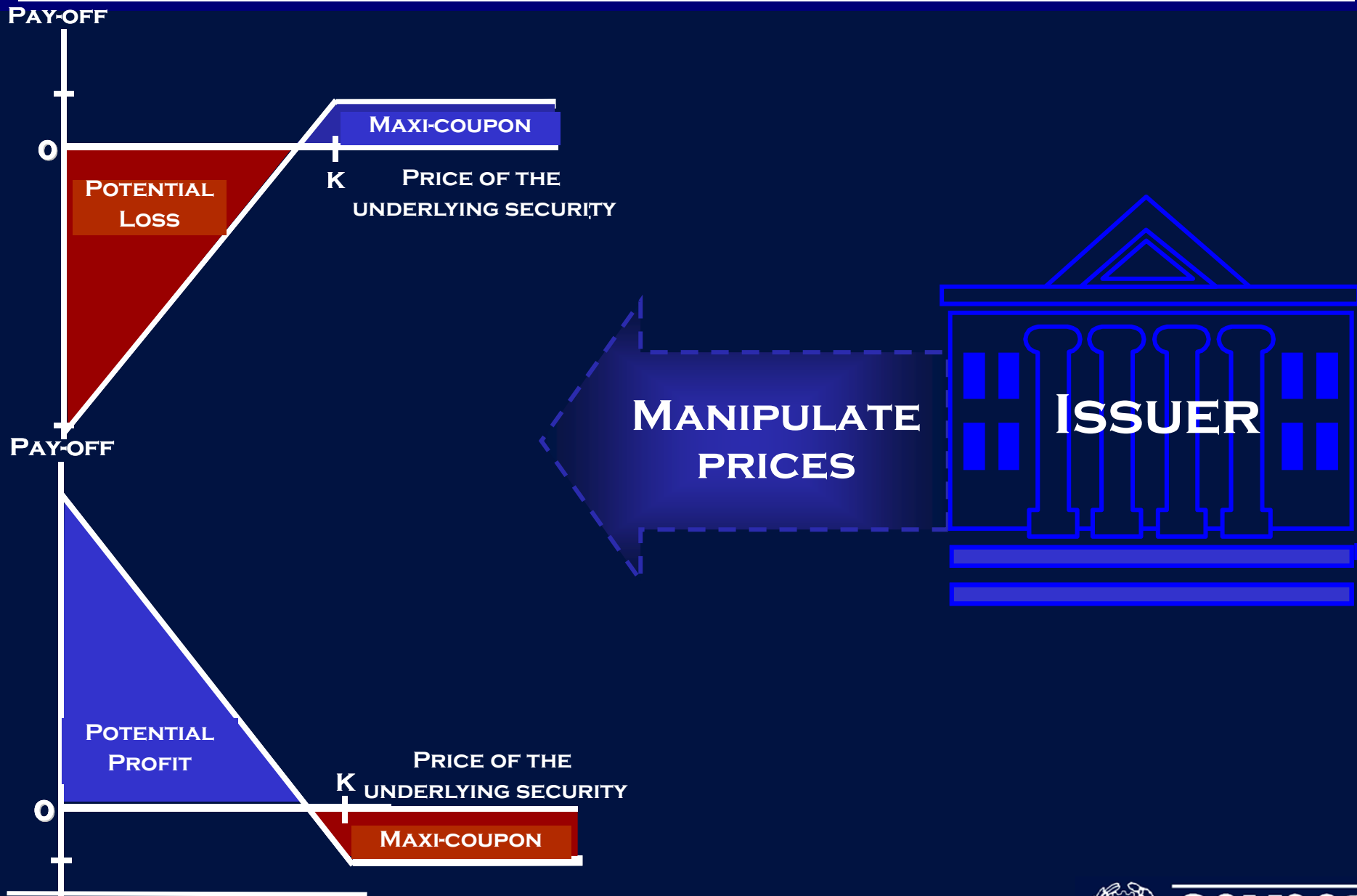
NOT VERY LIQUID PRICES

GENERATE

MANIPULATIONS

## 4. HEDGING LACK

# REVERSE CONVERTIBLE



**4.**  
**THE ISSUER HEDGES  
THE FINANCIAL RISK  
CONNECTED TO  
THE REVERSE BECAUSE ...**

**... BECAUSE  
THE PURCHASE OF AN  
OPTION ...**

**... IS PART OF THE MOST  
GENERAL SYSTEM  
OF RISK MANAGEMENT**

## FINANCIAL INSTITUTIONS FIX LIMITS IN TERMS OF GREEK LETTERS:

- SECURITY
- MARKET



## FINANCIAL INSTITUTIONS FIX LIMITS IN TERMS OF GREEK LETTERS:

- **SECURITY**
- **MARKET**

THE RESULTS THAT WE ARE GOING TO  
SHOW ARE EASILY EXTENSIBLE

## CASE STUDIES

PLAIN VANILLA

KNOCK-IN



OTM

ATM

ITM



### SETTLEMENT:

- CASH
- PHYSICAL SETTLEMENT

## PLAIN VANILLA



## SETTLEMENT:

- CASH
- PHYSICAL SETTLEMENT

## PLAIN VANILLA

**OTM**

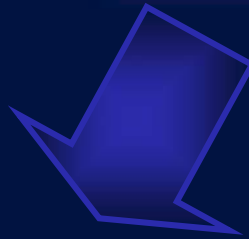
**SETTLEMENT BY  
PHYSICAL DELIVERY**



**RISK MANAGEMENT  
OF A  
FINANCIAL INSTITUTION**

**MICRO-MANIPULATIONS**

## PLAIN VANILLA



**OTM**



**SETTLEMENT  
BY CASH**



## PLAIN VANILLA

SETTLEMENT BY  
PHYSICAL DELIVERY

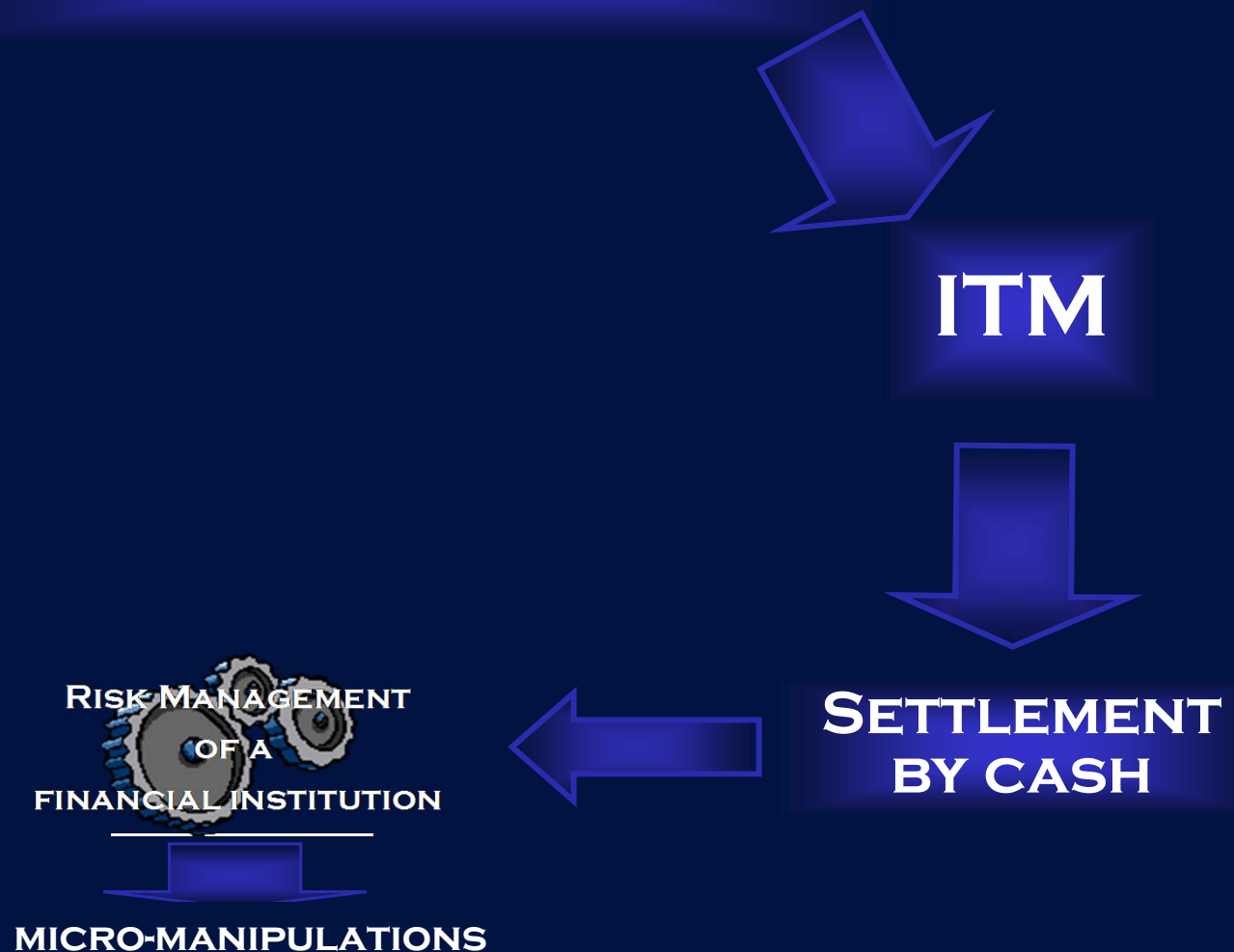
ITM



RISK MANAGEMENT  
OF A  
FINANCIAL INSTITUTION

MICRO-MANIPULATIONS

## PLAIN VANILLA



## WHY IS THERE MICRO-MANIPULATION?

FINANCIAL INSTITUTION IS A PUTS' NET BUYER





**CLOSE TO MATURITY ...**



**IT WILL HOLD**

**A LARGE AMOUNT OF**

**THE STOCKS UNDERLYING**

**THE PUT**

AT MATURITY THE OPTION IS ITM.....



IT WILL HOLD ALL THE STOCKS  
UNDERLYING THE PUTS

**IN ORDER TO SETTLE THE OPTION'S PAY-OFF ...**



**IT WILL SELL ALL THE STOCKS  
SO CALLED 'RISK UNWINDING'**

## SELLING ALL THE STOCKS ...



**IT WILL CAUSE A FALL IN PRICES  
OF THE SECURITY**

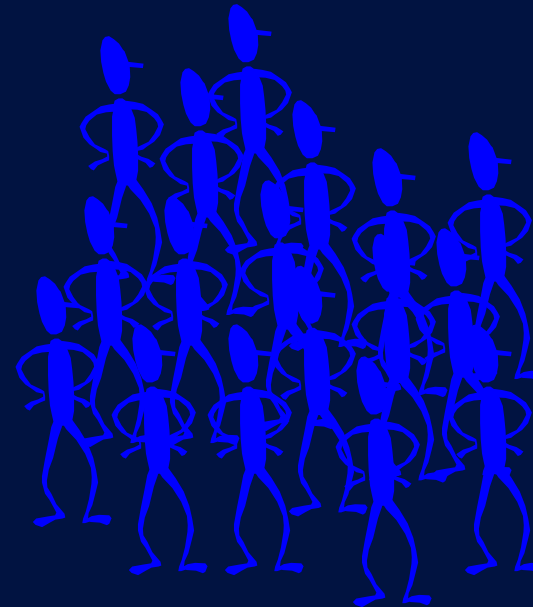
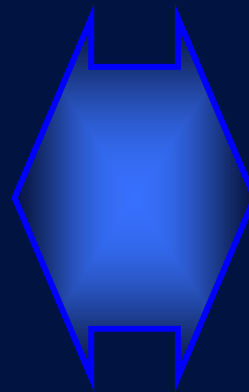
## DRIVING A FALL IN PRICES ...



IT WILL INCREASE  
THE INVESTOR'S LOSS

## A SUMMARY CONDUCTED THROUGH....

## DELTA HEDGING ANALYSIS

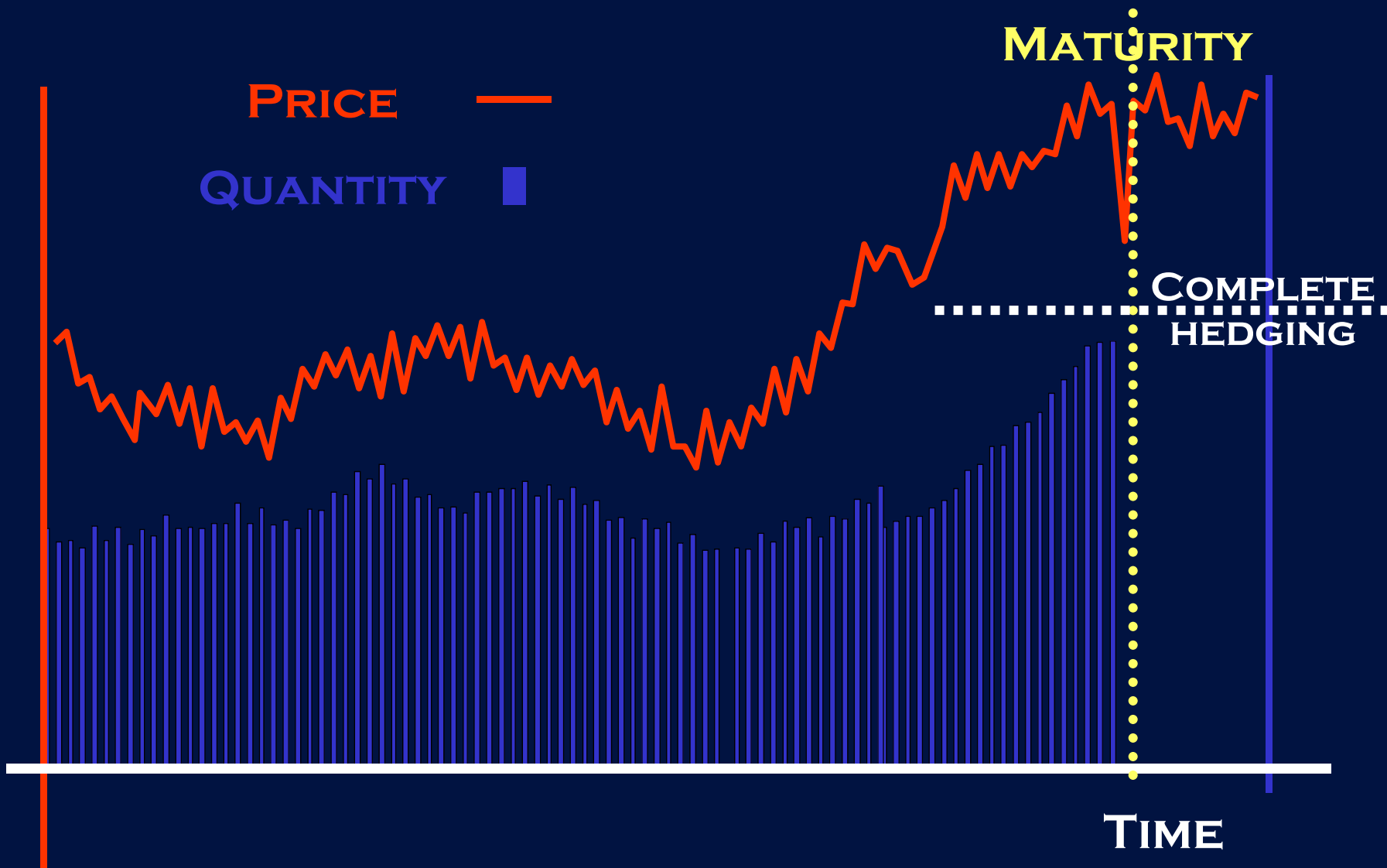


# THE POINT OF VIEW

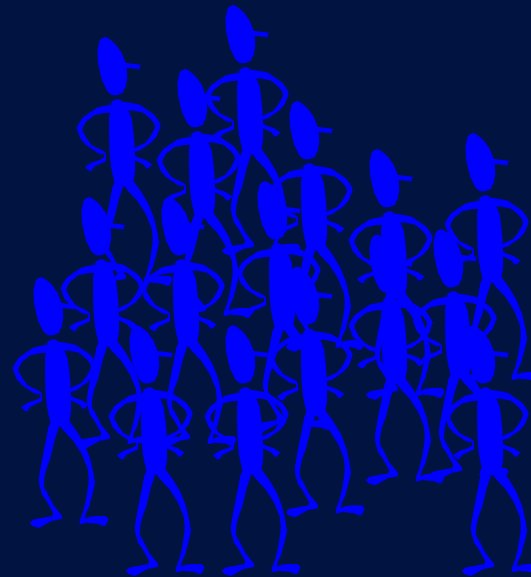


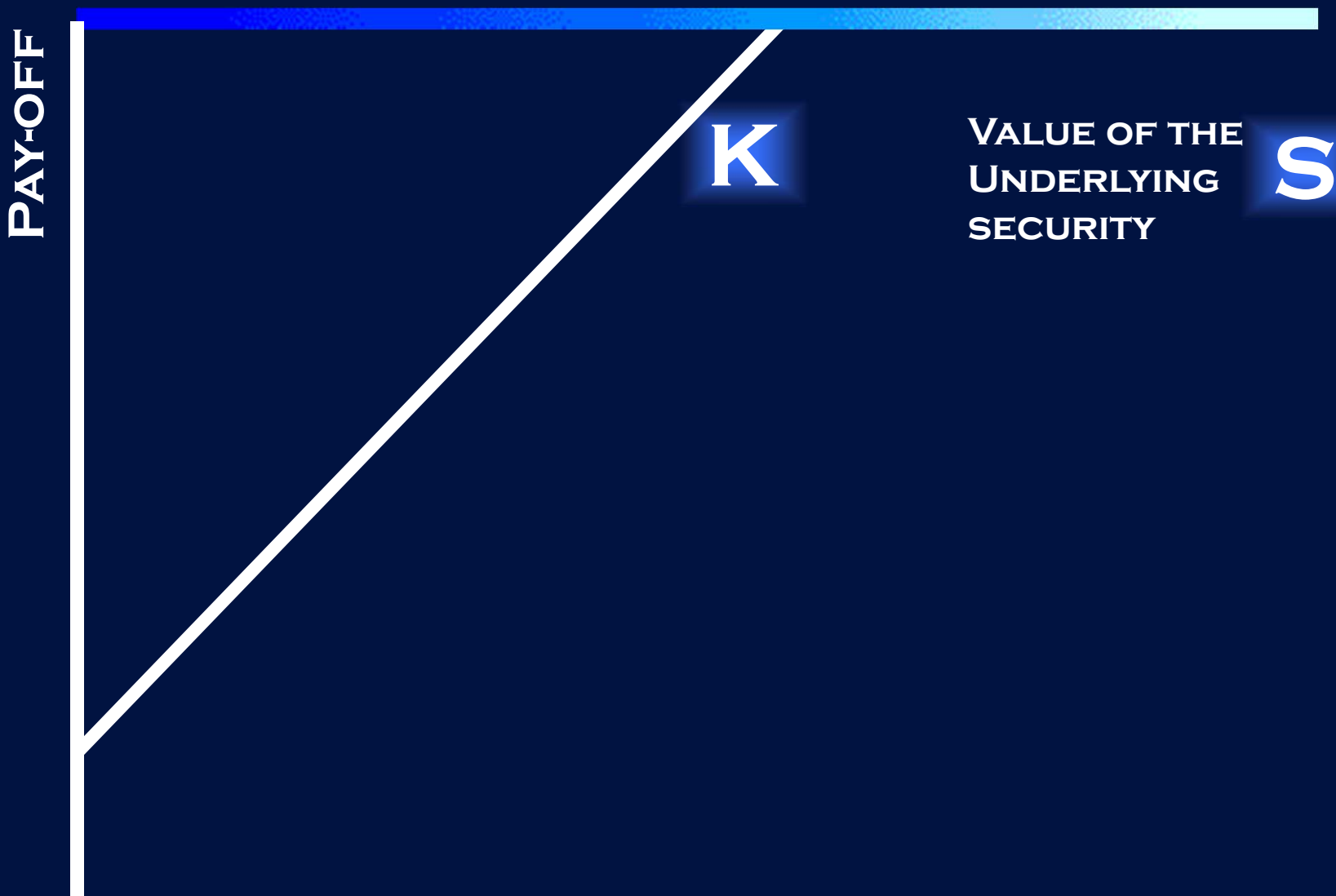


# REV.CONV. : CASE STUDIES

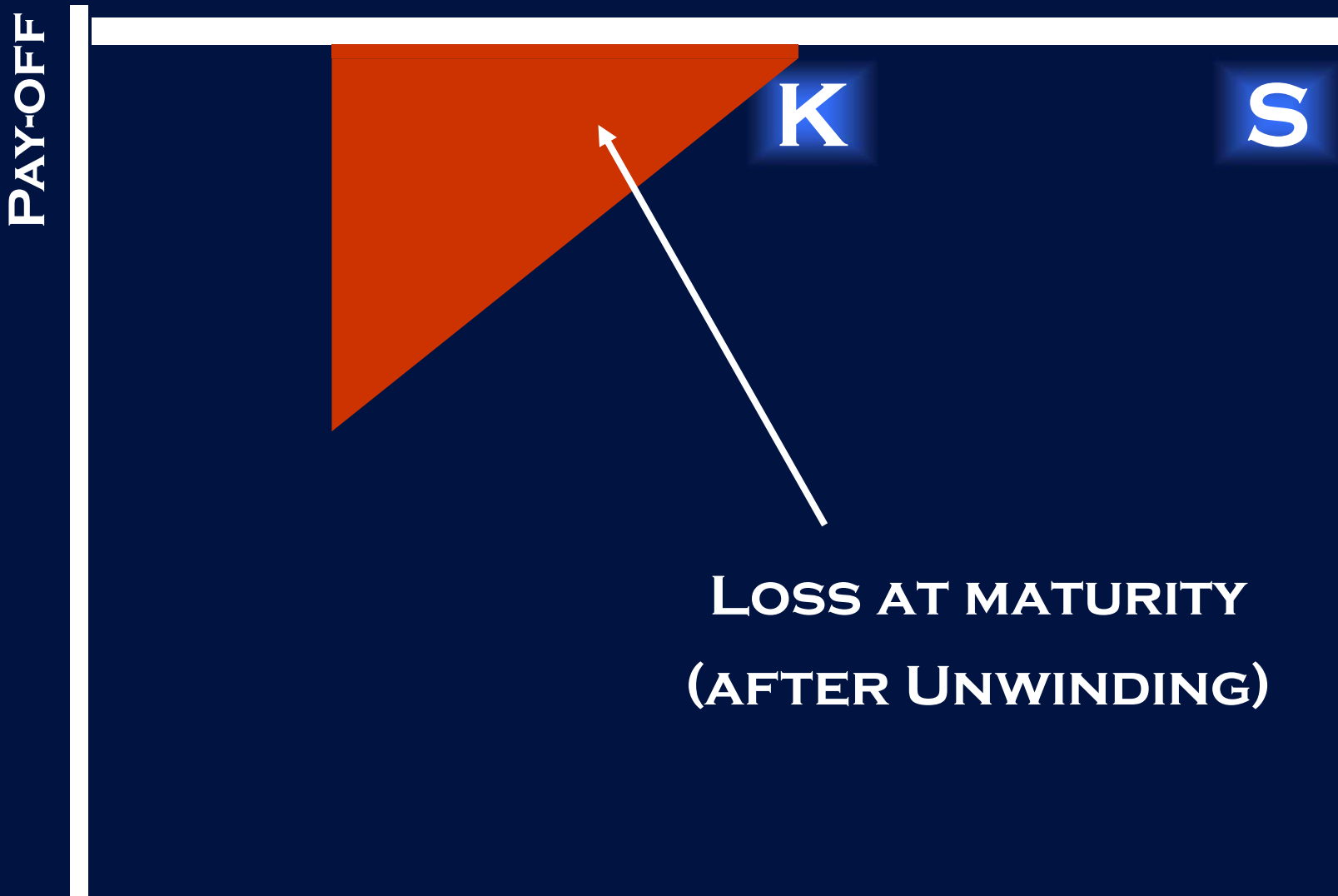


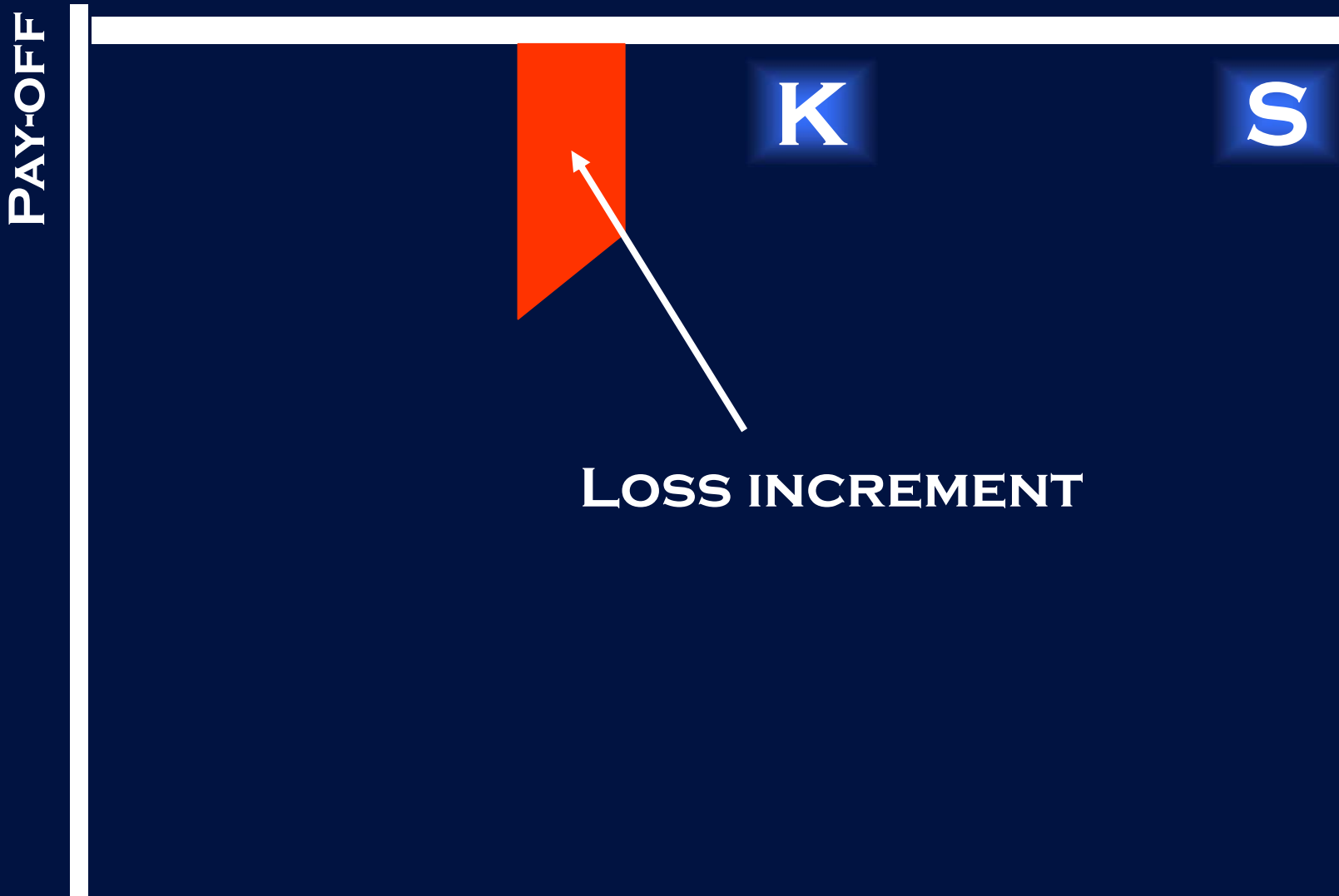
# THE POINT OF VIEW









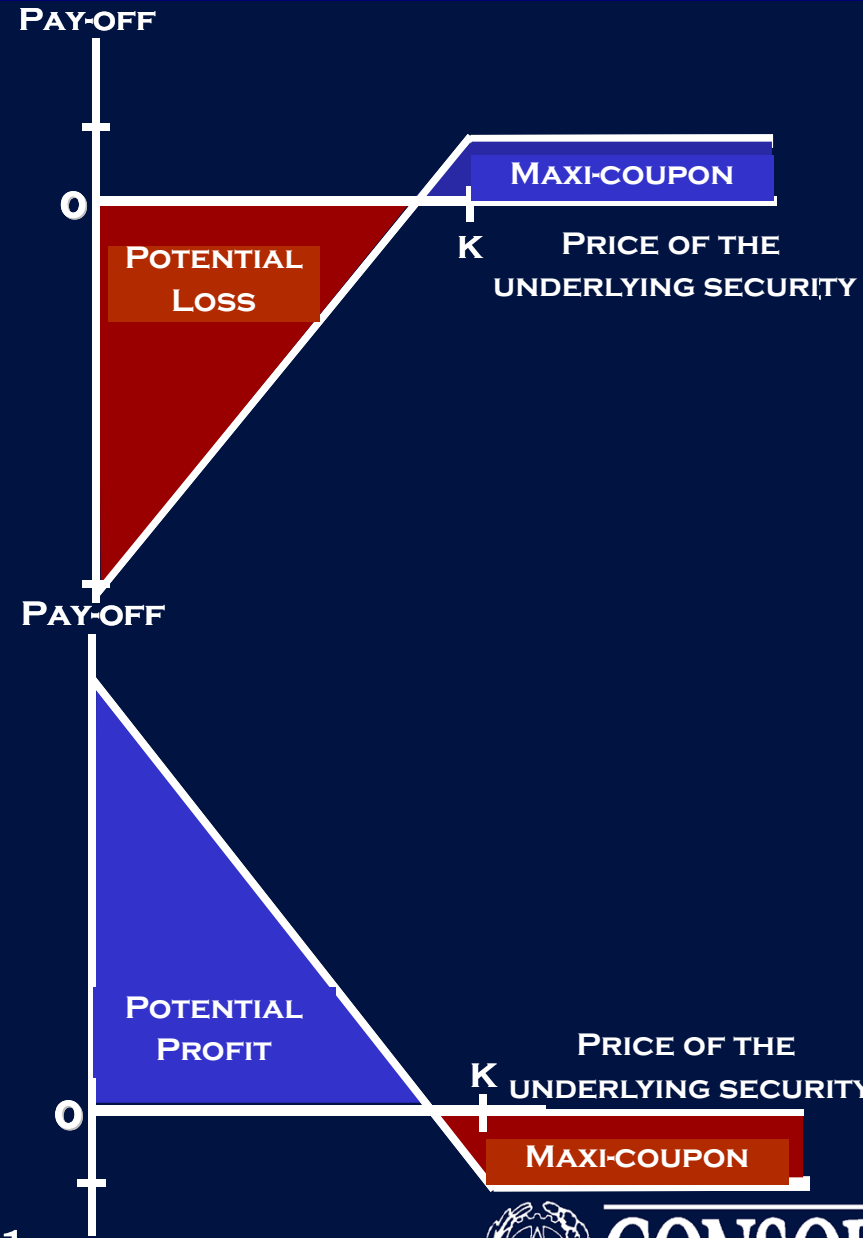


# REVERSE CONVERTIBLE

INVESTORS



ISSUER



**PLAIN VANILLA**

**ATM**

**PROBLEMS CONNECTED TO  
THE SO CALLED 'VIEW'**

**RISK MANAGEMENT  
OF A  
FINANCIAL INSTITUTION**

**MICRO-MANIPULATIONS**



**FINANCIAL INSTITUTIONS ACTS CLOSE**

**BOTH TO MATURITY AND STRIKE**



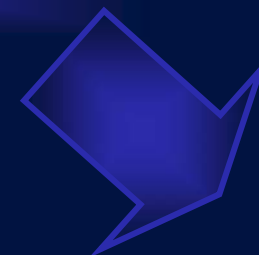
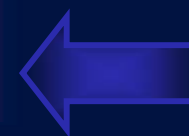
**THEY HAVE TO CHOOSE IF IT IS (OR NOT) THE  
CASE TO COMPLETE THE HEDGING ACTIVITY  
(SO CALLED VIEW)**

**VIEW**

**PURCHASE OF  
THE SECURITY**

**SETTLEMENT BY  
PHYSICAL DELIVERY**

**ITM**



## VIEW

**PURCHASE OF  
THE SECURITY**

**SETTLEMENT BY  
PHYSICAL DELIVERY**

**ITM**

**MATURITY**

**ITM**

## VIEW

PURCHASE OF  
THE SECURITY

SETTLEMENT BY  
PHYSICAL DELIVERY

ITM

MATURITY

ITM

NEUTRAL

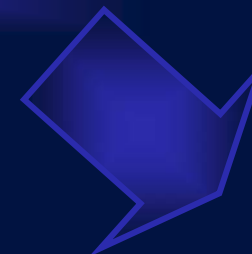
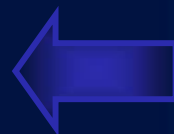
DELIVERY OF THE SECURITY

**VIEW**

**PURCHASE OF  
THE SECURITY**

**SETTLEMENT BY  
CASH**

**ITM**



## VIEW

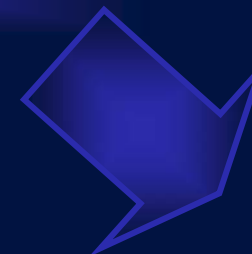
**PURCHASE OF  
THE SECURITY**

**MATURITY**

**ITM**

**SETTLEMENT BY  
CASH**

**ITM**



## VIEW

PURCHASE OF  
THE SECURITY

SETTLEMENT BY  
CASH

ITM

MATURITY

ITM

SELLING OF  
THE SECURITY

INFLUENCE ON  
PRICE

Loss

## VIEW

**PURCHASE OF  
THE SECURITY**

**SETTLEMENT BY  
CASH**

**ITM**

**MATURITY**

**ITM**

**SELLING OF  
THE SECURITY**

**INFLUENCE ON  
PRICE**

**PROFIT**

**IF**



**VIEW**

**PURCHASE OF  
THE SECURITY**

**ITM**



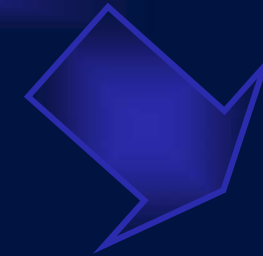
**VIEW**

**PURCHASE OF  
THE SECURITY**

**MATURITY**

**OTM**

**ITM**



## VIEW



## VIEW

**OTM**



**SELLING OF  
THE SECURITY**

## VIEW

**OTM**



**SELLING OF  
THE SECURITY**

**MATURITY**

**OTM**

## VIEW

OTM

SELLING OF  
THE SECURITY

MATURITY

OTM

NEUTRAL

## VIEW

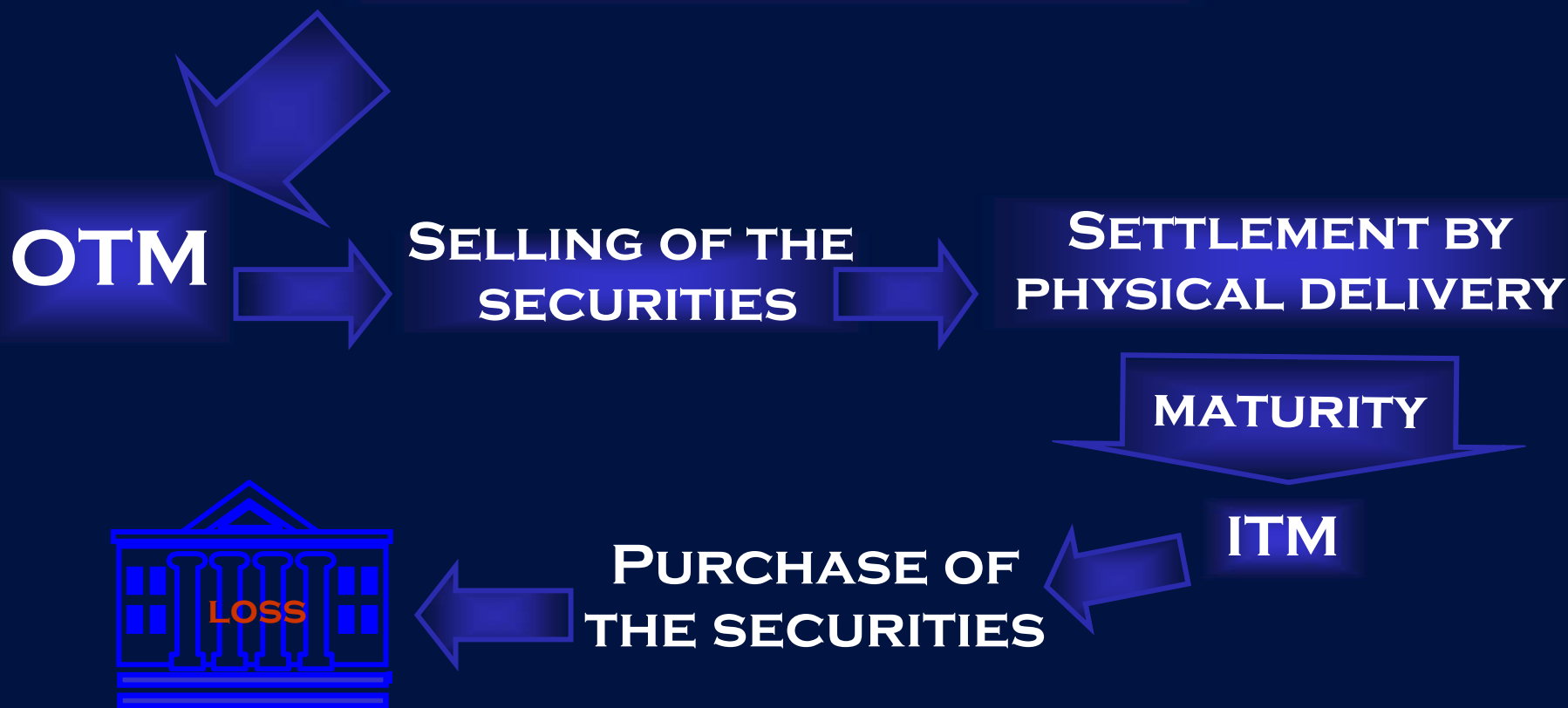


## VIEW





## VIEW



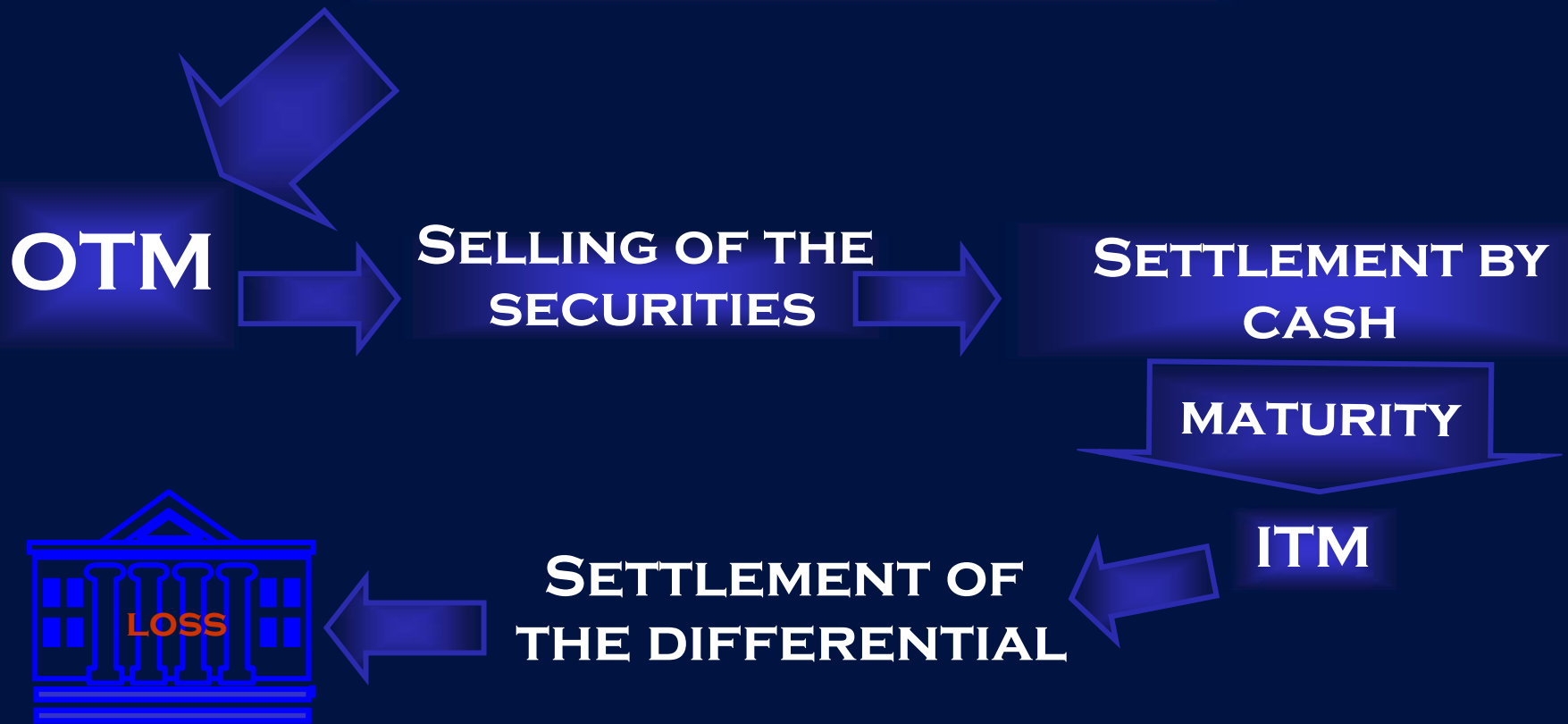
## VIEW



## VIEW

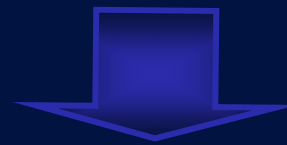


## VIEW



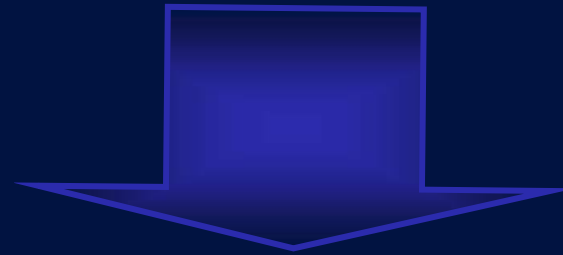
## SUMMARY

View	Expiry date	Settlement	Fin.Institution
ITM	ITM	Cash Settlement	Profit
"	"	physical delivery	Neutral
ITM	OTM	Cash Settlement	Loss
"	"	physical delivery	Loss
OTM	ITM	Cash Settlement	Loss
"	"	physical delivery	Loss
OTM	OTM	Cash Settlement	Neutral
"	"	physical delivery	Neutral



**ITM VIEW IS BETTER**

**FINANCIAL INSTITUTIONS CAN BE  
TEMPTED TO CAUSE THE *VIEW* TO  
COME TRUE**



**CASES OF MICROMANIPULATION**

# KNOCK-IN

DEF. : IT IS AN OPTION SUCH THAT WHEN A BARRIER  
IS CROSSED YOU HAVE A PLAIN VANILLA ONE

## CASES OF MICROMANIPULATION



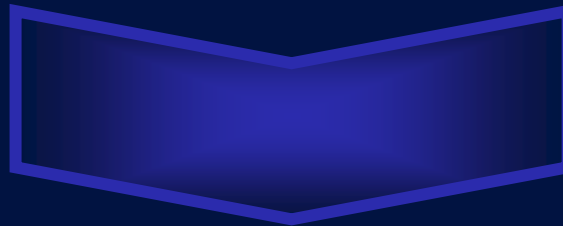
## CROSSING OF THE BARRIER



## CASES OF MICROMANIPULATION



## CROSSING OF THE BARRIER



## DEEP ITM OPTION



## KNOCK-IN



OTM

ITM

ATM



## SETTLEMENT:

- CASH
- PHYSICAL DELIVERY

... AS A CONSEQUENCE OF WHAT HAVE BEEN  
SAID BEFORE, WE WILL OMIT THE

**KNOCK-IN**

**OTM**

**ATM**

**ITM**

**CROSS-REFERENCE**

SEE WHAT HAVE BEEN SAID ABOUT  
PLAIN VANILLA OPTIONS

... LET US FOCUS ON

**KNOCK-IN**

```
graph TD; A[KNOCK-IN] --> B[OTM]; A --> C[ATM]; A --> D[ITM]
```

**OTM**

**ATM**

**ITM**

**KNOCK-IN**



**OTM**

**... WE DISTINGUISH**

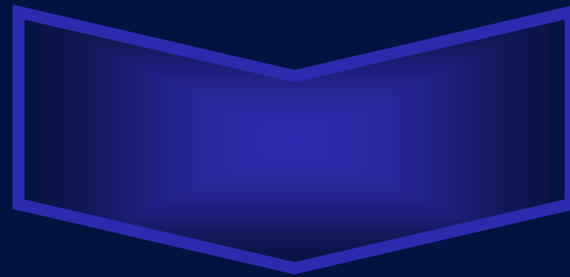


**... CLOSE TO THE  
BARRIER**

**...NOT CLOSE TO THE  
BARRIER**

## INTRODUCTION:

### RISK MANAGEMENT FOR A KNOCK-IN OPTION



## NUMERIC GREEK LETTERS

## NUMERIC GREEK LETTERS



**MISTAKES IN CASE OF CLOSENESS  
TO THE BARRIER**

**LET US RECALL WHAT A NUMERIC**

**GREEK LETTER IS**

$$\Delta = \frac{1}{2}(\Delta_{+1\%} + \Delta_{-1\%})$$

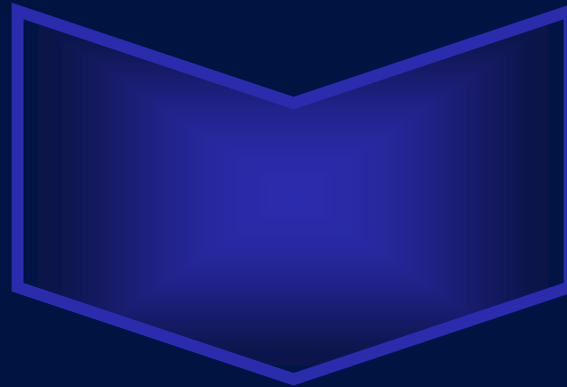
$$\Gamma = \frac{1}{2}(\Gamma_{+1\%} + \Gamma_{-1\%})$$

$$v = \frac{1}{2}(v_{+1\%} + v_{-1\%})$$

**... LET US OMIT THE OTHERS BECAUSE THEY ARE NOT VERY IMPORTANT**



**WHY DOES IT LEAD TO A MISTAKE?**



**BECAUSE IT COMPARES  
DISOMOGENEOUS QUANTITIES**

## EXAMPLE:

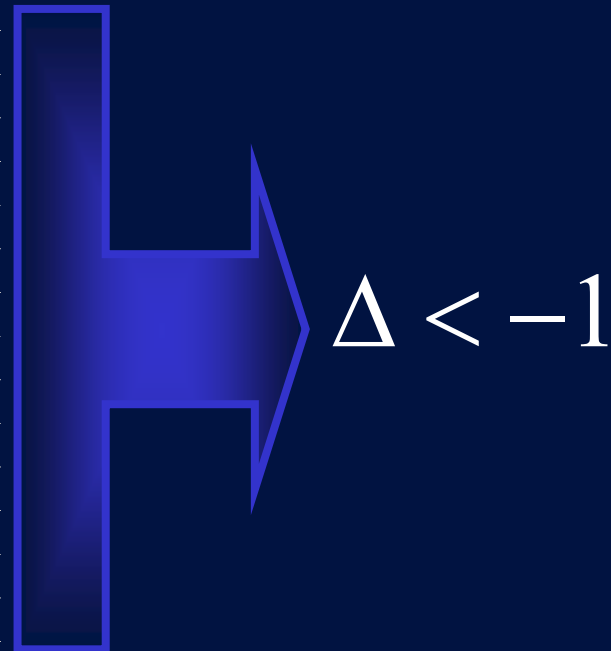
**CLOSE (1%) TO THE BARRIER  
THE FORMULA BECOMES:**

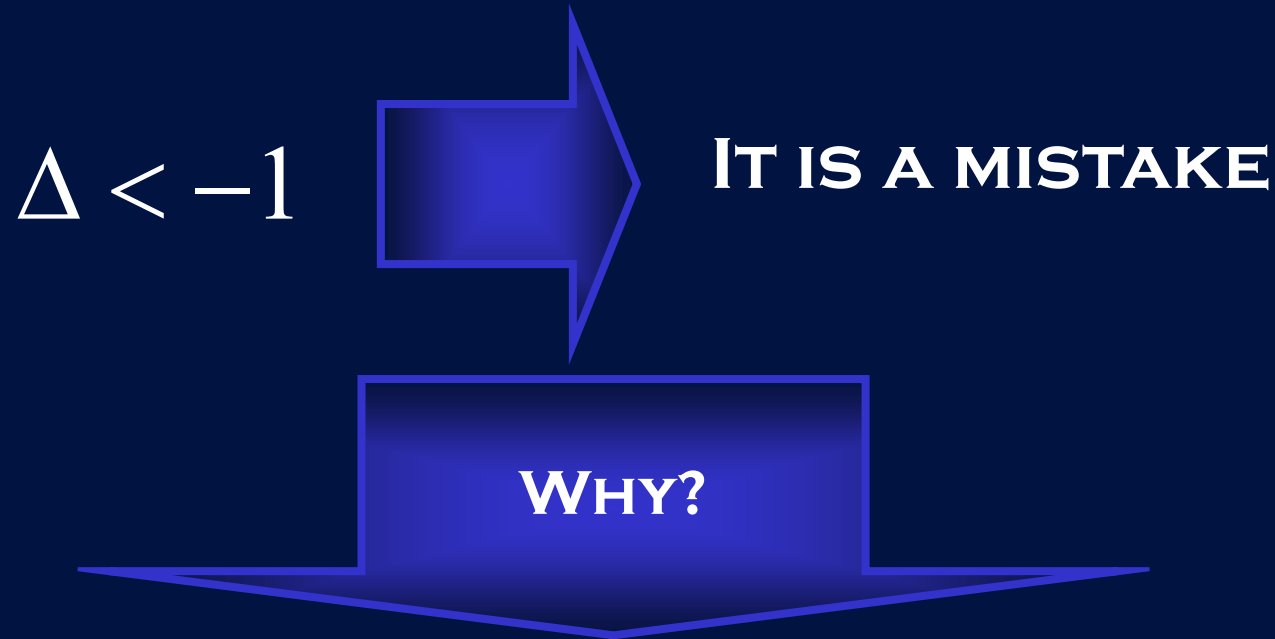
$$\Delta = \frac{1}{2} \left( \Delta^{+1\%} - \Delta^{-1\%} \right)$$

$$\Delta^{\pm 1\%} = \frac{P_{plain-vanilla}^1 - P_{Knock-in}^0}{S^{\pm 1\%} - S^0}$$

# REV.CONV. : CASE STUDIES

K	H	
32,76	21,90	
price	put	$\Delta$ numeric
22,600	8,410	-326%
22,550	8,574	-328%
22,500	8,738	-330%
22,450	8,904	-332%
22,400	9,071	-334%
22,350	9,238	-335%
22,300	9,407	-337%
22,250	9,576	-338%
22,200	9,745	-340%
22,150	9,916	-341%
22,100	10,086	-329%
22,050	10,258	-303%
22,000	10,429	-276%
21,950	10,601	-248%
21,900	10,771	-221%
21,850	10,821	-193%
21,800	10,870	-165%
21,750	10,920	-137%
21,700	10,970	-109%
21,650	11,020	-100%
21,600	11,070	-100%
21,550	11,120	-100%
21,500	11,170	-100%
21,450	11,220	-100%





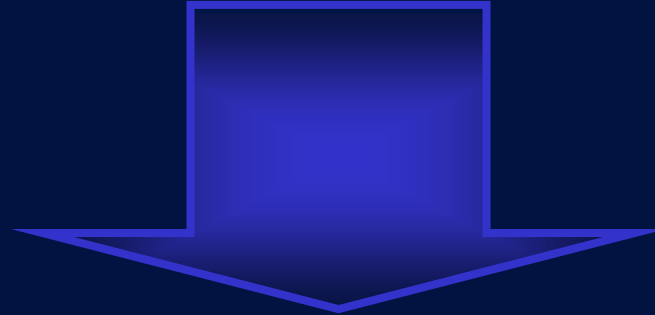
**BECAUSE IT COMPARES  
DIFFERENT CONTINGENT CLAIMS**

**RISK MANAGEMENT BASED ON  
GREEK LETTERS REFERRED TO  
THE BARRIER OPTIONS**



**MISLEADING**

**... FURTHERMORE, IT CAN BE VERY EXPANSIVE**



**BECAUSE IT CAN REQUIRE BOTH CONTINUOUS  
AND RELEVANT PORTFOLIO REBALANCES**

## EXAMPLE:

<b>K</b>	<b>H</b>	
32,76	21,90	
<b>price</b>	<b>put</b>	<b><math>\Delta</math> numeric</b>
22,150	9,916	-341%
21,950	10,601	-248%
22,200	9,745	-340%
21,910	10,739	-226%
22,000	10,429	-276%
22,050	10,258	-303%
21,920	10,704	-232%

# REV.CONV. : CASE STUDIES

K	H	
32,76	21,90	
price	put	$\Delta$ numeric
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22,450	8,904	-332%
22,400	9,071	-334%
22,350	9,238	-335%
22,300	9,407	-337%
22,250	9,576	-338%
22,200	9,745	-340%
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21,850	10,821	-193%
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21,750	10,920	-137%
21,700	10,970	-109%
21,650	11,020	-100%
21,600	11,070	-100%
21,550	11,120	-100%
21,500	11,170	-100%
21,450	11,220	-100%



$$\Delta < -1$$

K	H	
32,76	21,90	

## PORTAFOGLIO RE-BALANCING

21,910	10,739	-226%
22,000	10,429	-276%
22,050	10,258	-303%
21,920	10,704	-232%

**FINANCIAL INSTITUTIONS DO NOT EMPLOY  
TRADITIONAL  $\Delta$  HEDGING,  
BUT THEY USE SOME DEVICES,  
AT LEAST IN CASE OF CLOSENESS TO THE BARRIER**



## DEVICES:

- LET US FIX THE MAXIMUM FLUCTUATION OF  $\Delta$  TO  $-1$
- LET US USE  $\Theta$  IN ORDER TO REDUCE THE VALUE OF  $\Delta$

... **NOT** CLOSE TO THE BARRIER



△ HEDGING WORKS WELL

... **NOT** CLOSE TO THE BARRIER



$\Delta$  HEDGING WORKS WELL



WHY?

BECAUSE IT COMPARES CONTINGENT  
CLAIMS THAT ARE EQUAL

## EXAMPLE:

THE FORMULA BECOMES:

$$\Delta = \frac{1}{2} \left( \Delta^{+1\%} - \Delta^{-1\%} \right)$$

$$\Delta^{\pm 1\%} = \frac{P_{Knock-in}^1 - P_{Knock-in}^0}{S^{\pm 1\%} - S^0}$$

**MARKET MANIPULATION TARGETED  
TO CROSS THE BARRIER**



**VERY EXPANSIVE**

***WARNING IN THE  
RISK MANAGEMENT***

## CLOSE TO THE BARRIER



**ADJUSTED  $\Delta$  HEDGING WORKS WELL**

MARKET MANIPULATION TARGETED  
TO CROSS THE BARRIER



NOT EXPANSIVE

NO WARNING IN THE  
RISK MANAGEMENT

**MARKET MANIPULATION TARGETED  
TO CROSS THE BARRIER**



**NOT EXPANSIVE**

**NO WARNING IN THE  
RISK MANAGEMENT**

**THE FINANCIAL INSTITUTION COULD  
BE TEMPTED TO CROSS THE BARRIER**



**... BUT IT IS NOT SURE THAT THE FINANCIAL  
INSTITUTION WILL ADOPT AN ADJUSTED  
GREEK HEDGING SYSTEM**

**... BUT IT IS NOT SURE THAT THE FINANCIAL  
INSTITUTION WILL ADOPT AN ADJUSTED  
GREEK HEDGING SYSTEM**



**... IF FOLLOWING THE TRADITIONAL  
HEDGING, CLOSE TO THE BARRIER,  
ALLOWS THE RISK MANAGEMENT  
TO OBTAIN “POSITIVE” EFFECTS**

**... BECAUSE AFTER HAVING REALIZED THAT  
THE ACTIVITY CLOSE TO THE BARRIER  
LEADS TO AN OVER-HEDGING, THE FINANCIAL  
INSTITUTION DISINVESTS THE PART IN EXCESS  
BY SELLING SECURITIES**

**... BECAUSE AFTER HAVING REALIZED THAT  
THE ACTIVITY CLOSE TO THE BARRIER  
LEADS TO AN OVER-HEDGING, THE FINANCIAL  
INSTITUTION DISINVESTS THE PART IN EXCESS  
BY SELLING SECURITIES**



**... AND THIS SELLING ACTIVITY CAN CAUSE A  
FALL IN PRICE AND A BARRIER CROSSING**

# REV.CONV. : CASE STUDIES

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21,500	11,170	-100%
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$$\Delta < -1$$

K	H	
32,76	21,90	

## PORTAFOGLIO RE-BALANCING

21,910	10,739	-226%
22,000	10,429	-276%
22,050	10,258	-303%
21,920	10,704	-232%

**THE FINANCIAL INSTITUTION RESTORES THE  
 $\Delta$  HEDGING AT ITS MAXIMUM VALUE (-1)  
AND SELLS THE SECURITIES IN EXCESS**

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21,450	11,220	-100%



$$\Delta < -1$$

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32,76	21,90	

## PORTAFOGLIO RE-BALANCING

21,910	10,739	-226%
22,000	10,429	-276%
22,050	10,258	-303%
21,920	10,704	-232%

**THE FINANCIAL INSTITUTION RESTORES THE  $\Delta$  HEDGING AT ITS MAXIMUM VALUE (-1) AND SELLS THE SECURITIES IN EXCESS**



**... BEING CLOSE TO THE BARRIER THE FINANCIAL INSTITUTION CAN REACH THE TARGET TO CROSS IT**

... AND WHAT HAS BEEN SAID BEFORE, HAPPENS IN AN  
APPARENT SITUATION OF CORRECTIVENESS

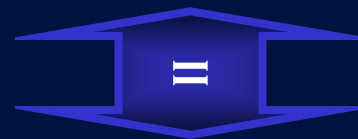


... FOR THE **KNOCK-IN** OPTIONS ...

... FOR THE KNOCK-IN OPTIONS ...



**NOT** CORRECT  
RISK MANAGEMENT



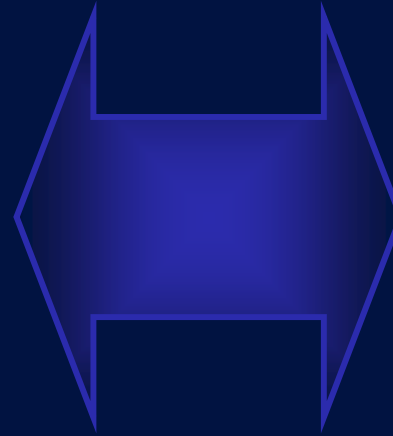
**NOT** CORRECT  
FINANCIAL INSTITUTION



# HEDGING OF A FINANCIAL INSTITUTION

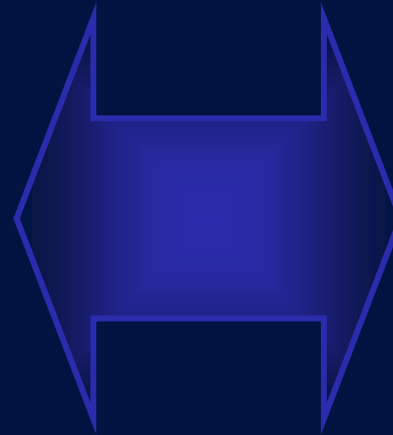
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**RISK MANAGEMENT  
OF A FINANCIAL  
INSTITUTION**



**COVERED  
WARRANT**

**RISK MANAGEMENT  
OF A FINANCIAL  
INSTITUTION**



**REVERSE  
CONVERTIBLE**

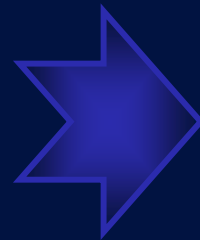
**PLAIN-VANILLA  
OPTIONS**

**COVERED  
WARRANT**

## AFTER BUYING ...

**AFTER BUYING ...**

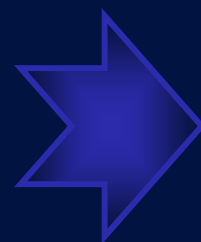
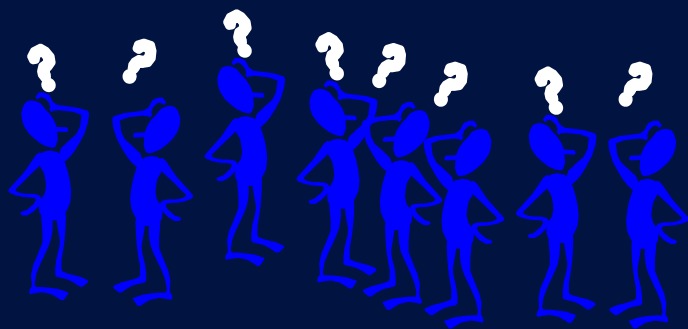
**WHAT TO DO?**



**LET US  
NEGOTIATE**

**AFTER BUYING ...**

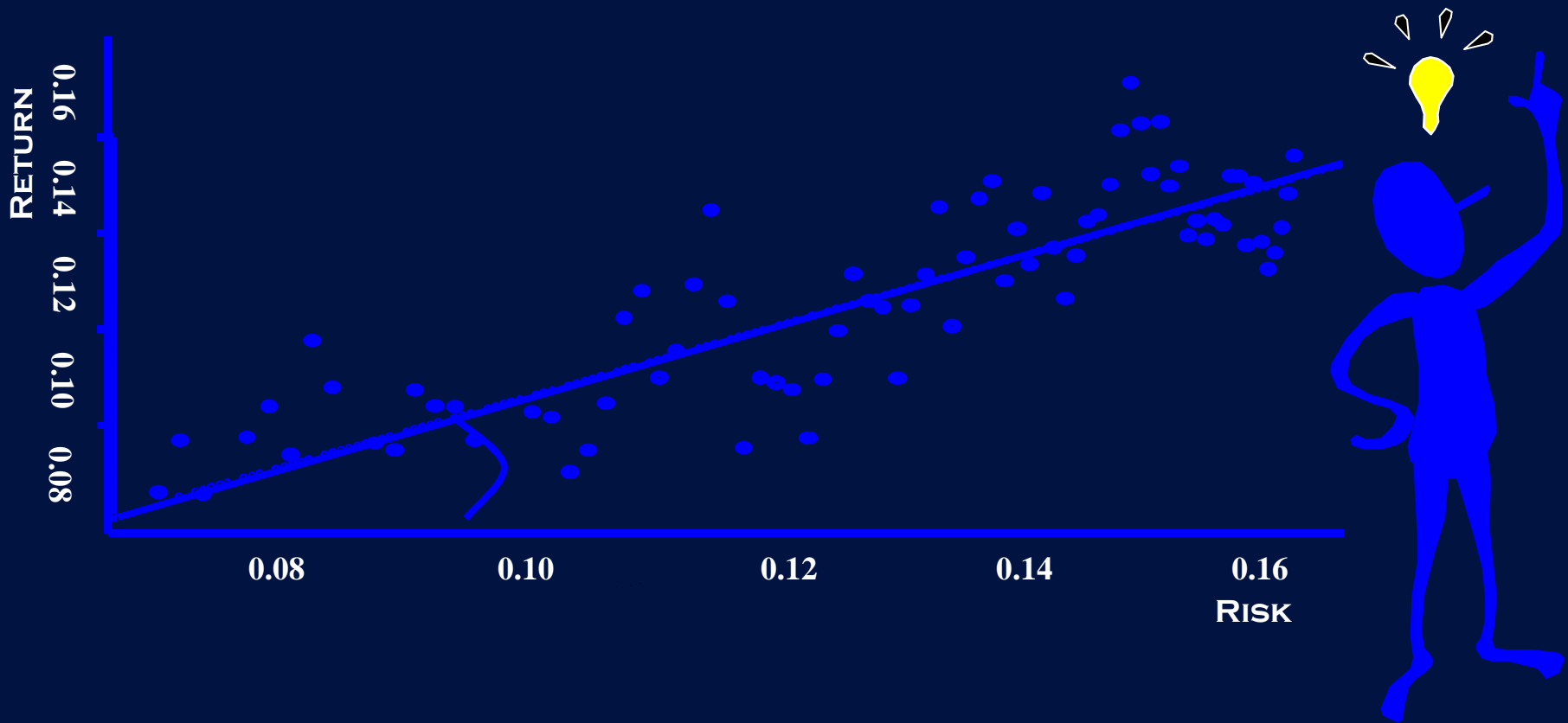
**WHAT TO DO?**



**LET US WAIT FOR  
THE MATURITY**

# COVERED WARRANT – WHAT TO DO AFTER?

IT DEPENDS FROM INDIVIDUAL RISK – RETURN PREFERENCES



# COVERED WARRANT – WHAT TO DO AFTER?

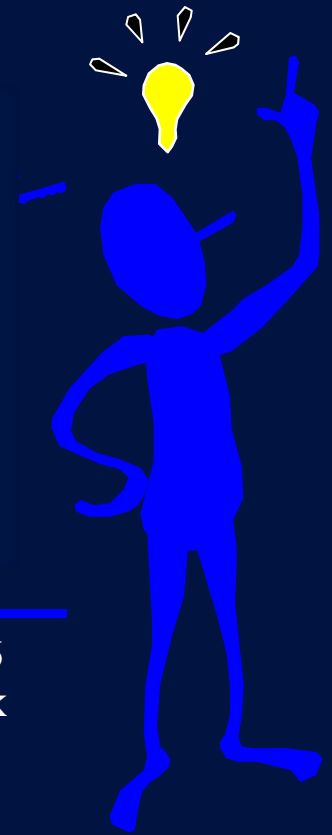
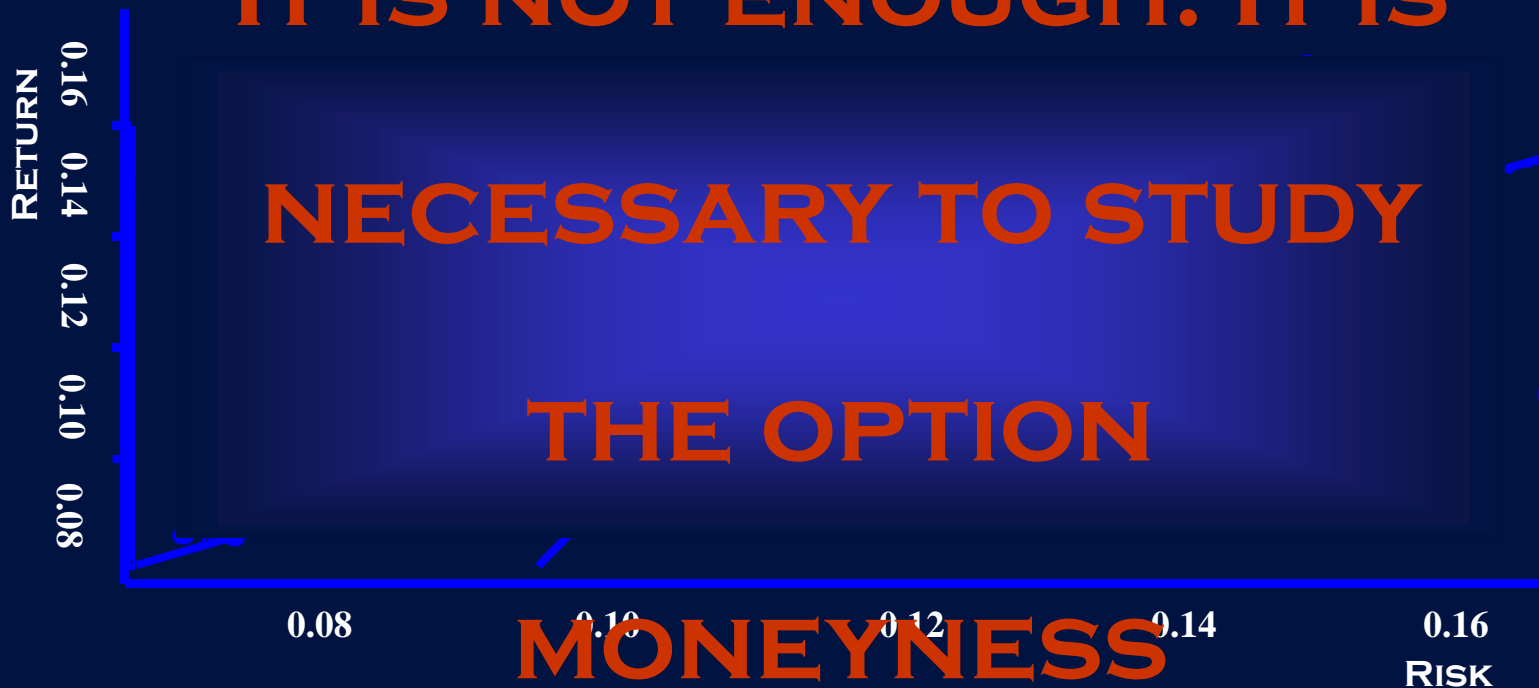
IT DEPENDS FROM INDIVIDUAL RISK – RETURN PREFERENCES

**IT IS NOT ENOUGH. IT IS**

**NECESSARY TO STUDY**

**THE OPTION**

**MONEYNESS**



# COVERED WARRANT – WHAT TO DO AFTER?

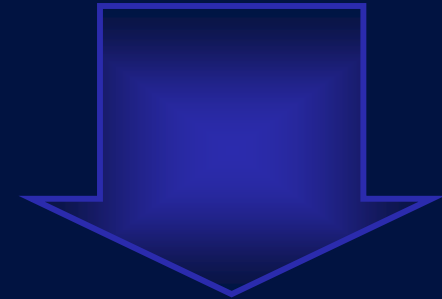
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CW IN-THE-MONEY   CW AT-THE-MONEY   CW OUT-THE-MONEY





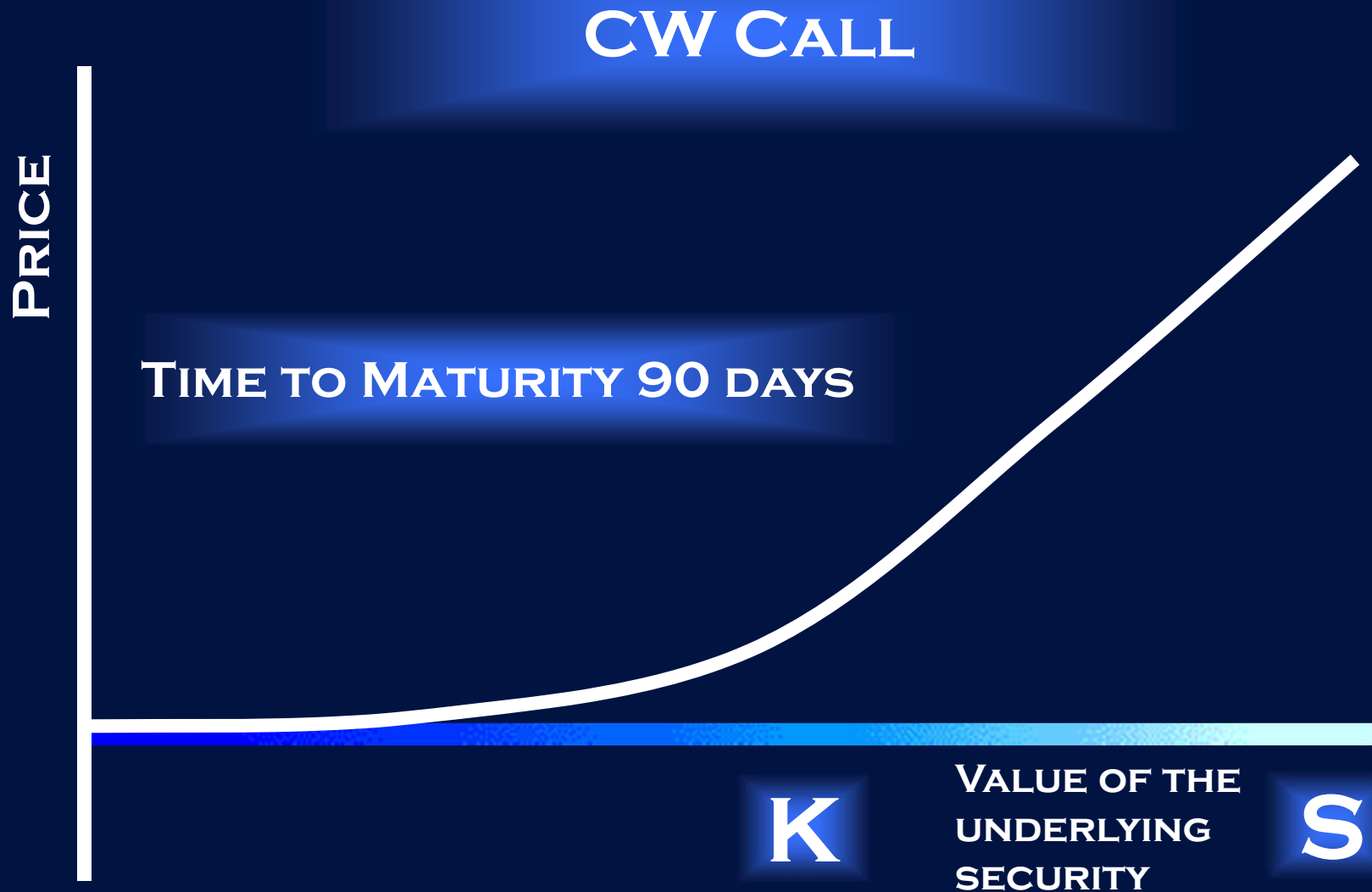
**CW OUT-THE-MONEY**



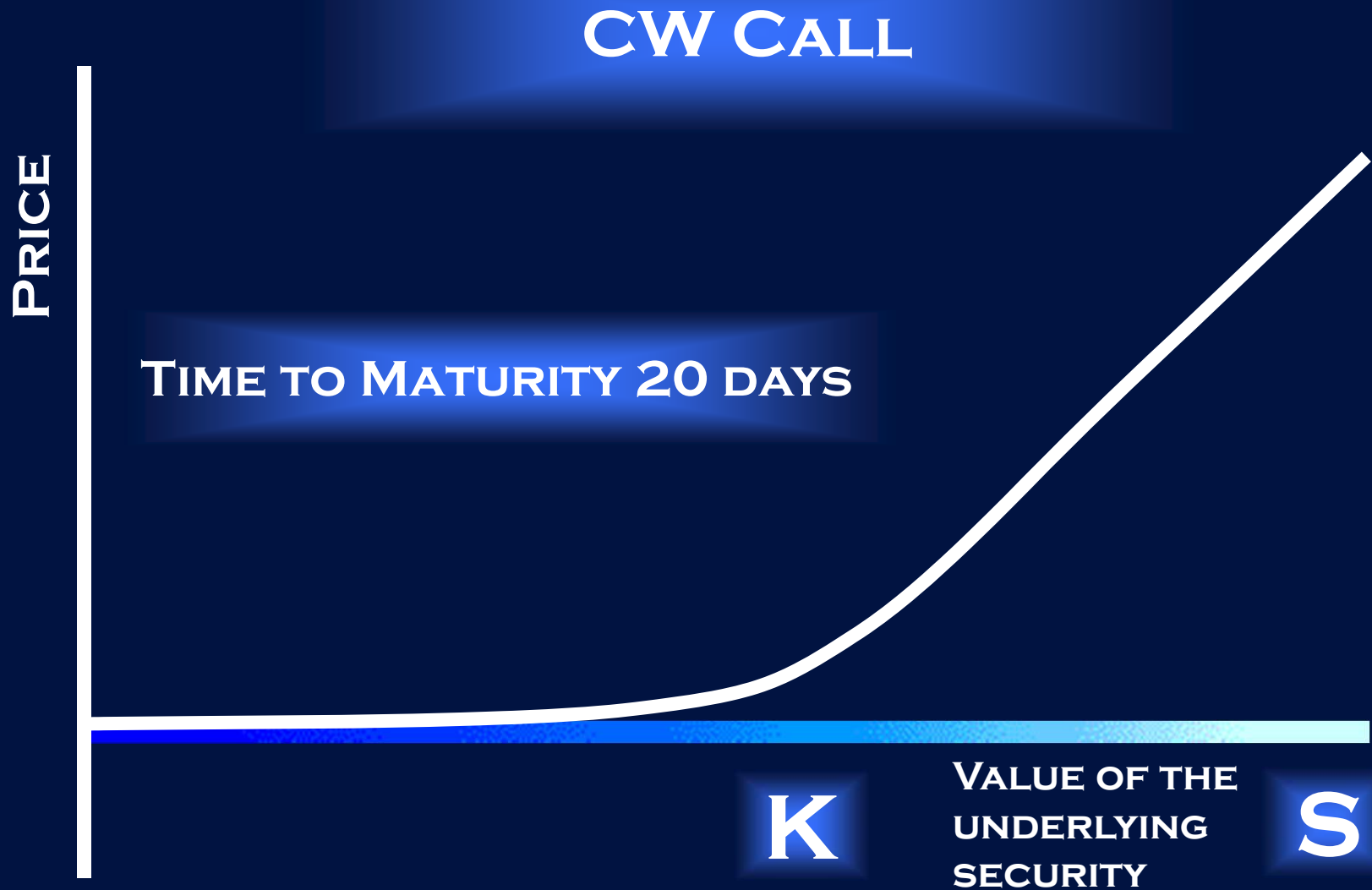
**PROBLEMS OF THE  
MINIMUM TICK WITH  
REGARD TO THE  
TRADING  
INSTRUMENTS**



# CW OUT-THE-MONEY – WHAT TO DO AFTER?

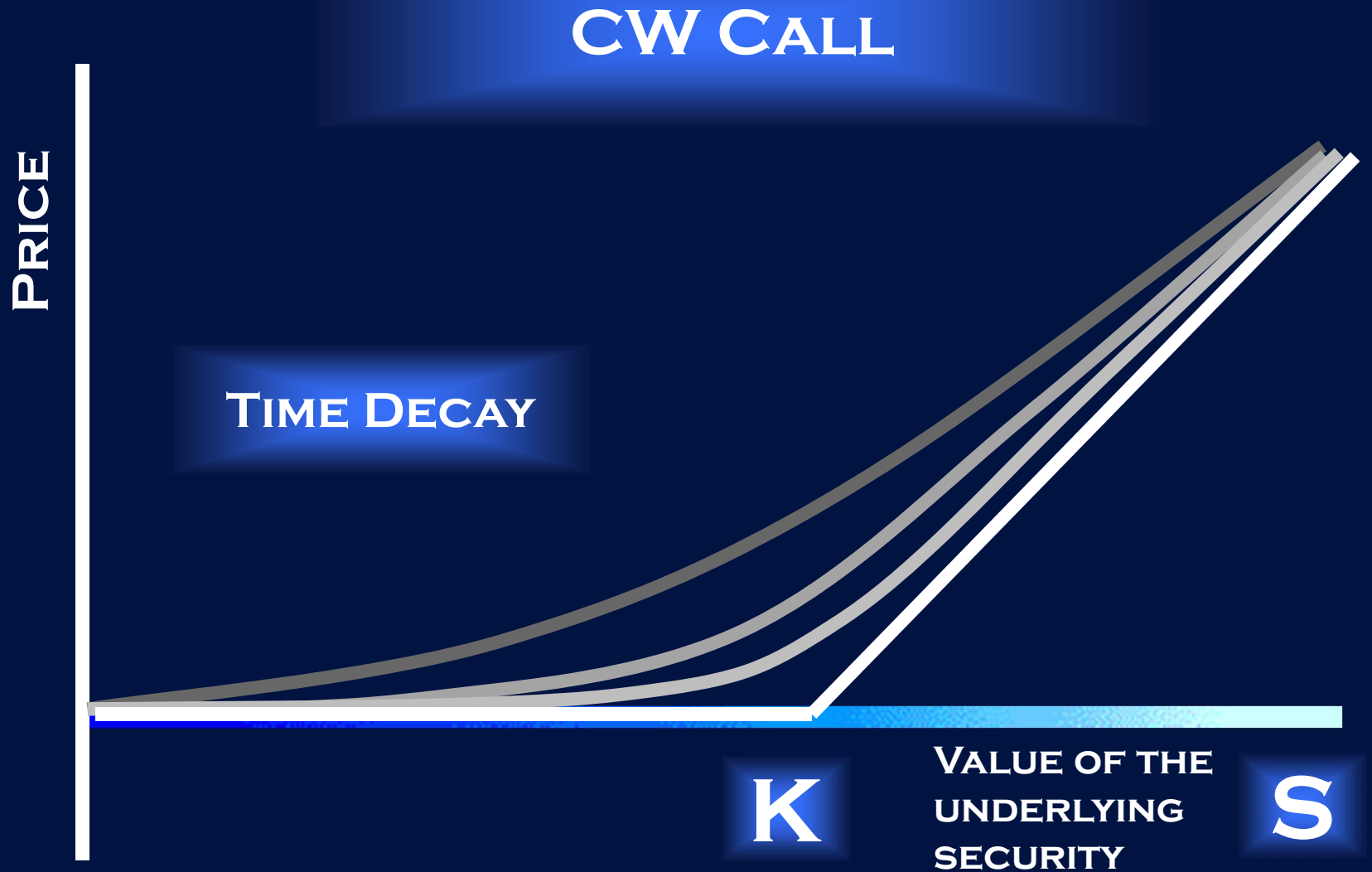


# CW OUT-THE-MONEY – WHAT TO DO AFTER?



# CW OUT-THE-MONEY – WHAT TO DO AFTER?



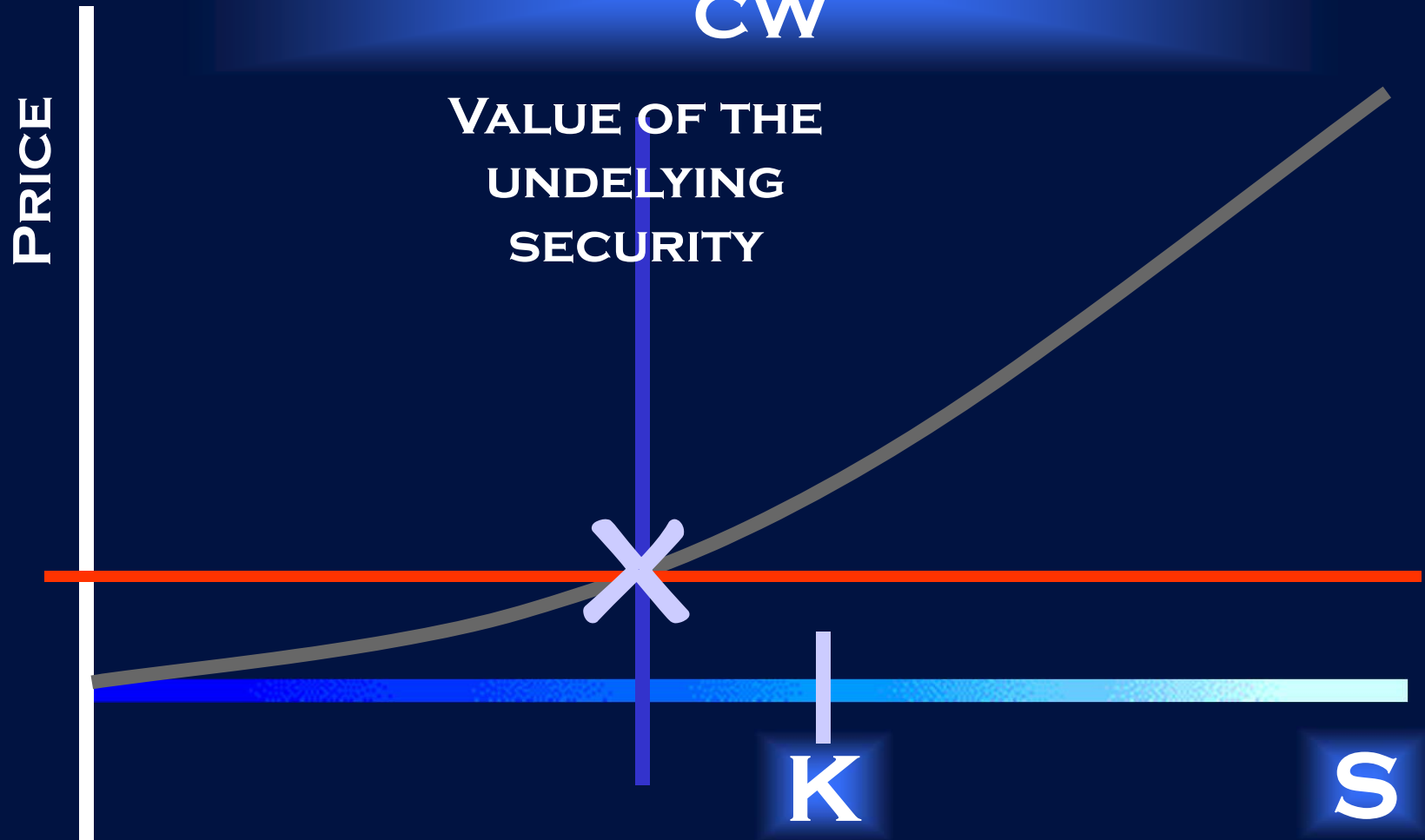


## CW CALL



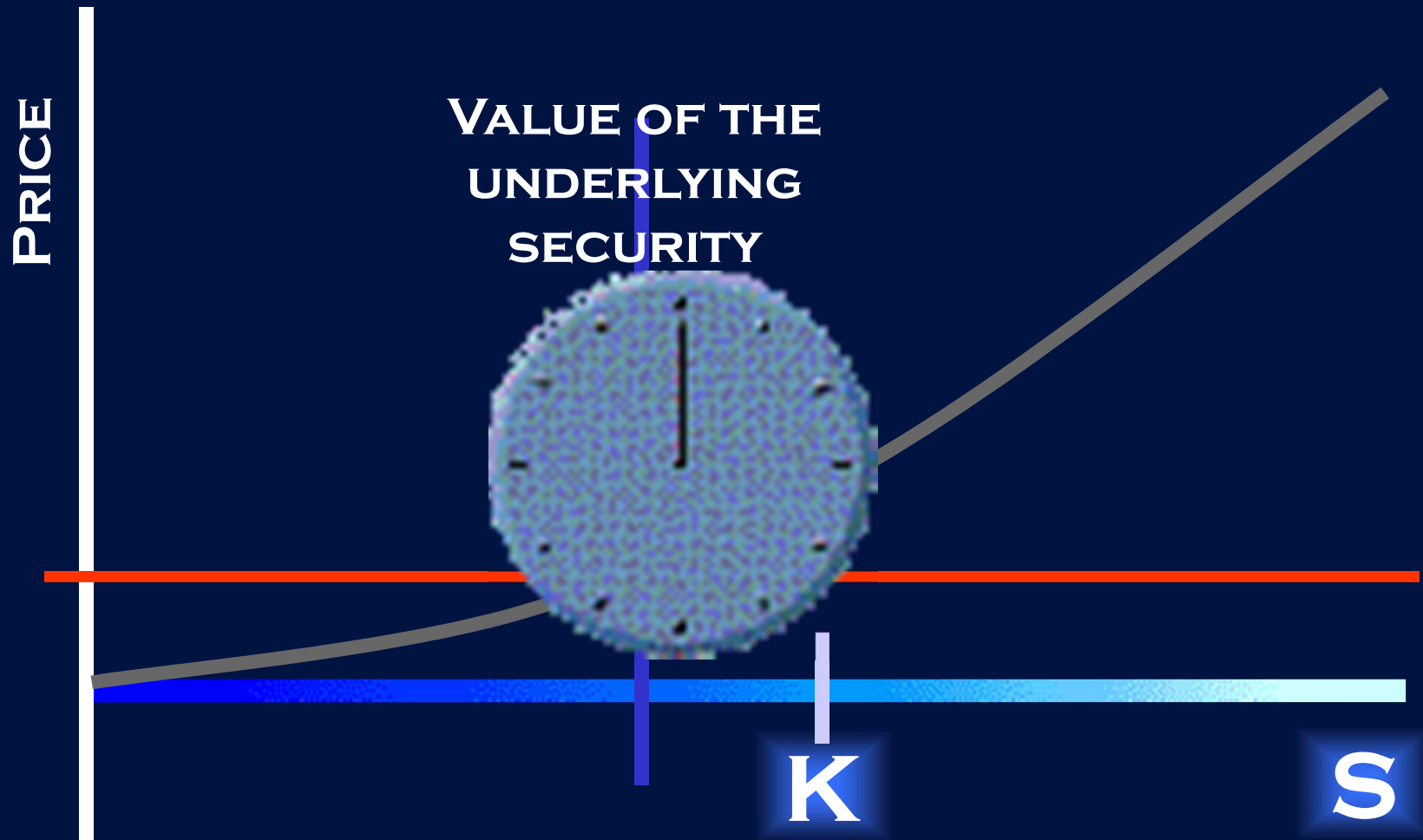
# PURCHASE OF AN OTM CALL

CW

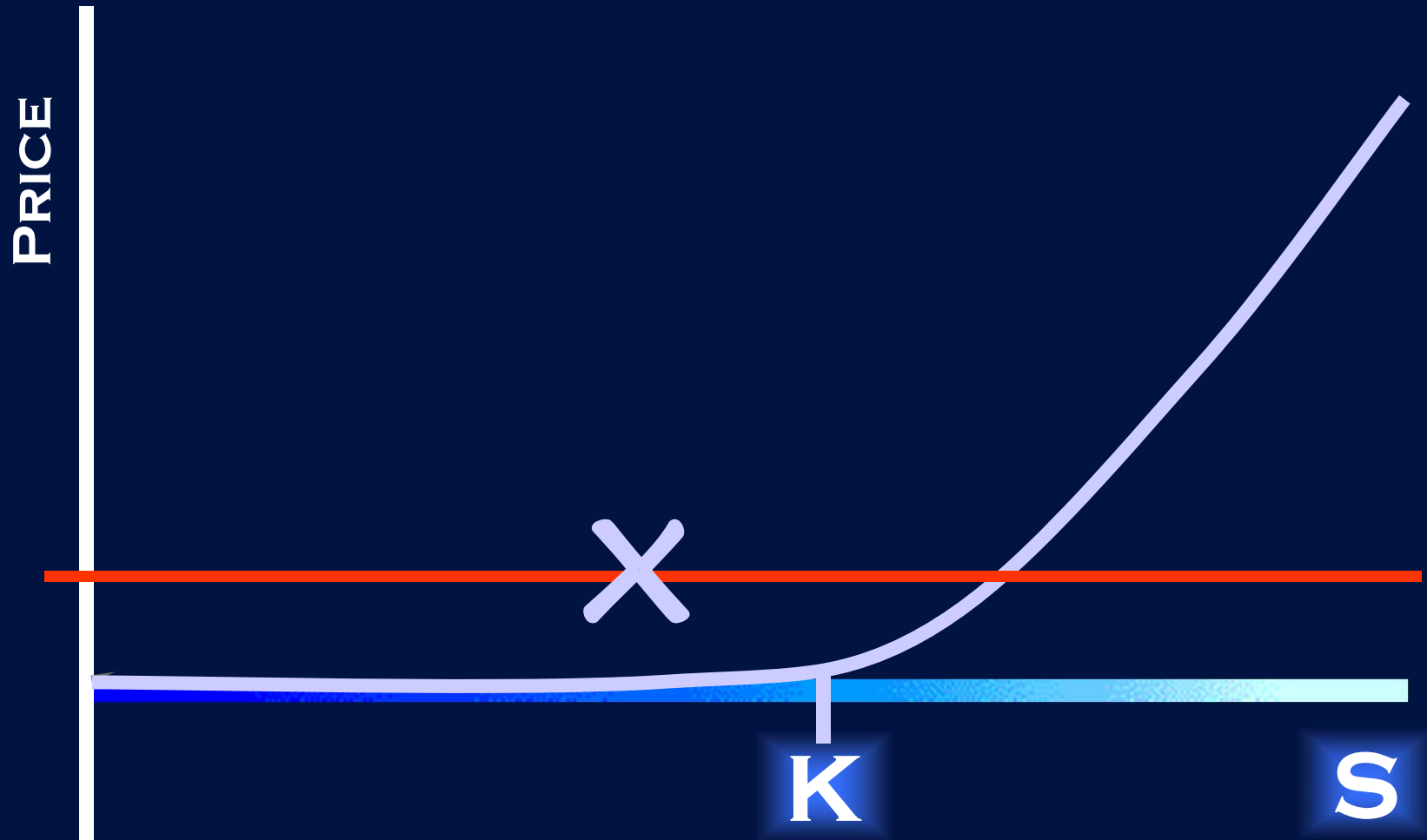




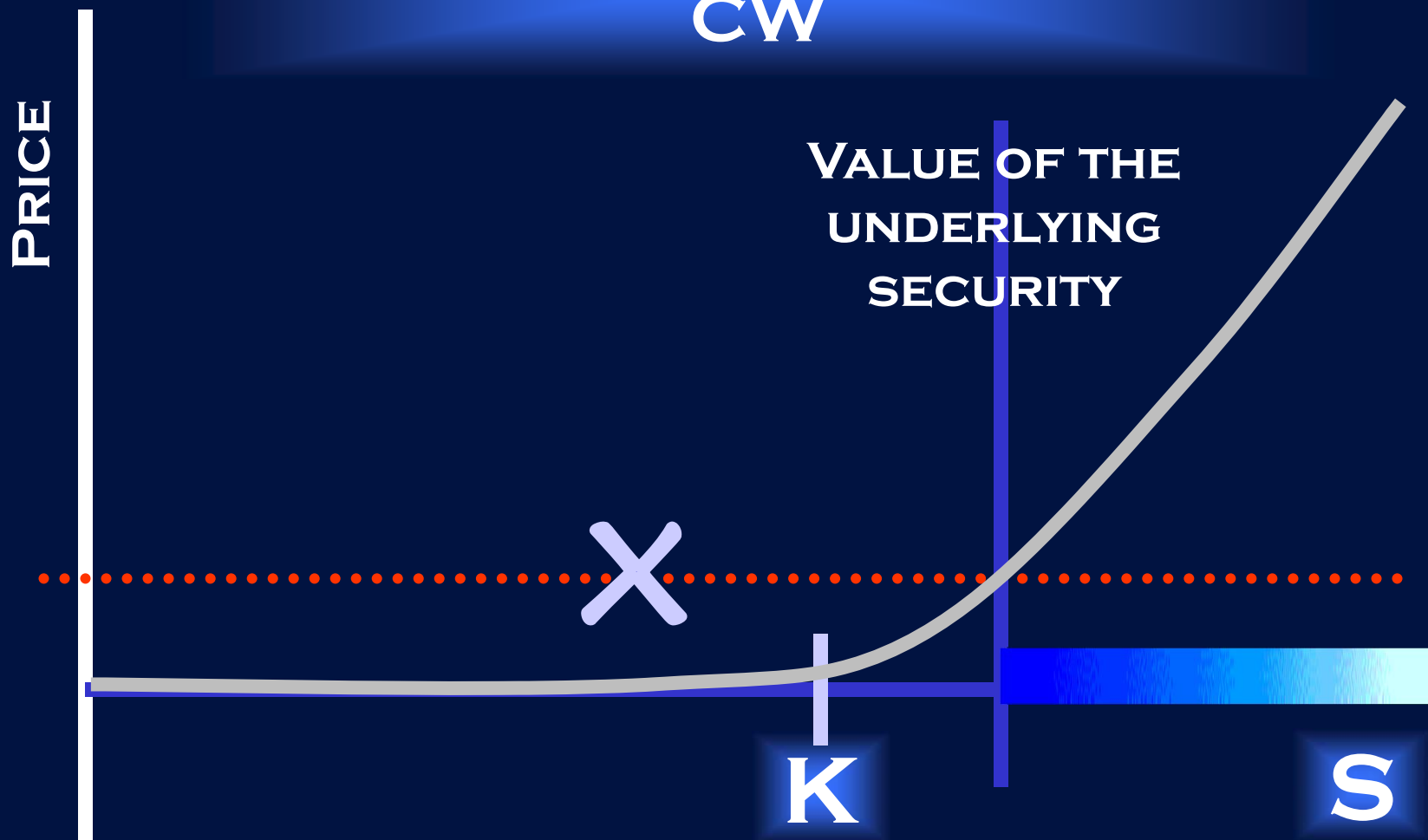
# CW OUT-THE-MONEY – WHAT TO DO AFTER?



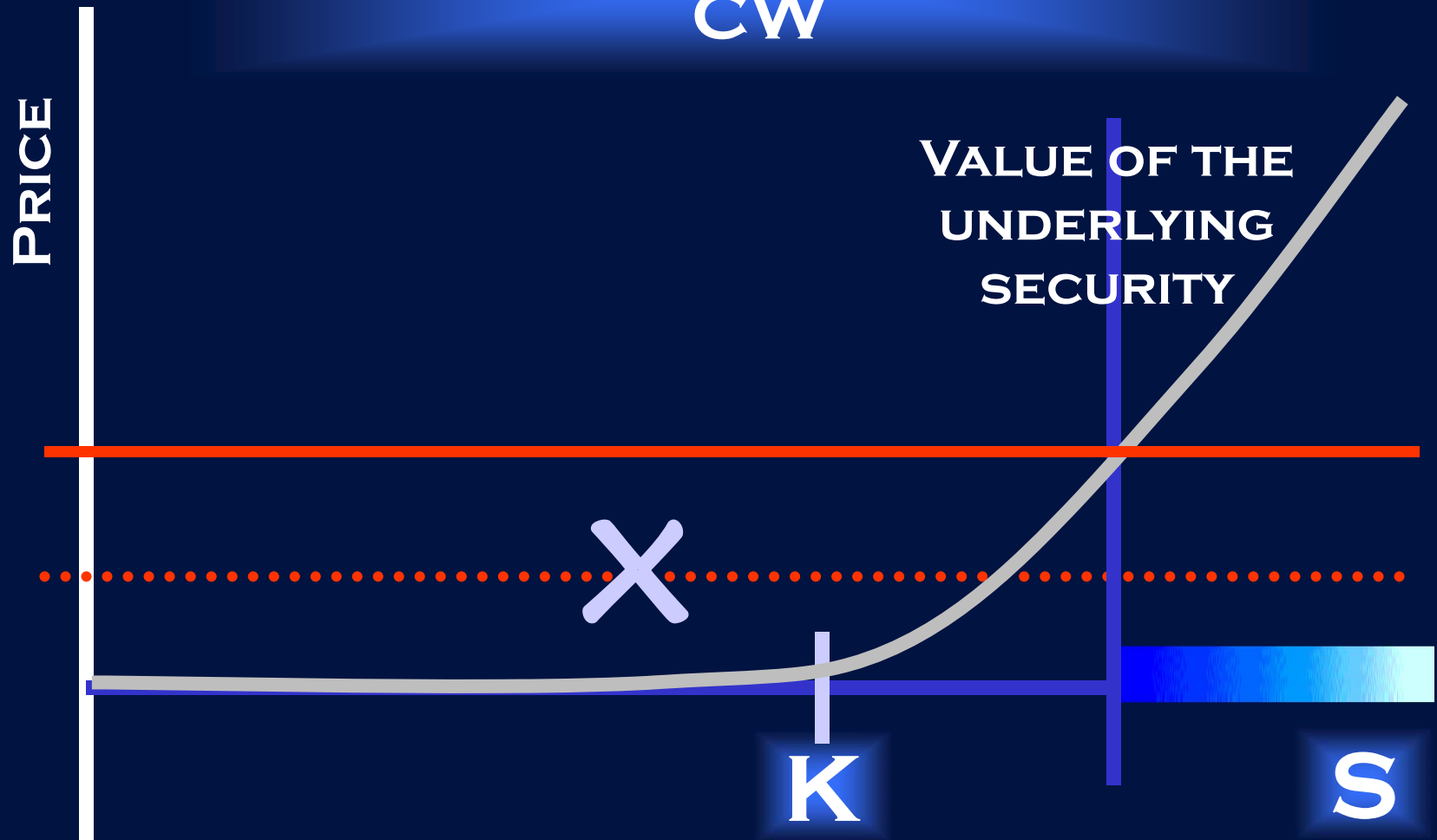
# CW OUT-THE-MONEY – WHAT TO DO AFTER?

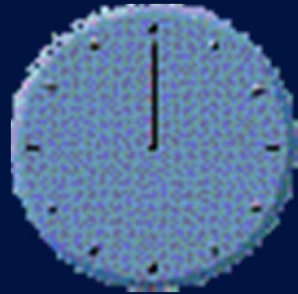


# PURCHASE OF AN OTM CALL CW



# PURCHASE OF AN OTM CALL CW





**PROBLEMS  
REGARDING THE  
TRADING  
INSTRUMENTS**



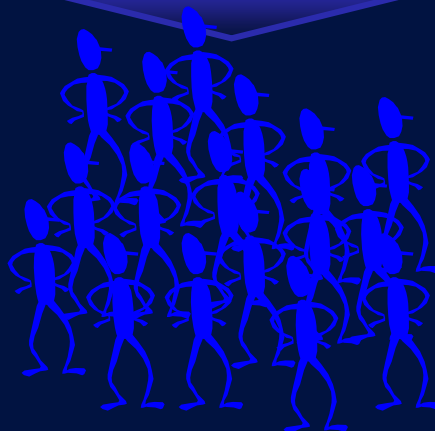
**OTM COVERED WARRANT HARDLY  
RECOVER THE INVESTMENT VALUE**

CW IN-THE-MONEY



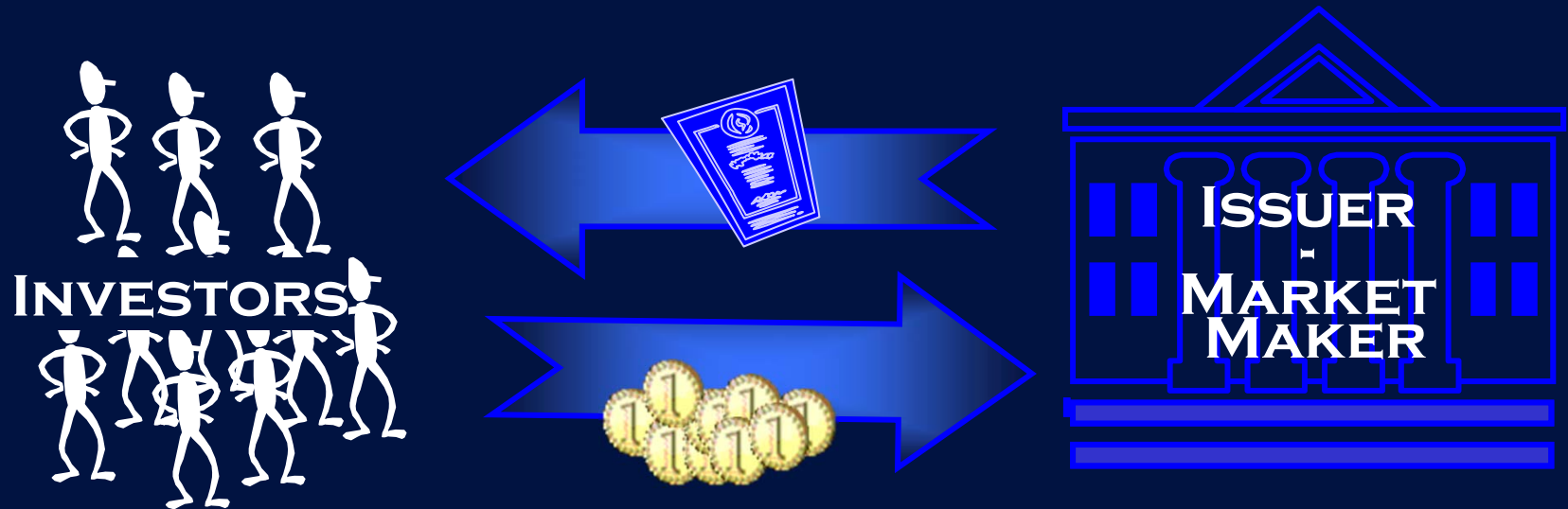
**PROBLEMS REGARDING THE RISK MANAGEMENT**

**OF THE FINANCIAL INSTITUTION**



# EXAMPLE

## FINANCIAL INSTITUTION IS A NET SELLER OF CALLS





CLOSE TO MATURITY ...



HE WILL HOLD IN HIS PORTFOLIO

A LARGE AMOUNT OF THE

STOCKS UNDERLYING THE CALL

AT MATURITY THE OPTION IS ITM.....



HE WILL HOLD IN HIS  
PORTFOLIO ALL THE STOCKS  
UNDERLYING THE CALLS

**IN ORDER TO SETTLE THE OPTION'S PAY-OFF ...**



**HE WILL SELL ALL THE STOCKS.**

**SO CALLED 'RISK UNWINDING'**

## SELLING ALL THE STOCKS ...



HE WILL DRIVE A FALL IN PRICES

**DRIVING A FALL IN PRICES ...**

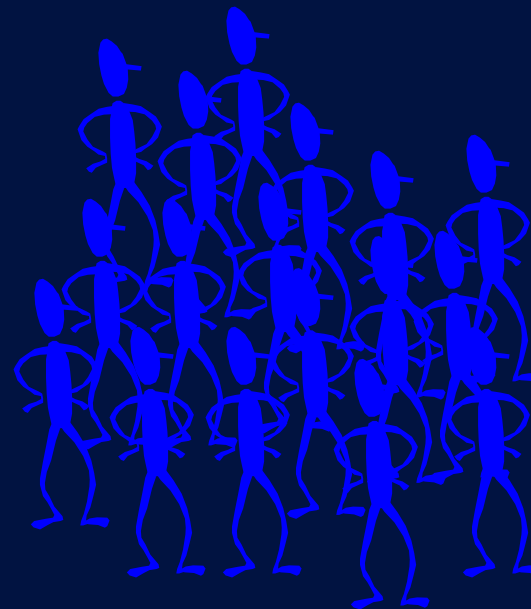
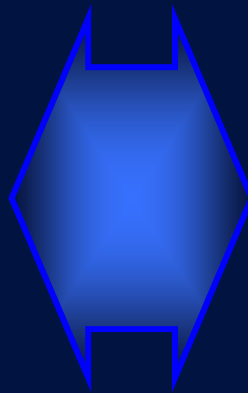


**HE WILL REDUCE THE  
INVESTOR'S POTENTIAL GAIN**

**ALL THE STORY CAN BE SUMMARIZED THROUGH...**

ALL THE STORY CAN BE SUMMARIZED THROUGH...

## DELTA HEDGING ANALYSIS

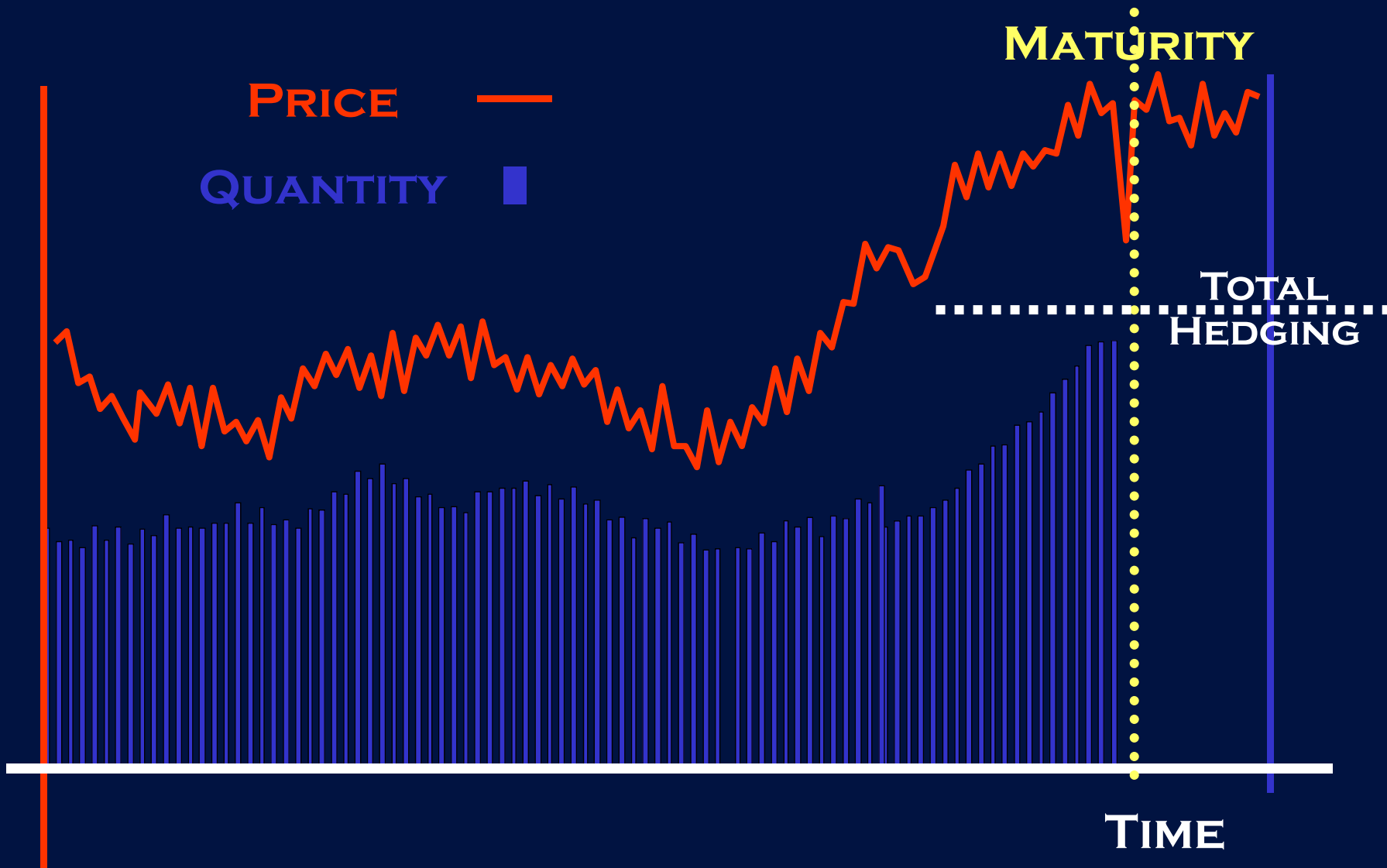


## THE POINT OF VIEW

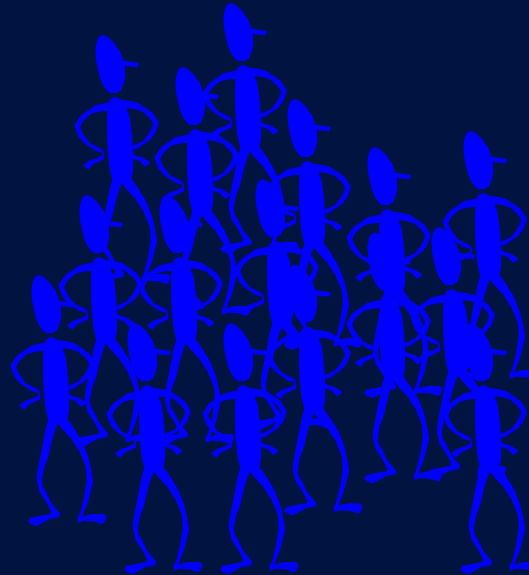




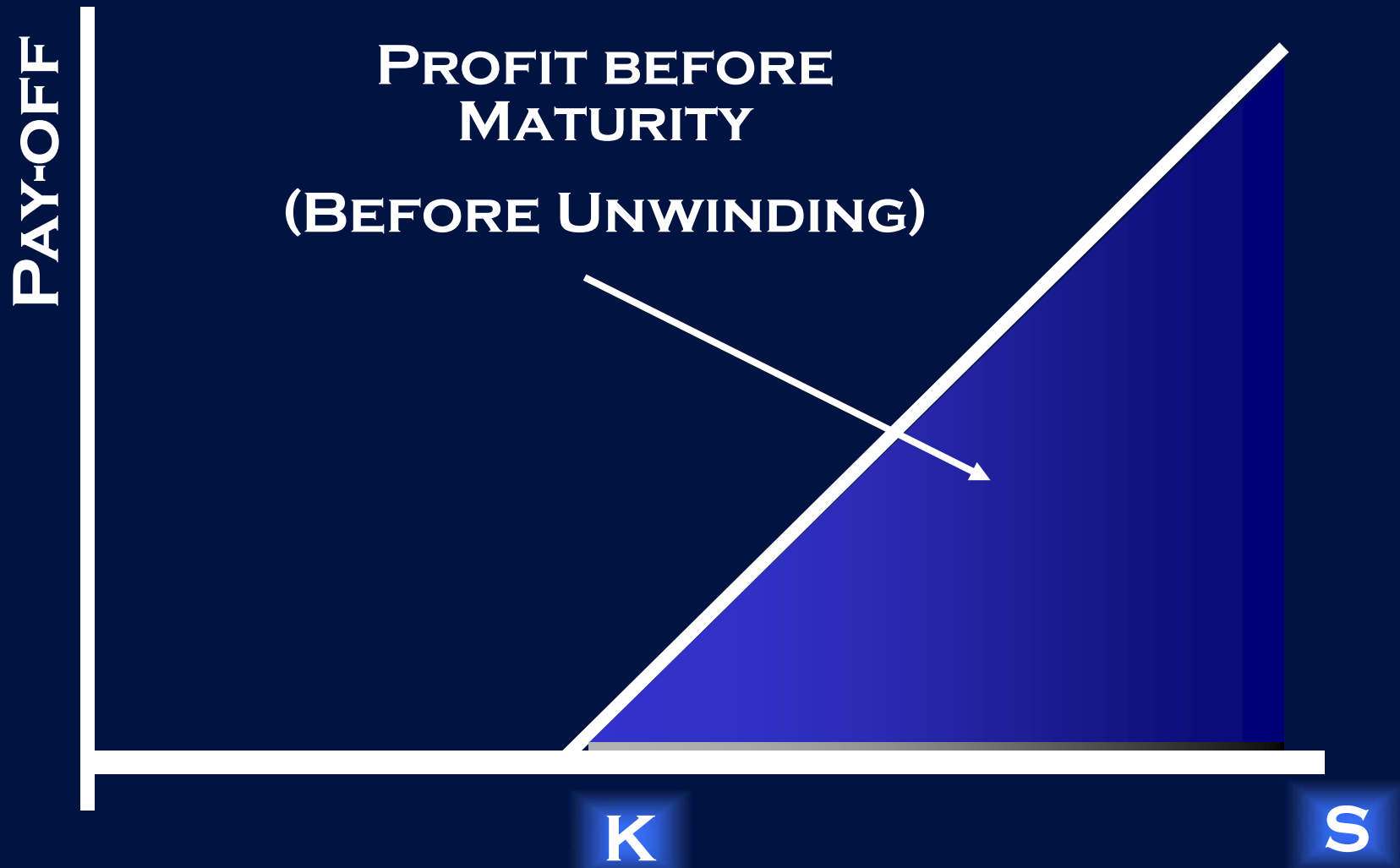
# DELTA HEDGING ON A SHORT CALL POSITION



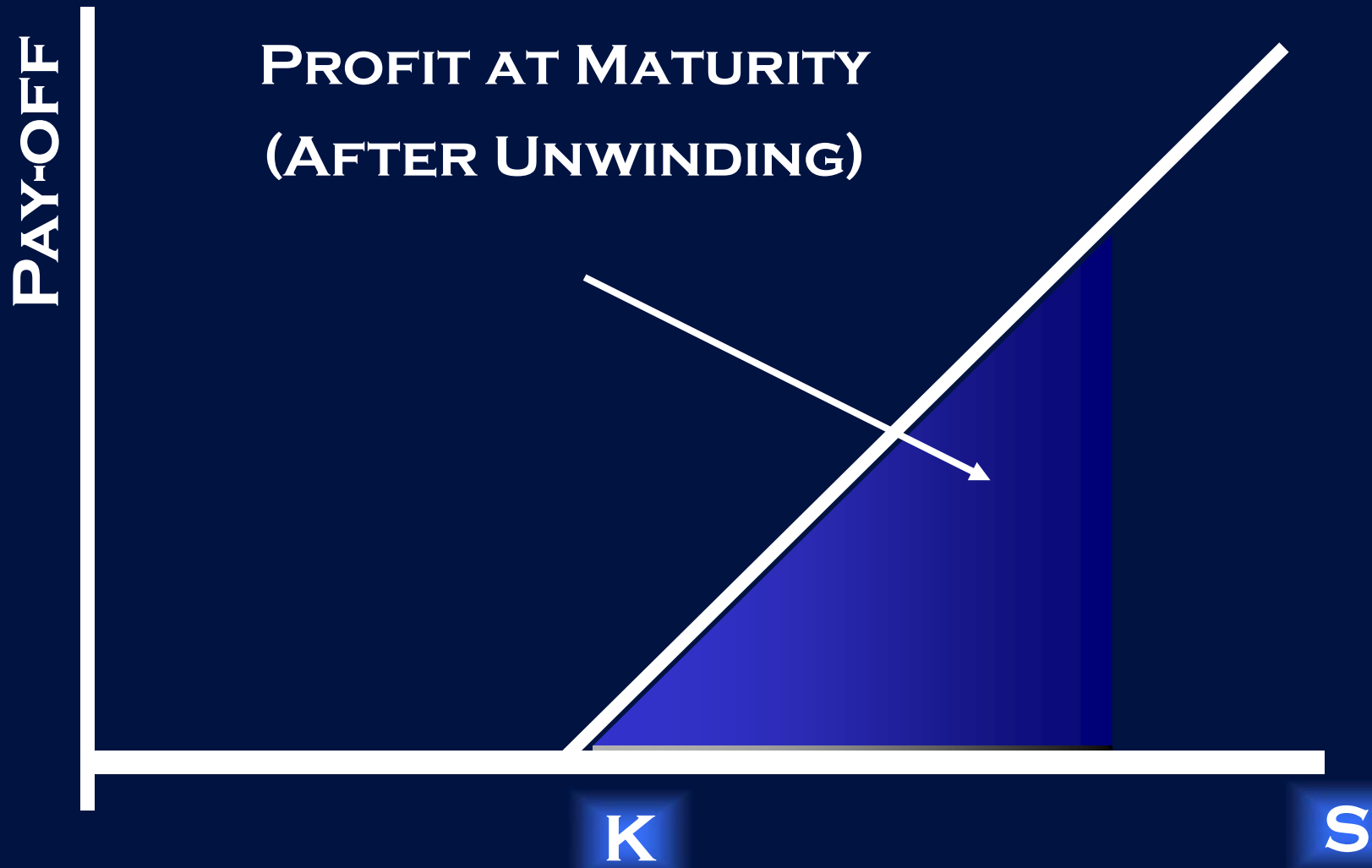
# THE POINT OF VIEW



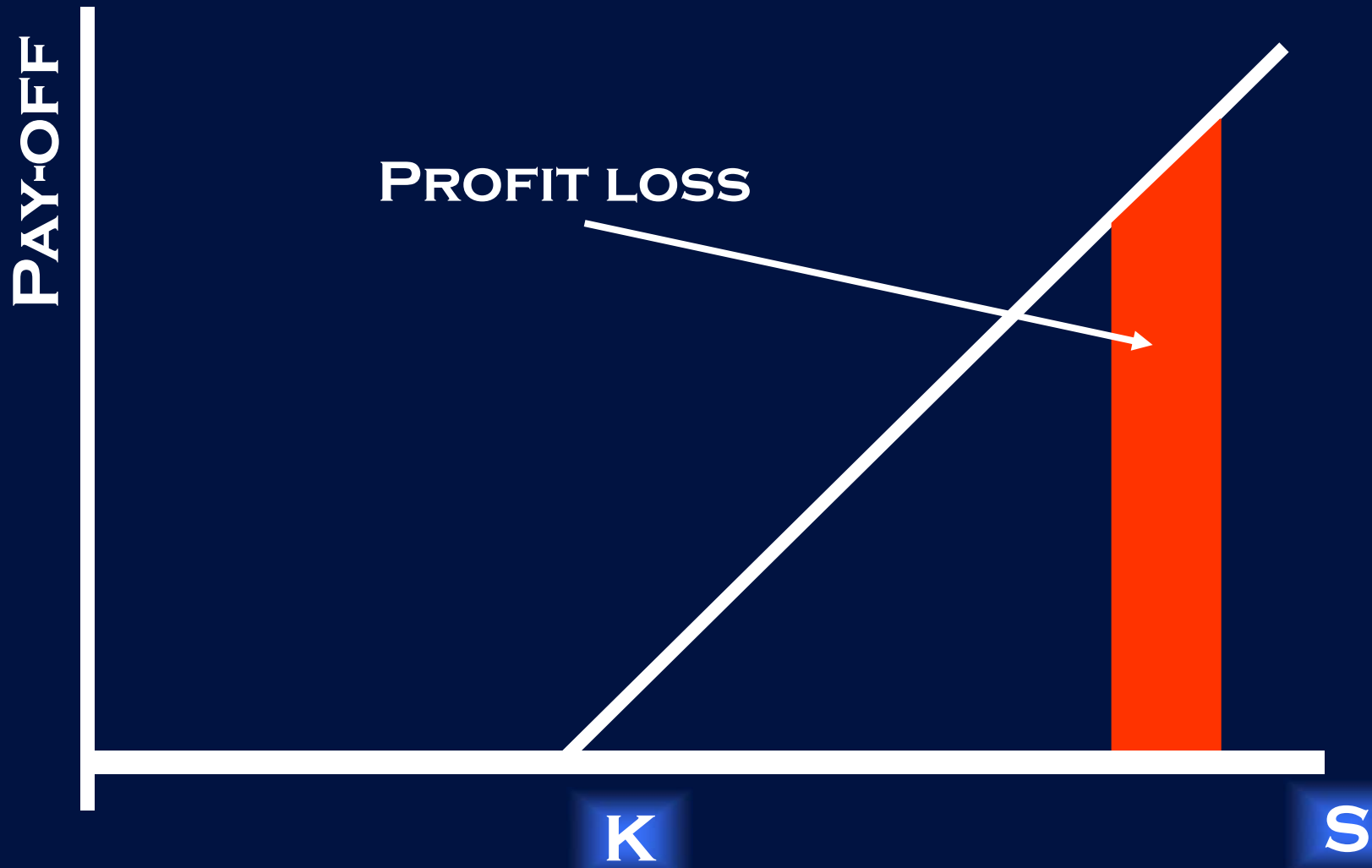
# DELTA HEDGING ON A SHORT CALL POSITION



# DELTA HEDGING ON A SHORT CALL POSITION



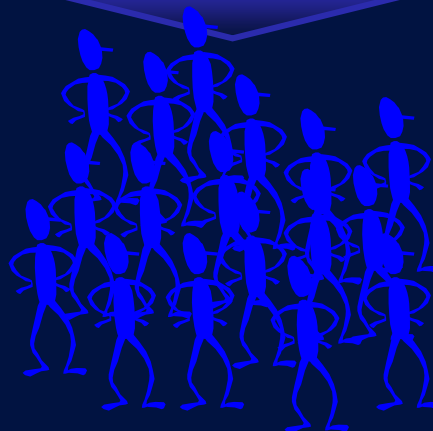
# DELTA HEDGING ON A SHORT CALL POSITION



CW AT-THE-MONEY



PROBLEMS CONNECTED TO THE SO CALLED ‘VIEW’



**THE STOCK IS CLOSE**

**BOTH TO MATURITY AND STRIKE**



**FINANCIAL INSTITUTIONS WILL HAVE**

**TO CHOOSE IF IT IS THE CASE TO**

**COMPLETE OR NOT THE HEDGING**

**(SO CALLED VIEW)**

# PROBLEMS CONNECTED TO THE SO CALLED 'VIEW'

Short 1000 call on 1 stock			Option and $\Delta$				Stock and $\Delta$				$\Delta$ Portfolio
Time Step	Time to Expiration	STOCK PRICE	Option Value	Q. Opz.	$\Delta$ call	$\Delta$ call Posit.	Stock to Buy/(Sell)	Warehouse	$\Delta$ Stock	$\Delta$ Stock Posit.	Total $\Delta$ position
0	0,2500	100,0	10,3776	(1.000)	0,56411596	(564)	564	564	1	564	-
1	0,2375	103,0	11,8661	(1.000)	0,609628	(610)	46	610	1	610	-
2	0,2250	103,7	12,0368	(1.000)	0,6207246	(621)	11	621	1	621	-
3	0,2125	101,7	10,5181	(1.000)	0,58779993	(588)	(33)	588	1	588	-
4	0,2000	96,5	7,4017	(1.000)	0,49399277	(494)	(94)	494	1	494	-
5	0,1875	95,6	6,6706	(1.000)	0,47264412	(473)	(21)	473	1	473	-
6	0,1750	98,0	7,5759	(1.000)	0,51590073	(516)	43	516	1	516	-
7	0,1625	103,7	10,4769	(1.000)	0,62159169	(622)	106	622	1	622	-
8	0,1500	104,0	10,3404	(1.000)	0,62848623	(628)	6	628	1	628	-
9	0,1375	102,0	8,7708	(1.000)	0,58982183	(590)	(38)	590	1	590	-
10	0,1250	99,0	6,7342	(1.000)	0,5231959	(523)	(67)	523	1	523	-
11	0,1125	98,0	5,8476	(1.000)	0,49554047	(496)	(27)	496	1	496	-
12	0,1000	101,0	7,0373	(1.000)	0,56586158	(566)	70	566	1	566	-
13	0,0875	103,0	7,7894	(1.000)	0,61640622	(616)	50	616	1	616	-
14	0,0750	100,5	5,8907	(1.000)	0,55119095	(551)	(65)	551	1	551	-
15	0,0625	98,0	4,0990	(1.000)	0,46817516	(468)	(83)	468	1	468	-
16	0,0500	104,0	6,9440	(1.000)	0,66410039	(664)	196	664	1	664	-
17	0,0375	99,0	3,4276	(1.000)	0,48390678	(484)	(180)	484	1	484	-
18	0,0250	104,0	5,6701	(1.000)	0,70807478	(708)	224	708	1	708	-
19	0,0125	102,0	3,4230	(1.000)	0,65206982	(652)	(56)	652	1	652	-



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13	0,0875	103,0	7,7894	(1.000)	0,61640622	(616)	50	616	1	616	-
14	0,0750	100,5	5,8907	(1.000)	0,55119095	(551)	(65)	551	1	551	-
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17	0,0375	99,0	3,4276	(1.000)	0,48390678	(484)	(180)	484	1	484	-
18	0,0250	104,0	5,6701	(1.000)	0,70807478	(708)	224	708	1	708	-
19	0,0125	102,0	3,4230	(1.000)	0,65206982	(652)	(56)	652	1	652	-
20	0,0000	98,0	-	(1.000)	0	-	(652)	-	1	-	-

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19	0,0125	102,0	3,4230	(1.000)	0,65206982	(652)	(56)	652	1	652	-
20	0,0000	101,0	1,0000	(1.000)	1	(1.000)	348	1.000	1	1.000	-

**A *VIEW*'S MISTAKE CAN CAUSE A HIGH  
COST TO THE FINANCIAL INSTITUTION**



**CASES OF MICROMANIPULATION  
IN ORDER TO MAKE THE *VIEW* 'COME TRUE'**

CASES OF MICROMANIPULATION IN ORDER TO  
MAKE THE *VIEW* 'COME TRUE'



## FINAL REMARKS

## THE QUANT ENFORCEMENT



**EXAMINES**

## CASES OF MICROMANIPULATION

## THE QUANT ENFORCEMENT



**ANALYSIS**

**ACTIVITY OF THE FINANCIAL  
INSTITUTION ...**

## THE QUANT ENFORCEMENT



VERIFY

... THE FINANCIAL INSTITUTION'S PLACING  
WITH REFERENCE TO THE BOUNDS OF  
RISK MANAGEMENT



**... BECAUSE FINANCIAL INSTITUTIONS  
SOMETIMES JUSTIFY THEIR ACTIVITY AS  
CONNECTED TO THE INDICATIONS OF  
RISK MANAGEMENT TOOLS**